

## Role-based Synchronization of Transactions to Prevent Illegal Information Flow

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### Abstract

The role-based access control (RBAC) model is widely used to make systems secure. Even if every access request is authorized in the roles, illegal information flow might occur as the well known confinement problem. In this paper, we define types of information flow relations, legal (LIF), illegal (IIF), and possibly illegal (PIF) ones  $R_1 \Rightarrow R_2$ ,  $R_1 \Leftarrow R_2$ , and  $R_1 \rightarrow R_2$  among a pair of role families  $R_1$  and  $R_2$ , respectively. In addition, we discuss a mechanism to prevent illegal information flow where each object just keeps a role family of a transaction which has most recently manipulated the object.

### 役割の概念を用いた情報流制御方式

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役割 (Role) の概念は、安全な情報システムを設計、実装するための重要な概念である。役割とは、対象世界の業務に対応し、アクセス権限の集合として定義される。ロールベースアクセス制御方式は、利用者とオブジェクト間でのアクセス制御は行えるが、利用者間での情報流を制御することができない。本研究では、トランザクションの目的と利用者の役割の概念を基に利用者間の情報流を制御する新たな方式を提案する。

## 1 Introduction

Information systems have to be consistent and secure in presence of various kinds of security attacks and conflicting accesses from multiple transactions to resources. In the access control models [2], only a subject  $s$  is allowed to issue a method  $op$  to an object  $o$  only if an access right  $(o, op)$  is granted to the subject  $s$ . In the mandatory access control model [6], only an authorizer can grant access rights to subjects. On the other hand, a subject granted an access right can grant the access right to another subject in the discretionary access control model [2]. In the role-based access control (RBAC) models [5, 8], a role is specified in a collection of access rights, which shows what subjects playing the role can do on resource objects in an enterprise. While the access control models are widely used in information systems, illegal information flow among subjects through objects may occur even if each subject can safely manipulate objects according to the access rights. This is a well-known *confinement* problem [3]. In the lattice-based access control (LBAC) model [6], each entity, i.e. subject and object is classified into a security class. Information flow relation among security classes is defined. Access rules on read, write, and modify are defined according to the information flow relation. However, resource objects can be only manipulated in limited ways.

In traditional database systems, the two-phase locking (2PL) protocol [1] is widely used to synchronize conflicting transactions. If a transaction  $T$  holds an object, every transaction conflicting with the transaction  $T$  cannot use the object, i.e. waits until the object is released by the transaction  $T$ . On the other hand, each transaction  $T$  is assigned with timestamp  $TS(T)$  showing when the transaction  $T$  is initiated in the timestamp

ordering (TO) scheduler [1]. If a pair of transactions  $T_1$  and  $T_2$  issue conflicting methods  $op_1$  and  $op_2$  to an object  $o$ , respectively,  $op_1$  is performed prior to  $op_2$  if  $TS(T_1) < TS(T_2)$ . Objects are thus manipulated by conflicting transactions in the timestamp order and no deadlock occurs. We also discuss types of role-ordering (RO) schedulers to perform a method from a transaction with a more significant role prior to another transaction with a less significant role are also discussed [4]. In the RO scheduler, general abstract types of methods are supported by each object and the discretionary model is taken. In this paper, we discuss a simpler model where every object supports only *read* and *write* methods. In addition, we consider the mandatory model.

In the role-based access control model, the transaction  $T$  is assigned with a subfamily of the roles granted to the subject  $s$ . The subfamily of the roles is referred to as *purpose* of the subject  $s$  to perform the transaction  $T$ . Let  $T_1$  and  $T_2$  be a pair of transactions with purposes  $R_1$  and  $R_2$ , respectively. Suppose  $T_1$  writes an object  $y$  after reading an object  $x$  and then  $T_2$  reads the object  $y$ . Here, if  $T_2$  is not granted an access right  $(x, read)$ ,  $T_2$  illegally reads  $x$ 's data from the object  $y$ , i.e. illegal information flow occur. In this paper, we define types of information flow relations, legal (LIF), illegal (IIF), and possibly illegal (PIF) ones  $R_1 \Rightarrow R_2$ ,  $R_1 \Leftarrow R_2$ , and  $R_1 \rightarrow R_2$  among a pair of role families  $R_1$  and  $R_2$ , respectively. Then, we discuss how to schedule multiple conflicting transactions concurrently issued and how to perform conflicting methods on each object so as to prevent illegal information flow.

In section 2, we present a system model. In section 3, we define the types information flow relations among roles. In section 4, we discuss the concurrency control algorithm of multiple transactions to prevent illegal in-

formation flow and serialize conflicting methods from transactions.

## 2 System Model

### 2.1 Role-based access control (RBAC) model

Let  $S$  be a set of subjects in a system. An object is an entity which performs methods issued by subjects. Let  $O$  be a set of objects  $o_1, \dots, o_m$  in a system. Each object  $o_i$  is assumed to support *read* and *write* methods for manipulating data in  $o_i$  ( $i = 1, \dots, m$ ). Only a subject  $s$  granted an access right  $\langle o, op \rangle$  is allowed to issue a method  $op$  to an object  $o$  in the access control models [2, 6–8]. In the RBAC models [5, 8], a role is specified in a set of access rights. A *role* shows a job function in an enterprise. Let  $R$  be a set of roles  $\{r_1, \dots, r_n\}$  in a system. Each role  $r_i$  is a collection  $\{\alpha_{i1}, \dots, \alpha_{il_i}\}$  ( $l_i \geq 1$ ) of access rights. Let  $SR(s) (\subseteq R)$  be a family of roles granted to a subject  $s$ . That is, the subject  $s$  plays roles  $SR(s)$ . Suppose a subject  $s$  initiates a transaction  $T$ . Here,  $T$  is assigned with a subfamily  $PR(T)$  of the roles granted to the subject  $s$  ( $\subseteq SR(s)$ ).  $PR(T)$  is referred to as *purpose* [4] of the subject  $s$  to issue the transaction  $T$ .

The access control models imply the *confinement problem* [3]. For example, a subject  $s_1$  is granted a pair of access rights  $\langle f, read \rangle$  and  $\langle g, write \rangle$  on file objects  $f$  and  $g$  while another subject  $s_2$  is only granted an access right  $\langle g, read \rangle$ . Suppose the subject  $s_1$  reads data  $x$  from the file  $f$  and then writes  $x$  to the file  $g$ . Here, the subject  $s_2$  can read the data  $x$  from the file  $g$  although  $s_2$  is not allowed to read the data  $x$  in the file  $f$ . Here, information  $x$  in the file object  $f$  *illegally flows* to the subject  $s_2$  [Figure 1].

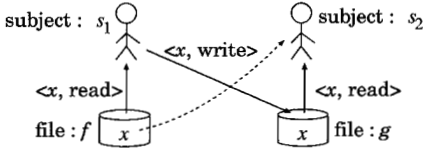


Figure 1. Illegal information flow.

### 2.2 Transactions

A *write* method *conflicts* with *write* and *read* methods while a *read* method conflicts with *write* on an object. A pair of transactions which issue conflicting methods are referred to as *conflict* with one another. Let  $T$  be a set  $\{T_1, \dots, T_m\}$  of transactions which are concurrently performed. A *schedule*  $S$  of the transaction set  $T$  shows a history of methods which are issued by the transactions in the set  $T$ . The precedent relation  $\rightarrow$  on transactions is defined as follows [1]:

**[Definition]** A transaction  $T_i$  *precedes* a transaction  $T_j$  in a schedule  $S$  of the transaction set  $T$  ( $T_i \rightarrow T_j$ ) iff (and only if) one of the following conditions holds:

1. A method  $op_i$  issued by the transaction  $T_i$  is performed prior to a method  $op_j$  of the transaction  $T_j$  if the method  $op_i$  conflicts with the method  $op_j$ .

2.  $T_i \rightarrow T_k \rightarrow T_j$  for some transaction  $T_k$  in  $T$ .

A pair of transactions  $T_i$  and  $T_j$  are *independent* ( $T_i \parallel T_j$ ) iff neither  $T_i \rightarrow T_j$  nor  $T_j \rightarrow T_i$ . A schedule  $S$  is *serializable* iff the precedent relation  $\rightarrow$  of the transactions in the schedule  $S$  is acyclic. Conflicting transactions should be performed in a serializable schedule to keep objects consistent. In the locking protocols like two-phase locking protocols [1], transactions arbitrarily hold objects based on the first-come-first-served principle. If some transaction  $T_i$  holds an object  $o$ , the other transactions which would like to use the object  $o$  have to wait for release of the object  $o$ . In addition, deadlock might occur. In the timestamp ordering (TO) schedulers [1], transactions are totally ordered in their timestamps. Each transaction is assigned with timestamp showing when the transaction is initiated. Objects are manipulated by conflicting transactions in the timestamp order. That is, the elder a transaction is, the earlier the transaction holds an object. No deadlock occurs in the TO scheduler.

## 3 Information Flow Relations

### 3.1 Transactions

We discuss what information flow to occur by performing transactions. For each role  $r$  in  $R$ , let  $In(r)$  and  $Out(r)$  be *input* and *output* sets of objects  $\{o \mid \langle o, read \rangle \in r\}$  and  $\{o \mid \langle o, write \rangle \in r\}$  for a role  $r$ , respectively. Let  $In(R)$  and  $Out(R)$  be  $\bigcup_{r \in R} In(r)$  and  $\bigcup_{r \in R} Out(r)$ , respectively. Let  $In(T)$  and  $Out(T)$  show  $r \in R$  *input* and *output* sets of objects which a transaction  $T$  in the set  $T$  reads and writes, respectively. Here,  $In(T) \subseteq In(PR(T))$  and  $Out(T) \subseteq Out(PR(T))$  where  $PR(T)$  is a purpose of a transaction  $T$ .

**[Definition]** A transaction  $T_2$  *reads* from another transaction  $T_1$  in a schedule  $S$  ( $T_1 \vdash T_2$ ) iff one of the following conditions holds:

1.  $T_1$  precedes  $T_2$  in  $S$  ( $T_1 \rightarrow T_2$ ) and  $Out(T_1) \cap In(T_2) \neq \emptyset$ .
2.  $T_1 \vdash T_3 \vdash T_2$  for some transaction  $T_3$ .

We define the illegal information flow to occur by performing transactions.

**[Definition]** A transaction  $T_2$  *illegally reads* from a transaction  $T_1$  in a schedule  $S$  ( $T_1 \leftrightarrow T_2$ ) iff the following conditions hold:

1.  $T_1 \vdash T_2$  in  $S$ .
2.  $In(T_1) - In(PR(T_2)) \neq \emptyset$ .

The first condition shows that data written by a transaction  $T_1$  might be read by another transaction  $T_2$ . The second condition means that a transaction  $T_2$  is not granted an access right to read some object read by another transaction  $T_1$ . That is, a transaction  $T_2$  might read data in an object on which the transaction  $T_2$  has no read access right. In a schedule of the set  $T$ , illegal information flow occur iff there are a pair of transactions  $T_1$  and  $T_2$  such that the transaction  $T_2$  illegally reads from the transaction  $T_1$  ( $T_1 \leftrightarrow T_2$ ) in  $T$ .

**[Definition]** A transaction  $T_2$  legally reads from a transaction  $T_1$  in schedule  $S$  ( $T_1 \Rightarrow T_2$ ) iff the following conditions hold:

1.  $T_1 \vdash T_2$ .
2.  $In(T_1) \subseteq In(PR(T_2))$ .

**[Example 1]** Let us consider the following roles  $ra$ ,  $rb$ ,  $rc$ , and  $rd$  on four objects  $x$ ,  $y$ ,  $z$ , and  $w$ ;

$$\begin{aligned} ra &= \{\langle x, read \rangle, \langle y, read \rangle, \langle y, write \rangle, \langle w, write \rangle\}. \\ rb &= \{\langle x, write \rangle, \langle x, read \rangle, \langle y, read \rangle, \langle z, read \rangle\}. \\ rc &= \{\langle y, write \rangle, \langle z, read \rangle, \langle w, write \rangle\}. \\ rd &= \{\langle y, read \rangle, \langle w, read \rangle\}. \end{aligned}$$

Here,  $In(ra) = \{x, y\}$ ,  $Out(ra) = \{y, w\}$ ,  $In(rb) = \{x, y, z\}$ ,  $Out(rb) = \{x\}$ ,  $In(rc) = \{z\}$ ,  $Out(rc) = \{y, w\}$ ,  $In(rd) = \{y, w\}$ , and  $Out(rd) = \phi$ . Suppose four transactions  $T_1, T_2, T_3$ , and  $T_4$  are initiated with roles  $ra$ ,  $rb$ ,  $rc$ , and  $rd$ , respectively. Let us first consider a pair of the transactions  $T_1$  and  $T_2$ . The transaction  $T_1$  can read a pair of the objects  $x$  and  $y$  and write a pair of the objects  $y$  and  $w$  since the role  $ra$  is assigned to  $T_1$ . On the other hand, the transaction  $T_2$  can read the objects  $x$ ,  $y$ , and  $z$  and write the object  $x$ . Here, suppose the transaction  $T_1$  is performed prior to the other transaction  $T_2$ , i.e.  $T_1$  precedes  $T_2$  ( $T_1 \rightarrow T_2$ ) in a schedule  $S$  of the transactions. That is, the transaction  $T_1$  writes the object  $y$  after reading the object  $x$  and then the transaction  $T_2$  reads the object  $y$  ( $T_1 \mapsto T_2$ ) as shown in Figure 2. Here, data  $v$  in the object  $x$  might be brought into the object  $y$  by the transaction  $T_1$ . The data  $v$  can be read by reading the object  $y$ . Since the role  $rb$  includes an access right  $\langle y, read \rangle$ , the transaction  $T_2$  can obtain the data in the object  $x$  and can read the object  $y$ . Thus, no illegal information flow occur if transactions with the role  $ra$  precede transactions with role  $rb$ . However, the transaction  $T_4$  cannot read the object  $y$  after performing  $T_1$  because  $T_4$  is not granted an access right  $\langle x, read \rangle$  in the role  $rd$ . That is,  $T_1 \not\leftrightarrow T_4$ .

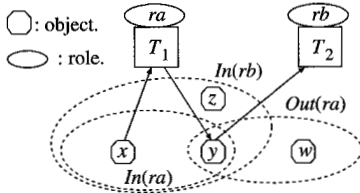


Figure 2. Information flow on roles.

### 3.2 Information Flow Relations

We define a legal information flow (LIF) relation among roles as follows:

**[Definition]** A role  $r_1$  legally flows into a role  $r_2$  ( $r_1 \Rightarrow r_2$ ) iff one of the following conditions holds:

1.  $Out(r_1) \cap In(r_2) \neq \phi$  and  $In(r_1) \subseteq In(r_2)$
2.  $r_1 \Rightarrow r_3 \Rightarrow r_2$  for some role  $r_3$ .

A role  $r_1$  is legally equivalent with a role  $r_2$  ( $r_1 \equiv r_2$ ) iff  $r_1 \Rightarrow r_2$  and  $r_2 \Rightarrow r_1$ . Based on the legal information flow relation  $\Rightarrow$  among roles, a least upper

bound (lub)  $r_1 \sqcap^{LIF} r_2$  of roles  $r_1$  and  $r_2$  is defined to be a role  $r_3$  such that  $r_1 \Rightarrow r_3$ ,  $r_2 \Rightarrow r_3$ , and there is no role  $r_4$  such that  $r_1 \Rightarrow r_4 \Rightarrow r_3$  and  $r_2 \Rightarrow r_4 \Rightarrow r_3$ . A greatest lower bound (glb)  $r_1 \sqcup^{LIF} r_2$  is also defined to be a role  $r_3$  such that  $r_3 \Rightarrow r_1$ ,  $r_3 \Rightarrow r_2$ , and there is no role  $r_4$  such that  $r_3 \Rightarrow r_4 \Rightarrow r_1$  and  $r_3 \Rightarrow r_4 \Rightarrow r_2$ . Thus, a lattice  $(\mathbf{R}, \Rightarrow, \sqcup^{LIF}, \sqcap^{LIF})$  is defined for a set  $\mathbf{R}$  of roles and the legal information flow relation  $\Rightarrow$  in a system. Here, the bottom  $\perp^{LIF}$  is  $\phi$  and the top  $\top^{LIF}$  is in a set  $\mathbf{R}$  of all the roles.

**[Definition]** A role  $r_1$  is legally independent of a role  $r_2$  ( $r_1 \parallel r_2$ ) iff one of the following conditions holds:

1.  $Out(r_1) \cap In(r_2) = \phi$
2.  $r_2 \parallel r_1$ .

It is noted that the legal information flow relation is transitive but the independent relation is not transitive.

In the example 1,  $Out(ra) \cap In(rb) = \{y\} \neq \phi$  and  $In(ra) (= \{x, y\}) \subseteq In(rb) (= \{x, y, z\})$ . Hence,  $ra \Rightarrow rb$ .  $rb \parallel rc$  since  $Out(rb) (= \{x\}) \cap In(rc) (= \{z\}) = \phi$ .

The illegal information flow (IIF) relation  $\not\leftrightarrow$  of transactions satisfies the following property:

**[Theorem]** Let  $T_1$  and  $T_2$  be a pair of transactions with roles  $r_1$  and  $r_2$ , respectively. " $T_1 \not\leftrightarrow T_2$ " does not hold if the following conditions hold:

1.  $r_1 \parallel r_2$ .
2.  $r_1 \Rightarrow r_2$  and  $T_1 \rightarrow T_2$ .

**[Proof]** If  $r_1 \parallel r_2$ , it is trivial that  $T_1 \not\leftrightarrow T_2$  holds. Next, assume  $r_1 \Rightarrow r_2$  and  $T_1 \rightarrow T_2$ . Here,  $T_2$  is allowed to read every object read by  $T_1$  according to the definition. Hence,  $T_1 \not\leftrightarrow T_2$ .

This theorem means that no illegal information flow occur if a transaction with a role  $r_1$  precedes every transaction with a role  $r_2$  and  $r_1 \Rightarrow r_2$ . Next, let us consider a pair of the transactions  $T_1$  and  $T_4$  with the roles  $ra$  and  $rd$ , respectively, in the example 1. If the transaction  $T_1$  writes the object  $w$  after reading the object  $y$  and then the transaction  $T_4$  reads the object  $w$ , there is no illegal information flow since the transaction  $T_4$  is granted a read right  $\langle y, read \rangle$  in the role  $rd$  as shown in Figure 3. However, if the transaction  $T_1$  writes the object  $w$  after reading the object  $x$ , illegal information flow occur since the transaction  $T_4$  is not granted a read right  $\langle x, read \rangle$  in the role  $rd$ . Thus, it depends on which objects are read and written in transactions whether or not illegal information flow to occur.

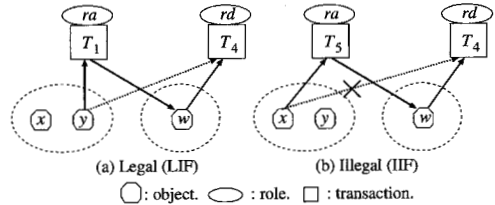


Figure 3. Information flow relations.

**[Definition]** A role  $r_1$  possibly illegally flows into a



role  $r_2$  ( $r_1 \mapsto r_2$ ) iff one of the following conditions holds:

1.  $Out(r_1) \cap In(r_2) \neq \phi$  and  $In(r_1) - In(r_2) \neq \phi$ .
2.  $r_1 \mapsto r_3 \mapsto r_2$  for some role  $r_3$ .

Figure 4 shows possible types of illegal information flow relations of roles  $r_1$  and  $r_2$ .

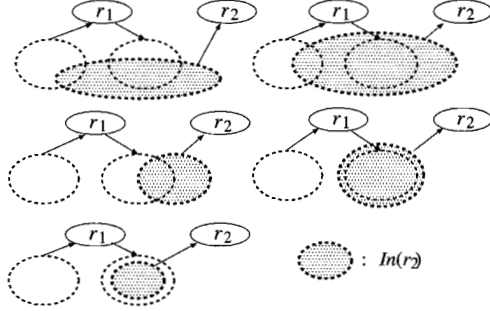


Figure 4. PIF relation ( $r_1 \mapsto r_2$ ).

In the example 1, the role  $ra$  legally flows into the role  $rd$  ( $ra \Rightarrow rd$ ). Let  $T_1$  and  $T_2$  be a pair of transactions with roles  $r_1$  and  $r_2$ , respectively. Suppose the transaction  $T_1$  precedes the transaction  $T_2$  ( $T_1 \rightarrow T_2$ ) in a schedule. If the role  $r_1$  legally flows into the role  $r_2$  ( $r_1 \Rightarrow r_2$ ), there is no illegal information flow to occur even if each transaction issues any method of the roles in any order. However, if  $r_1 \mapsto r_2$ , illegal information flow might occur depending on which methods the transactions issue in which order.

**[Definition]** A role  $r_1$  *illegally flows* into a role  $r_2$  ( $r_1 \hookrightarrow r_2$ ) iff  $In(r_1) \cap In(r_2) = \phi$  and  $Out(r_1) = In(r_2)$ .

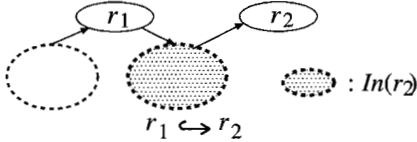


Figure 5. IIF relation.

**[Definition]** A role  $r_1$  *possibly illegally flow* into a role  $r_2$  ( $r_1 \mapsto r_2$ ) iff one of the following conditions holds:

1.  $r_1 \hookrightarrow r_2$ .
2.  $In(r_1) \cap In(r_2) = \phi$  and  $r_1 \mapsto r_3 \mapsto r_2$  for some role  $r_3$ .

In the example 1, let us consider a pair of the transactions  $T_3$  and  $T_4$  with roles  $rc$  and  $rd$ , respectively. Here,  $Out(rc) = In(rd) = \{y, w\}$ . Since  $In(r_1) = \{z\}$ ,  $In(r_1) \cap In(r_2) = \phi$ . Here, the role  $rc$  necessarily illegally flows into the role  $rd$  ( $rc \hookrightarrow rd$ ).

**[Theorem]** A transaction  $T_2$  *illegally reads* from another transaction  $T_1$  in a schedule  $S$  ( $T_1 \hookrightarrow T_2$ ) iff the following conditions hold:

1.  $r_1 \hookrightarrow r_2$  where  $PR(T_1) = \{r_1\}$  and  $PR(T_2) = \{r_2\}$ .

2.  $T_1 \vdash T_2$  and no transaction  $T_3$  such that  $T_1 \vdash T_3 \vdash T_2$  in the schedule  $S$ .
3.  $In(T_1) \neq \phi$  and  $In(T_2) \neq \phi$ .

**[Definition]** A transaction  $T_1$  *possibly illegally reads* from a transaction  $T_2$  in a schedule  $S$  ( $T_1 \mapsto T_2$ ) iff one of the following conditions hold:

1.  $T_1 \hookrightarrow T_2$ .
2.  $T_1 \Rightarrow T_3 \hookrightarrow T_2$  for some transaction  $T_3$  and  $In(T_1) \cap In(T_2) = \phi$ .

The following properties hold for the information flow relations  $\Rightarrow$ ,  $\mapsto$ ,  $\parallel$ , and  $\mapsto$  of roles:

1.  $r_1 \Rightarrow r_3$  if  $r_1 \Rightarrow r_2 \Rightarrow r_3$ .
2.  $r_1 \mapsto r_3$  if  $r_1 \mapsto r_3 \mapsto r_2$ .
3.  $r_1 \mapsto r_3$  if  $r_1 \mapsto r_2 \mapsto r_3$  or  $r_1 \Rightarrow r_2 \mapsto r_3$ .
4.  $r_1 \mapsto r_3$  if  $r_1 \hookrightarrow r_2 \Rightarrow r_3$ .
5.  $r_1 \parallel r_3$  if  $r_1 \Rightarrow r_2 \hookrightarrow r_3$ .
6.  $r_1 \mapsto r_3$  if  $r_1 \mapsto r_2 \hookrightarrow r_3$ .
7.  $r_1 \mapsto r_2$  if  $r_1 \hookrightarrow r_2$ .

With respect to the illegal information flow relation  $\hookrightarrow$  of roles, we define the *lub*  $r_1 \sqcup^{II} r_2$  and *glb*  $r_1 \sqcap^{II} r_2$  of a pair of roles  $r_1$  and  $r_2$  similarly to the *lub*  $\sqcup^{LI}$  and *glb*  $\sqcap^{LI}$ . We also define a lattice  $\langle \mathbf{R}, \hookrightarrow, \sqcup^{II}, \sqcap^{II} \rangle$  is defined for a set  $\mathbf{R}$  of roles and the illegal information flow relation  $\hookrightarrow$ . The bottom  $\perp^{II}$  is  $\phi$  and the top  $\top^{II}$  is in a set  $R$  of all the roles. A lattice  $\langle \mathbf{R}, \mapsto, \sqcup^{PI}, \sqcap^{PI} \rangle$  is also defined for the possibly illegal (PI) information flow relation  $\mapsto$ .

### 3.3 Information flow on role families

Let  $SR(s) (\subseteq R)$  show a family of roles granted to a subject  $s$ . If a subject  $s$  is granted three roles  $r_1$ ,  $r_2$ , and  $r_3$ ,  $SR(s) = \{r_1, r_2, r_3\}$ . A transaction  $T$  issued by a subject  $s$  is assigned a purpose  $PR(T) (\subseteq SR(s))$ . The subject  $s$  assigns a transaction  $T$  with a pair of the roles  $r_1$  and  $r_2$  in  $SR(s)$  and then issues the transaction  $T$ , i.e. the purpose  $PR(T)$  is  $\{r_1, r_2\}$ . We discuss the information flow relations among role families.

- A role family  $R_1$  *legally flows* into a role family  $R_2$  ( $R_1 \Rightarrow R_2$ ) iff one of the following conditions holds:

1.  $\sqcup_{r_1 \in R_1}^{LI} r_1 \Rightarrow \sqcap_{r_2 \in R_2}^{LI} r_2$ .
2.  $R_1 \Rightarrow R_3 \Rightarrow R_2$  for some role family  $R_3$ .

- A role-family  $R_1$  is *legally equivalent* with a role family  $R_2$  with respect to the legal information flow (LI) relation  $\Rightarrow$  ( $R_1 \equiv^{LI} R_2$ ) iff  $R_1 \Rightarrow R_2$  and  $R_2 \Rightarrow R_1$ .

- A role family  $R_1$  *illegally flows* into a role family  $R_2$  ( $R_1 \hookrightarrow R_2$ ) iff one of the following conditions holds:

1.  $\sqcup_{r_1 \in R_1}^{II} r_1 \hookrightarrow \sqcap_{r_2 \in R_2}^{II} r_2$ .
2.  $R_1 \hookrightarrow R_3 \hookrightarrow R_2$  for some role family  $R_3$ .

- $R_1$  *possibly illegally flows* into  $R_2$  ( $R_1 \mapsto R_2$ ) iff one of the following conditions holds:

1.  $\sqcup_{r_1 \in R_1}^{PI} r_1 \mapsto \sqcap_{r_2 \in R_2}^{PI} r_2$ .
2.  $R_1 \mapsto R_3 \mapsto R_2$  for some role family  $R_3$ .

- $R_1$  is independent of  $R_2$  ( $R_1 \parallel R_2$ ) iff neither  $R_1 \Rightarrow R_2$ ,  $R_2 \Rightarrow R_1$ ,  $R_1 \mapsto R_2$ , nor  $R_2 \mapsto R_1$ .

Suppose there are a pair of role families  $R_1 = \{r_1, r_2\}$  and  $R_2 = \{r_2, r_3\}$  as shown in Figure 6. Here,  $r_1, r_2$ , and  $r_3$  are roles where  $r_1 = \{\langle x, read \rangle, \langle y, write \rangle\}$ ,  $r_2 = \{\langle x, read \rangle, \langle y, read \rangle, \langle z, write \rangle\}$ , and  $r_3 = \{\langle x, read \rangle, \langle y, read \rangle, \langle z, read \rangle\}$ . According to the definitions,  $r_1 \Rightarrow r_2 \Rightarrow r_3$ . Here,  $\sqcup_{r \in R_1} r = r_1 \sqcup^{LI} r_2 = r_2$  since  $r_1 \Rightarrow r_2$  and there is no role  $r'$  such that  $r_1 \Rightarrow r' \Rightarrow r_2$ . Similarly,  $\sqcap_{r \in R_2} r = r_2 \sqcap^{LI} r_3 = r_2$ . Then,  $R_1 \Rightarrow R_2$  since  $\sqcup_{r \in R_1} r \Rightarrow \sqcap_{r \in R_2} r$ .

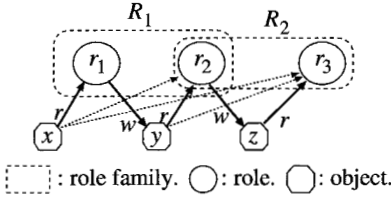


Figure 6. LIF relation.

The following property holds for the legal information flow (LI) relation  $\Rightarrow$ .

**[Property]** Let  $R_1, R_2$ , and  $R_3$  be role families.  $R_2 \not\Rightarrow R_3$  if  $R_1 \Rightarrow R_2$  but  $R_1 \not\Rightarrow R_3$ .

**[Proof]** Assume  $R_1 \Rightarrow R_2$ ,  $R_1 \not\Rightarrow R_3$ , and  $R_2 \Rightarrow R_3$ . Since  $R_1 \Rightarrow R_2$  and  $R_2 \Rightarrow R_3$ ,  $R_1 \Rightarrow R_3$  from the property 1. This contradicts the assumption  $R_1 \not\Rightarrow R_3$ . Hence, the property holds.

Suppose a collection  $R$  of roles are defined on a set  $\mathbf{O}$  of objects. First, for a pair of roles  $r_1$  and  $r_2$  in the set  $R$ , it is checked if the legal information flow (LIF) relation  $r_1 \Rightarrow r_2$  or the illegal information flow (IIF) relation  $r_1 \mapsto R_2$  holds by comparing the input and output sets according to the definitions. This is a simple computation realized in matrices LIM and IIM where  $\text{LIM}(r_1, r_2) = 1$  if  $r_1 \Rightarrow r_2$ , else 0, and  $\text{IIM}(r_1, r_2) = 1$  if  $r_1 \mapsto r_2$ , else 0.

Next, we have to check if  $R_1 \Rightarrow R_2$  for a pair of role families  $R_1$  and  $R_2$ . In order to do it, we use a basic procedure  $\text{Llub}(r_1, r_2)$  and  $\text{llub}(r_1, r_2)$  to obtain least upper bounds of a pair of roles  $r_1$  and  $r_2$  by using the matrices LIM and IIM, respectively. By using the lub procedures  $\text{Llub}$  and  $\text{llub}$  the least upper bounds of role families  $R_1$  and  $R_2$ ,  $R_1 \sqcup^{LI} R_2$  and  $R_1 \sqcup^{II} R_2$  are obtained by a procedure  $\text{LLUB}(R_1, R_2)$  and  $\text{ILUB}(R_1, R_2)$ , respectively. If a set  $\mathbf{T}$  of transactions is a priori defined, a collection  $\mathbf{P}$  of purposes is obtained. Then, for each pair of purposes  $R_1$  and  $R_2$ , i.e. role families, it is checked if  $R_1 \Rightarrow R_2$ . It spends computation resource to check the legal information (LI) and illegal information (II) flow relations for  $\mathbf{P}$ . However, the LI-relation and II-relation can be obtained at the initialization of the system. If a new type of transaction  $T$  is initiated, the purpose  $PR(T)$  is added to the purpose set  $\mathbf{P}$  and the LI-relation and II-relations are checked for the purpose  $PR(T)$ .

## 4 Information Flow Check

We discuss how to enhance the two-phase locking (2PL) protocol so that no illegal information occurs. A transaction  $T_t$  locks an object  $o$  before performing a method  $op$  on the object  $o$ . If the object  $o$  could not be locked, i.e. another transaction  $T_u$  locks the object  $o$ , the transaction  $T_t$  waits until  $T_u$  unlocks the object  $o$ . In this paper, we assume every transaction takes the strict two phase locking protocol, i.e. a transaction  $T_t$  does not issue a lock request after issuing an unlock request and every lock hold by  $T_t$  is released at the end on  $T_t$ . Suppose the transaction  $T_t$  reads an object  $o_j$  in a read method  $op_{tj}$  before writing the object  $o_i$  in  $op_{ti}$ . If an access right  $\langle o_j, read \rangle$  is not in  $PR(T_u)$ , illegal information flow occur. Otherwise, no illegal information flow occur. Thus, it depends on what method is performed on what object whether or not illegal information flow occur. Suppose after a *write* method  $op_{ti}$  of a transaction  $T_t$  is performed on an object  $o_i$ , a *read* method  $op_{ui}$  for another transaction  $T_u$  is issued to the object  $o_i$ . If  $PR(T_t) \not\Rightarrow PR(T_u)$ , i.e.  $PR(T_t) \Rightarrow PR(T_u)$  or  $PR(T_t) \parallel PR(T_u)$ , no illegal information flow occurs. If  $PR(T_t) \mapsto PR(T_u)$ , illegal information flow occur. Hence, the read method  $op_{ui}$  cannot be performed, i.e.  $T_u$  is aborted. If  $PR(T_t) \rightarrow PR(T_u)$  but  $PR(T_t) \not\mapsto PR(T_u)$ , illegal information flow might occur.

Each time a method  $op_{ti}$  is issued to an object  $o_i$ , we check if illegal information flow might occur by performing the method  $op_{ti}$ . A variable  $o_i.P$  denoting a role family, i.e. purpose of a transaction which has most recently written the object  $o_i$  is manipulated for each object  $o_i$ .  $o_i.P = \phi$  in the initialization of the system. Let  $op_{ti}$  be a method which is issued by a transaction  $T_t$ . The method  $op_{ti}$  is performed on the object  $o_i$  as follows [Figure 7]:

```

Perform( $T_t, op_{ti}, o_i$ ) {
  if an object  $o_i$  could be locked, {
    if  $op_{ti} = write$ , {
       $o_i.P = PR(T_t)$ ;
      write  $o_i$ ; }
    else { /*  $op_{ti} = read$  */
      if  $o_i.P \Rightarrow PR(T_t)$  or  $o_i.P \parallel PR(T_t)$ ,
        read  $o_i$ ; /* no illegal information flow */
      else abort  $T_t$ ; }
    } else wait;
}

```

If  $op_{ti}$  is *write*, a purpose  $PR(T_t)$  of the transaction  $T_t$  is stored in a variable  $o_i.P$  and the *write* method  $op_{ti}$  is performed on the object  $o_i$ . Next, suppose  $op_{ti}$  is *read*. If  $o_i.P \Rightarrow PR(T_t)$  or  $o_i.P \parallel PR(T_t)$ , the transaction  $T_t$  reads the object  $o_i$ . If  $o_i.P \mapsto PR(T_t)$ , the transaction  $T_t$  is aborted. In this paper, if  $o_i.P \rightarrow PR(T_t)$ ,  $T_t$  is aborted. Thus, unless  $o_i.P \Rightarrow PR(T_t)$  or  $o_i.P \parallel PR(T_t)$ , the transaction  $T_t$  is aborted since illegal information flow might occur.

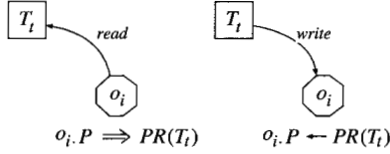


Figure 7. Information flow check.

#### 4.1 Scheduling of methods

We discuss an information flow scheduler (IFS) to perform multiple conflicting transactions so as to keep objects consistent and prevent illegal information flow. First, suppose a pair of transactions  $T_t$  and  $T_u$  issue methods  $op_{ti}$  and  $op_{ui}$  to an object  $o_i$ , respectively. First, suppose every method issued by transactions is sent to a scheduler  $IFS_i$  of the object  $o_i$ . Suppose the method  $op_{ti}$  arrives prior to  $op_{ui}$ .

```
Schedule( $op_{ti}, op_{ui}$ ) {
  if  $op_{ti}$  is write and  $op_{ui}$  is read,
    if  $PR(T_t) \not\Rightarrow PR(T_u)$ , or  $PR(T_t) \parallel PR(T_u)$  {
      /* illegal information flow might occur */
      cfresolve( $T_t, T_u$ ); }
     $op_{ti}$  precedes  $op_{ui}$  ( $op_{ti} \Rightarrow op_{ui}$ ) in  $LIFS_i$ ;
  }
  else  $op_{ti}$  and  $op_{ui}$  are arbitrarily ordered ( $op_{ti} \parallel op_{ui}$ );
}
```

Suppose that a transaction  $T_t$  issues a method  $op_{ti}$  and another transaction  $T_u$  issues a method  $op_{ui}$  to a object  $o_i$  and  $op_{ti}$  conflicts with  $op_{ui}$ . Here, suppose that  $op_{ti}$  is write and  $op_{ui}$  is read. Here, if  $PR(T_t) \Rightarrow PR(T_u)$ , no illegal information flow occur. However, illegal information flow might occur unless  $PR(T_u) \not\Rightarrow PR(T_t)$ , i.e.  $PR(T_t)$  and  $PR(T_u)$  conflict. Hence, the methods  $op_{ti}$  (write) and  $op_{ui}$  (read) cannot be performed in this order. Either  $T_t$  or  $T_u$  is aborted since illegal information flow might occur. In the procedure  $cfresolve(T_t, T_u)$ , the confliction of the purposes  $PR(T_t)$  and  $PR(T_u)$  of  $T_t$  and  $T_u$  is resolved by aborting one of the transactions. In another way, the execution order of the methods  $op_{ui}$  and  $op_{ti}$  is reversed, i.e.  $op_{ui}$  is performed on the object  $o_i$  prior to  $op_{ti}$  if  $PR(T_t) \rightarrow PR(T_u)$ . Here, if the transactions  $T_t$  and  $T_u$  issue other conflicting methods  $op_{tj}$  and  $op_{uj}$  to another object  $o_j$ , the method  $op_{uj}$  has to be performed prior to the method  $op_{tj}$ . If the method  $op_{tj}$  had been already performed prior to the method  $op_{uj}$ ,  $op_{ui}$  cannot be performed prior to  $op_{ti}$ . Here,  $T_t$  or  $T_u$  has to be aborted. If the following conditions are satisfied, conflicting methods  $op_{ti}$  and  $op_{ui}$  are rather primarily ordered in the relation  $\Rightarrow$ :

##### [IF dominant conditions]

1. Any method is performed in neither  $T_t$  nor  $T_u$ .
2.  $op_{ti} = \text{write}$  and  $op_{ui} = \text{read}$ .
3.  $PR(T_u) \Rightarrow PR(T_t)$ .

In this paper, we take the abort-oriented procedure  $cfresolve$  as follows:

```
cfresolve( $T_t, T_u$ ) {
  abort  $T_t$  or  $T_u$ ;
}
```

Since conflicting methods issued by multiple transactions are totally ordered on each object in the significance of purposes of the transactions, the transactions are serializable in the scheduler  $LIFS_i$ . In addition, one of transactions  $T_t$  and  $T_u$  is aborted if illegal information flow would occur by performing methods from the transactions  $T_t$  and  $T_u$  in the scheduled order.

## 5 Concluding Remarks

In the access control models, there might occur confinement problem, i.e. illegal information flow occur even if only authorized subjects manipulate objects in authorized ways. We take a simple model where each object supports a pair of *read* and *write* method and each subject is granted a family of roles in the mandatory access control model. In this paper, we define a legal information flow relation  $\Rightarrow$  and necessarily illegal information flow relation  $\not\Rightarrow$  among role families. If  $R_1 \Rightarrow R_2$  for role families  $R_1$  and  $R_2$ , no illegal information flow occur if a transaction with purpose  $R_1$  is performed prior to a transaction with  $R_2$ . On the other hand, if  $R_1 \not\Rightarrow R_2$ , illegal information flow surely occurs. We discussed the locking protocol to keep objects secure. Then, A method is performed on an object if no illegal information flow would occur.

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