# Concurrency Control for Distributed Objects using Role Ordering（RO）Scheduler 

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A concept of role is significant to design and implement a secure information system．A role shows a job function in an enterprise．In addition to keeping systems secure，objects have to be consistent in presence of multiple transactions．Traditional locking protocols and timestamp ordering schedulers are based on principles＂first－comer－ winner＂and＂timestamp order＂to make multiple conflicting transactions serializable，respectively．We define a significantly precedent lation on roles showing which one of a pair of roles is more significant than another one in an enterprise．We discuss a scheduler so that multiple conflicting transactions are serializable in a significant order of roles of transactions．

# ロール順序付け（RO）スケジューラを用いた同時実行制御 

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役割（role）は対象世界（企業等）の業務に対応し，アクセス権限の集合として定義される，システム内で複数のトラ ンザクションが並列に実行されるとき，システム内のオブジェクトを正しい状伯に保つためには，䭗合する複数のトラン ザクションを直列に実行する必要がある。競合する複数のトランサクションを直列化する方法として，ロック，時刻印順序付けプロトコルが掘案されている。これらの手法は「早いもの勝ち」および「時刻印順」でトランザクションを直列化している．役割は，対象世界の業務に対応することから重要度の高い業務は優先して行われるべきである。本論文では，複数のトランザクションを役割の重要度を基に直列化して実行する新たな同時実行制御方法を提案する。

## 1 Introduction

Information systems like relational database systems ［ 5,7 ］adopt role－based access control（RBAC）models［ 6,8 ］． A role shows a job function like president and secretary， which each person performs in an enterprise．A role is a collection of access rights which a subject who plays the role is allowed to do for objects in an enterprise．Here，an access right（or permission）is a pair $\langle o, o p\rangle$ of an object $o$ and a method $o p$ on the object $o$ ．Only if an access right $\langle o, o p\rangle$ is granted to a subject $s$ ，the subject $s$ is allowed to manipulate the object $o$ through the method $o p$ ．In the discretionary approach［5，7］，a subject who is granted a role can further grant the role to another subject．

A transaction is an atomic sequence of methods which are performed on objects［1，3］．A pair of methods conflict if and only if（iff）the result obtained by performing the methods depends on the computation order．Transac－ tions are referred to as conflict if the transactions ma－ nipulate a same object through conflicting methods．A collection of conflicting transactions are required to be serializable in order to keep objects consistent．In order to realize the serializability of multiple conflicting trans－ actions，locking protocols $[1,3]$ are widely used．A trans－ action $T$ locks an object before manipulating the object by a method op．Other transactions to manipulate the object in a conflicting manner with the method op have to wait until the transaction $T$ releases the object．Lock－ ing protocols are based on a principle that only the first comer is a winner and the others are losers．Another way is a timestamp ordering（TO）scheduler［1］．Each trans－ action $T$ is stamped time when the transaction $T$ is initi－ ated，timestamp $t s(T)$ ．Transactions are totally ordered in their timestamps．Differently from the locking proto－ cols，objects are manipulated by conflicting transactions
in the timestamp order and no deadlock occurs．
In this paper，we discuss a concurrency control al－ gorithm based on roles associated for transactions，role ordering（ $R O$ ）scheduler．Let $T_{1}$ and $T_{2}$ be a pair of transactions which are associated with roles $R_{1}$ and $R_{2}$ ， respectively，and which manipulate an object $o$ in a con－ flicting manner．Here，the transaction $T_{1}$ manipulates the object $o$ before $T_{2}$ if the role $R_{1}$ is more significant than the other role $R_{2}$ ．This means the more significant job a transaction does，the earlier an object can be manipulated by the transaction．In the RO scheduler，conflicting meth－ ods issued by transactions are ordered in the significancy of the roles．Transactions can concurrently manipulate objects in such an order that persons really do their jobs in an enterprise．

In section 2，we present a system model．In section 3， we newly define significantly dominant relations among roles．In section 4，we discuss the role ordering（RO）seri－ alizability．In section 5，we discuss the role ordering（RO） scheduler．In section 6，we evaluate the RO scheduler compared with the two－phase locking（2PL）protocol．

## 2 System Model

## 2．1 Object－based system

A system is composed of objects［4］which are dis－ tributed on multiple computers in networks．An object is an encapsulation of data and methods for manipulating the data．An object can be manipulated only through methods．A method is more abstract than primitive methods like read and write．A pair of methods $o p_{1}$ and $o p_{2}$ supported by an object o are referred to as conflict with one another iff the result obtained by performing the methods $o p_{1}$ and $o p_{2}$ depends on the computation or－ der．Otherwise，a pair of the methods $o p_{1}$ and $o p_{2}$ are

## compatible with one another.

A transaction is modeled to be an atomic sequence of methods issued to objects [1]. Multiple transactions are concurrently performed in order to increase the throughput of the system. Multiple conflicting transactions are required to be serializable to keep objects mutually consistent $[1,3]$. Let $T_{i}$ be a transaction which issues a method $o p_{1 i}$ to an object $o_{1}$ and a method $o p_{2 i}$ to another object $o_{2}$. Suppose there are a pair of transactions $T_{1}$ and $T_{2}$ where $o p_{11}$ and $o p_{21}$ conflict on the object $o_{1}$ as well as the methods $o p_{12}$ and $o p_{22}$ on the object $o_{2}$. If the method $o p_{11}$ is performed on the object $o_{1}$ before $o p_{21}$, $o p_{21}$ is required to be performed before $o p_{22}$ on the other object $o_{2}$ according to the serializebility theory [1]. In the timestamp ordering (TO) scheduler [1], each transaction $T_{i}$ is assigned with real time $t s\left(T_{i}\right)$ when the transaction $T_{i}$ is initiated on a client. If $t s\left(T_{1}\right)<t s\left(T_{2}\right)$, the method $o p_{11}$ is performed before $o p_{21}$ on the object $o$ and the method $o p_{12}$ is performed before $o p_{22}$ on the object $o_{2}$. Thus, a pair of conflicting transactions $T_{1}$ and $T_{2}$ are performed in the timestamp order.

In the two-phase locking protocol [3], the transaction $T_{1}$ is performed if a pair of the objects $o_{1}$ and $o_{2}$ are locked before the other transaction $T_{2}$. The transaction $T_{2}$ cannot manipulate the objects $o_{1}$ and $o_{2}$ until the transaction $T_{1}$ releases the objects. In the strict protocol [1], every transaction releases all the objects locked on termination of the transaction. Hence, no cascading abort occur.

### 2.2 Roles

In access control models [6], a system is composed of two types of entities, subject and object. A subject is an active entity which issues a request to an object like user and program. On the other hand, an object is a passive entity like database which receives a request and then sends back its response. A subject can manipulate an object only through a method which the subject is allowed to issue. An access right is a pair $\langle o, o p\rangle$ of an object o and a method $o p$. Only if an access right $\langle o, o p\rangle$ is granted to a subject $s$, the subject $s$ is allowed to manipulate an object $o$ through a method op.

A role shows a job function in an enterprisc. Each subject $s$ plays a role like president in an enterprise. A subject which plays a more significant role should be more prioritized than less significant subjects. If a pair of tasks in different jobs would like to use an object, one task in a more significant job should take the object earlier than the other. A task is realized as a transaction.

A role is a collection of access rights in a role-based access control (RBAC) model [6]. A subject $s$ is first granted a role $R$. Then, the subject is allowed to issue an access request $o p$ to an object $o$ only if an access right $\langle o, o p\rangle$ is included in the role $R$. Suppose a subject $s$ initiates a transaction $T$ with a role $R$ granted to the subject $s$. We assume each transaction is associated with only one role in this paper. Here, let subject( $T$ ) denote a subject which initiates a transaction $T$. Let role $(T)$ show a role which is associated to a transaction $T$. A transaction $T$ issues an access request ( $o, o p$ ) to manipulate an object $o$ through a method $o p$. The request $\langle o, o p\rangle$ is accepted if $\langle o, o p\rangle \in \operatorname{role}(T)$. Otherwise, the access request $\langle o, o p\rangle$ is rejected, i.e. the transaction $T$ is aborted.

The relational database systems take the discretionary approach [5,7]. A role $R$ is first created by a subject $s_{0}$. Here, the subject $s_{0}$ is an owner
of the role $R$, denoted by owner $(R)$. Then, the owner $s_{0}$ grants the role $R$ to a subject $s_{1}$. Furthermore, the subject $s_{1}$ can grant the role $R$ to another subject $s_{2}$. A role is also an object with methods grant and revoke for granting and revoking and methods delete and add for deleting and adding access rights in the role, respectively. If the subject $s_{1}$ changes the role $R$, e.g. adds an access right to $R$, the role $R$ granted to the subjects $s_{0}$ and $s_{2}$ is also changed.

## 3 Significancy on Roles

### 3.1 Significancy of subjects on a role

We take the discretionary approach to adopting the role-based access control (RBAC) model [6] to objectbased systems. First, suppose that a subject $s_{0}$ creates a role $R$. Here, the subject $s_{0}$ is an owner owner $(R)$ of the role $R$. Then, the owner subject $s_{0}$ grants the role $R$ to another subject $s_{1}$. The subject $s_{1}$ furthermore grants the role $R$ to subjects $s_{2}$ and $s_{3}$ as shown in Figure 1. Here, the subject $s_{1}$ is more tightly related with the role $R$ than the subject $s_{2}$. This means, the subject $s_{1}$ is considered to be more significant than the other subject $s_{2}$ with respect to the role $R$.

We define a precedent relation among subjects showing which subjects are more significant than others with respect to a role $R$ :

- A subject $s_{1}$ is more significant than another subject $s_{2}$ with respect to a role $R\left(s_{1} \succ_{R} s_{2}\right)$ if and only if (iff) the subject $s_{1}$ grants the role $R$ to $s_{2}$ or $s_{1} \succ_{R} s_{3} \succ_{R} s_{2}$ for some subject $s_{3}$.


Figure 1. Discretionary approach.
The significantly precedent relation $\succ_{R}$ of subjects is acyclic. A pair of subjects $s_{1}$ and $s_{2}$ are independent with respect to a role $R\left(s_{1} \|_{R} s_{2}\right)$ iff $s_{1}$ and $s_{2}$ are granted the role $R$ and neither $s_{1} \succ_{R} s_{2}$ nor $s_{2} \succ_{R} s_{1}$. In Figure 1, an owner subject $s_{0}$ (owner $(R)$ ) of a role $R$ is more significant than a subject $s_{1}\left(s_{0} \succ_{R} s_{1}\right)$ since the owner $s_{0}$ grants the role $R$ to the subject $s_{1}$. In addition, $s_{1} \succ_{R}$ $s_{2}$ and $s_{1} \succ_{R} s_{3}$. Thus, $s_{0} \succ_{R} s_{1} \succ_{R} s_{2}$ and $s_{0} \succ_{R} s_{2}$. However, $s_{2} \|_{R} s_{3}$ and $s_{2} \|_{R} s_{4}$.

Let $\mathbf{S}(R)$ be a set of subjects which are granted a role $R$. Subjects in the set $S(R)$ are partially ordered in the significantly precedent relation $\succ_{R}$. Suppose the role $R$ includes a pair of access rights $\left\langle o, o p_{1}\right\rangle$ and $\left\langle o, o p_{2}\right\rangle$ where a method $o p_{1}$ conflicts with a method $o p_{2}$. A pair of the subjects $s_{1}$ and $s_{2}$ are granted the role $R$ and issue methods $o p_{1}$ and $o p_{2}$ to the object $o$, respectively. If the subject $s_{1}$ is more significant than the subject $s_{2}$ with respect to the role $R\left(s_{1} \succ_{R} s_{2}\right)$, the method $p_{1}$ is performed before another method $o p_{2}$ on the object $o$.

### 3.2 Significancy of roles

We discuss which roles are more significant than other roles. Suppose a subject $s_{1}$ is granted a role $R_{1}$ and a subject $s_{2}$ is granted another role $R_{2}$. Then, a pair of the subjects $s_{1}$ and $s_{2}$ issuc conflicting methods $o p_{1}$ and $o p_{2}$ to an object $o$, respectively. We discuss which method $o p_{1}$ or $o p_{2}$ to be performed on the object $o$ before the other method. It is true that $o p_{1}$ should be performed
before $o p_{2}$ if a job function shown by a role $R_{1}$ is more significant than another role $R_{2}$ in an enterprise.

A method $o p_{1}$ is more significant than another method $o p_{2}$ on an object $o\left(o p_{1} \succ o p_{2}\right)$ iff the state of the object $o$ is changed by the method $o p_{1}$ but is not changed by the method $o p_{2}$. Methods by which state of an object is changed are referred to as object methods. Object methods are classified into two types: output and input ones. By using an output type of method, data is derived from an object while an input type of method brings data into an object. Furthermore, there are class methods where an object is created for a class and is dropped. A pair of methods create and drop of an object are more significant than the object methods.

Let us consider a pair of methods withdraw and deposit on a bank object. Both the methods withdraw and deposit are input types. Hence, the methods withdraw and deposit are significantly equivalent (withdraw $\equiv$ deposit). In our life, a subject more carefully issues a method withdraw than a method deposit because the account value in the bank object is decremented by withdraw. This example shows that some methods are considered to be more significant than other methods by an application. Here, a method withdraw is referred to as more semantically significant than another method deposit (withdraw $\succ$ deposit). A semantically significant relation $\succ$ among methods is defined on each object by an application. A method $o p_{1}$ is referred to as semantically significantly equivalent with another method $o p_{2}\left(o p_{1} \cong o p_{2}\right)$ iff neither $o p_{1} \nrightarrow o p_{2}$ nor $o p_{2} \nsucc o p_{1} . o p_{1} \succcurlyeq o p_{2}$ iff $o p_{1} \nsucc o p_{2}$ or $o p_{1} \cong o p_{2}$.
[Definition] A method $o p_{1}$ is more significant than another method $o p_{2}\left(o p_{1} \succ o p_{2}\right)$ iff one of the following conditions is satisfied:

1. $o p_{1}$ is a class type and $o p_{2}$ is an object type.
2. $o p_{1}$ is an input type and $o p_{2}$ is an output one.
3. $o p_{1}$ and $o p_{2}$ are same types and $o p_{1}$ is semantically more significant than $o p_{2}\left(o p_{1} \succcurlyeq o p_{2}\right)$.
A method $o p_{1}$ is significantly equivalent with another method $o p_{2}\left(o p_{1} \equiv o p_{2}\right)$ iff neither $o p_{1} \succ o p_{2}$ nor $o p_{2} \succ o p_{1}$. A method $o p_{1}$ significantly dominates another method $o p_{2}\left(o p_{1} \succeq o p_{2}\right)$ iff $o p_{1} \succ o p_{2}$ or $o p_{1} \equiv o p_{2}$.

A system is composed of multiple objects. Objects are classified into some security classes [2]. An object $o_{1}$ is more significant than another object $o_{2}\left(o_{1} \succ o_{2}\right)$ if $o_{1}$ is more secure than $o_{2}$ in an enterprise. A pair of objects $o_{1}$ and $o_{2}$ are significantly equivalent ( $o_{1} \equiv o_{2}$ ) if neither $o_{1} \succ o_{2}$ nor $o_{2} \prec o_{1} . o_{1} \equiv o_{2}$ if $o_{1}=o_{2}$. An object $o_{1}$ significantly dominates another object $o_{2}\left(o_{1} \succeq o_{2}\right)$ iff $o_{1} \succ o_{2}$ or $o_{1} \equiv o_{2}$.

A role is a collection of access rights. Let $\left\langle o_{1}, o p_{1}\right\rangle$ and $\left\langle o_{2}, o p_{2}\right\rangle$ be access rights on a pair of objects $o_{1}$ and $o_{2}$. We discuss which one in the access rights $\left\langle o_{1}, o p_{1}\right\rangle$ and $\left\langle o_{2}, o p_{2}\right\rangle$ is more significant than the other. First, methods $o p_{1}$ and $o p_{2}$ are supported by a same object $o_{1}\left(o_{1}=o_{2}\right)$. An access right $\left\langle o_{1}, o p_{1}\right\rangle$ is more significant than $\left\langle o_{1}, o p_{2}\right\rangle\left(\left\langle o_{1}, o p_{1}\right\rangle \succ\left\langle o_{1}, o p_{2}\right\rangle\right)$ if $o p_{1} \succ o p_{2}$. Next, a pair of methods $o p_{1}$ and $o p_{2}$ are supported by different objects $o_{1}$ and $o_{2}$, respectively ( $o_{1} \neq o_{2}$ ). An access right $\left\langle o_{1}, o p_{1}\right\rangle$ is more significant than another access right $\left\langle o_{2}, o p_{2}\right\rangle\left(\left\langle o_{1}, o p_{1}\right\rangle \succ\left\langle o_{2}, o p_{2}\right\rangle\right)$ if $o_{1} \equiv o_{2}$ and $o p_{1} \succ o p_{2}$. Lastly, suppose that an object $o_{1}$ is more significant than another object $o_{2}\left(o_{1} \succ o_{2}\right)$. An access right $\left\langle o_{1}, o p_{1}\right\rangle$ is more significant than another access right
$\left\langle o_{2}, o p_{2}\right\rangle\left(\left\langle o_{1}, o p_{1}\right\rangle \succ\left\langle o_{2}, o p_{2}\right\rangle\right)$ if $o_{1} \succ o_{2}$.
[Definition] An access right $\left\langle o_{1}, o p_{1}\right\rangle$ is more significant than another access right $\left\langle o_{2}, o p_{2}\right\rangle\left(\left\langle o_{1}, o p_{1}\right)\right.$ $\succ\left\langle o_{2}, o p_{2}\right\rangle$ ) iff one of the following condition holds:

$$
\begin{aligned}
& \text { - } o p_{1} \succ o p_{2} \text { if } o_{1} \equiv o_{2} . \\
& \text { - } o_{1} \succ o_{2} .
\end{aligned}
$$

A pair of access rights $\left\langle o_{1}, o p_{1}\right\rangle$ and $\left\langle o_{2}, o p_{2}\right\rangle$ are significantly equivalent ( $\left\langle o_{1}, o p_{1}\right\rangle \equiv\left\langle o_{2}, o p_{2}\right\rangle$ ) iff neither $\left\langle o_{1}, o p_{1}\right\rangle \succ\left\langle o_{2}, o p_{2}\right\rangle$ nor $\left\langle o_{1}, o p_{1}\right\rangle \prec\left\langle o_{2}, o p_{2}\right\rangle$. An access right $\left\langle o_{1}, o p_{1}\right\rangle$ significantly dominates another access right $\left\langle o_{2}, o p_{2}\right\rangle\left(\left\langle o_{1}, o p_{1}\right\rangle \succeq\left\langle o_{2}, o p_{2}\right\rangle\right)$ iff $\left\langle o_{1}, o p_{1}\right\rangle$ $\succ\left\langle o_{2}, o p_{2}\right\rangle$ or $\left\langle o_{1}, o p_{1}\right\rangle \equiv\left\langle o_{2}, o p_{2}\right\rangle$.

We discuss which role is more significant than another role based on the significantly dominant relation $\succeq$ of access rights.
[Definition] A role $R_{1}$ significantly dominates another role $R_{2}\left(R_{1} \succeq R_{2}\right)$ if for every access right $\left\langle o_{2}, o p_{2}\right\rangle$ in $R_{2}$, there is at least one access right $\left(o_{1}, o p_{1}\right)$ in $R_{1}$ such that $\left\langle o_{1}, o p_{1}\right\rangle \succeq\left\langle o_{2}, o p_{2}\right\rangle$ and no $\left\langle o_{3}, o p_{3}\right\rangle$ in $R_{2}$ such that $\left\langle o_{3}, o p_{3}\right\rangle \succeq\left\langle o_{1}, o p_{1}\right\rangle$.

A role $R_{1}$ is significantly equivalent with another role $R_{2}\left(R_{1} \equiv R_{2}\right)$ if $R_{1} \succeq R_{2}$ and $R_{2} \succeq R_{1}$. A role $R_{1}$ is more significant than another role $R_{2}\left(R_{1} \succ R_{2}\right)$ iff $R_{1} \succeq R_{2}$ but $R_{1} \not \equiv R_{2}$. A pair of roles $R_{1}$ and $R_{2}$ are comparable if $R_{1} \succeq R_{2}$ or $R_{2} \succeq R_{1}$. Otherwise, $R_{1}$ and $R_{2}$ are uncomparable.

## 4 Serializability

Suppose a pair of transactions $T_{1}$ and $T_{2}$ are granted roles $R_{1}$ and $R_{2}$, respectively. Each transaction is submitted by a subject and assigned with one of roles granted to the subject. Let $\mathbf{T}$ be a set of transactions which are being performed in a system. The transaction set $\mathbf{T}$ is partially ordered based on the significantly dominant relation $\succeq$ of roles:
[Definition] A transaction $T_{1}$ significantly dominates another transaction $T_{2}\left(T_{1} \succeq T_{2}\right)$ iff role $\left(T_{1}\right) \succeq \operatorname{role}\left(T_{2}\right)$ or $\operatorname{subject}\left(T_{1}\right) \succeq_{R} \operatorname{subject}\left(\bar{T}_{2}\right)$ if $\operatorname{role}\left(T_{1}\right)=\operatorname{role}\left(T_{2}\right)=$ $R$.

A transaction $T_{1}$ is significantly equivalent with another transaction $T_{2}\left(T_{1} \equiv T_{2}\right)$ if $T_{1} \succeq T_{2}$ and $T_{2} \succeq T_{1}$. $T_{1}$ and $T_{2}$ are independent iff neither $T_{1} \succeq T_{2}$ nor $T_{2} \succeq$ $T_{1}$.

A schedule $H$ is an execution sequence of methods from transactions in the transaction set T. A transaction $T_{1}$ precedes another transaction $T_{2}$ in the schedule $H\left(T_{1}\right.$ $\rightarrow_{H} T_{2}$ ) iff a method $o p_{1}$ from $T_{1}$ is performed before a method $o p_{2}$ from $T_{2}$ which conflicts with $o p_{1}$. A schedule $H$ is serializable iff the precedent relation $\rightarrow_{H}$ is acyclic according to the traditional theory [1]. A schedule $H$ is shown in a partially ordered set $\left\langle\mathbf{T}, \rightarrow_{H}\right\rangle$.
[Definition] A transaction $T_{1}$ significantly precedes another transaction $T_{2}$ in a schedule $H$ of a transaction set $\mathrm{T}\left(T_{1} \Rightarrow_{H} T_{2}\right)$ iff $T_{1} \rightarrow_{H} T_{2}$ and $T_{1} \succeq T_{2}$.

Suppose a transaction $T_{1}$ precedes another transaction $T_{2}$ in a schedule $H$ of a transaction set $\mathbf{T}$. Here, if $T_{1} \succeq$ $T_{2}$, " $T_{1} \rightarrow H T_{2}$ " is referred to as legal, i.e. $T_{1}$ significantly precedes $T_{2}\left(T_{1} \Rightarrow_{H} T_{2}\right)$. That is, conflicting transactions are performed in the significantly precedent relation $\Rightarrow_{H}$. On the other hand, if $T_{1} \prec T_{2}$, " $T_{1} \rightarrow_{H} T_{2}$ " is illegal. A schedule $H$, i.e. $\left\langle\mathbf{T}, \rightarrow_{H}\right\rangle$ is legal iff $T_{1} \rightarrow_{H} T_{2}$ if $T_{1} \succeq$ $T_{2}$ for every pair of transactions $T_{1}$ and $T_{2}$ in $T$. In order to make a schedule legal, methods from transactions are
required to be buffered until all the transactions are initiated. Here, the throughput of the system is degraded since transactions have to wait in the buffer. In order to increase the throughput, only some number of transactions in $\mathbf{T}$ which are initiated during some time units are scheduled. A schedule $H$ is partitioned into subschedules $H_{1}, \ldots, H_{n}$ where each subschedule $H_{i}=\left\langle\mathbf{T}_{i}, \rightarrow_{H}\right\rangle$ ( $i=$ $1, \ldots, n$ ) satisfies the following conditions:
[Role ordering (RO) partition]

1. $\mathbf{T}_{i} \cap \mathbf{T}_{j}=\phi$ for every pair of subschedules $H_{i}$ and $H_{j}$ and $\mathbf{T}_{1} \cup \cdots \cup \mathbf{T}_{n}=\mathbf{T}$.
2. $T_{1} \rightarrow_{H} T_{2}$ is legal if $T_{1} \rightarrow_{H} T_{2}$ for every pair of transactions $T_{1}$ and $T_{2}$ in $\mathrm{T}_{i}$.
3. For every pair of subschedules $H_{i}$ and $H_{j}$, if $T_{i 1} \rightarrow_{H}$ $T_{j 1}$ for some pair of transactions $T_{i 1}$ in $H_{i}$ and $T_{j 1}$ in $H_{j}$, there are no pair of transactions $T_{i 2}$ in $H_{i}$ and $T_{j 2}$ in $H_{j}$ such that $T_{j 2} \rightarrow_{H} T_{i 2}$.
Figure 2 shows a hasse diagram of a schedule $H$ for a transaction set $\mathbf{T}=\left\{T_{1}, T_{2}, T_{3}, T_{4}, T_{5}, T_{6},\right\}$ where a directed edge from a transaction $T_{i}$ to $T_{j}$ shows $T_{i} \rightarrow H$ $T_{j} . \Rightarrow$ and $\rightarrow$ show legal and illegal precedent relation $\rightarrow_{H}$. Suppose that $T_{1} \succeq T_{2}, T_{3} \succeq T_{2}, T_{4} \succeq T_{5}, T_{4} \succeq T_{6}$, $T_{4} \succeq T_{2}$, and $T_{6} \succeq T_{3}$. Here, a pair of subschedules $H_{1}$ with $\mathbf{T}_{1}=\left\{T_{1}, T_{2}, T_{3}\right\}$ and $H_{2}$ with $\mathbf{T}_{2}=\left\{T_{4}, T_{5}, T_{6}\right\}$ are RO partitions of the schedule $H$. In the schedule $H_{1}$, methods from the transactions $T_{1}, T_{2}$, and $T_{3}$ are first performed in the significantly dominant relation $\succeq$, i.e. $T_{1} \Rightarrow_{H} T_{2}$ and $T_{3} \Rightarrow_{H} T_{2}$. Since $T_{2} \preceq T_{4}$ and $T_{3} \preceq T_{6}$, the transactions $T_{4}$ and $T_{6}$ cannot be performed as long as every transaction in $H_{i}$ completes. After $T_{2}$ commits, the transactions in $\mathrm{H}_{2}$ are performed.


Figure 2. Schedule $H$.
[Definition] A history $H$ of transactions is $R O$ serializable if the schedule $H$ is RO partitioned.

It is straightforward to hold that a history $H$ is serializable if $H$ is RO serializable because $T_{i} \rightarrow_{H} T_{j}$ if $T_{i} \Rightarrow_{H}$ $T_{j}$ for every pair of transactions $T_{i}$ and $T_{j}$.

## 5 Role-Ordering (RO) Scheduler

We discuss a role-ordering (RO) scheduler based on the significancy of subjects and roles.

### 5.1 One-object model

First, we discuss a role-ordering (RO) scheduler for a single object which is manipulated by multiple transactions. An object is stored in an object base ( $O B$ ) of a server. Multiple transactions on clients issue methods to an object $o$. A transaction issues a commit (c) or abort (a) method at the end. An RO scheduler is composed of a receipt queue $R Q$ and auxiliary receipt queue $A R Q$. On receipt of a method from a transaction, the method is first enqueued in $R Q$ of the object $o$ [Figure 3]. Let $\operatorname{Tr}(o p)$ show a transaction which issues a method $o p$.

The following procedures are supported to manipulate a queue $Q$.

1. enqueue $(o p, Q)$ : a method $o p$ is enqueued into $Q$.
2. $o p:=\operatorname{dequeue}(Q):$ a method $o p$ is dequeued from $Q$.
3. $o p:=\operatorname{top}(Q):$ a method $o p$ is a top method in $Q$.
4. ROsort $(Q)$ : all methods in $Q$ are sorted in the significantly dominant relation $\succeq$ of transactions.


Figure 3. RO scheduler.
A variable $\mathbf{E}$ shows a set of methods being currently performed on an object $o$. Let TE be a set of transactions being currently performed, i.e. $\{T r(o p) \mid o p \in \mathbf{E}\}$. A variable $\mathbf{C}$ denotes a transaction which is performed on the object $o$ and which is significantly dominated by every transaction performed. Initially, $\mathbf{C}:=T$. Here, $T$ and $\perp$ denote top and bottom transactions, respectively, where $T \succeq T \succeq \perp$ for every transaction $T$. There are following procedures to perform a method $o p$ on the object $o$ :

1. conflict(op, $\mathbf{E}):$ false if $\mathbf{E}=\phi$ or a method $o p$ does not conflict with every method in $\mathbf{E}$, else true.
2. perform $(o p)$ : a method $o p$ is performed on the object $o$.
Suppose methods in transactions $T_{1}, \ldots, T_{m}$ are being performed, $\mathbf{T E}=\left\{T_{1}, \ldots, T_{m}\right\}$. Methods in $T_{1}, \ldots, T_{m}$ being performed are stored in $\mathbf{E}$. Here, $\mathbf{C}$ shows a transaction $T_{i}$ where $T_{i} \preceq T_{j}$ for every $j=1, \ldots, m$. If $T \succeq \mathbf{C}$, the method $o p$ is enqueued into $R Q$. However, if $T \succ \mathbf{C}$, the method $o p$ is enqueued into $A R Q$. After that, every method issued to the object $o$ from every transaction not in $\mathbf{E}$ is enqueued into $A R Q$. If every transaction in $\mathbf{E}$ commits or aborts, i.e. $\mathbf{E}$ is empty, all methods in $A R Q$ are moved to $R Q$. That is, one subschedule is finished and a new schedule is started. Then, methods in $R Q$ are sorted in the significantly dominant relation $\succeq$.
[Delivery of a method $o p$ from a transaction $T$ ]
if $T \in \mathbf{T E}$ or $T \preceq \mathbf{C}$, \{ enqueue $(o p, R Q)$; ROsort ( $R Q$ ); \}
else $\{\mathbf{C}:=\perp$; enqueue $(o p, A R Q) ;\}$
Methods in the receipt queuc $R Q$ are performed on an object $o$ as follows:

## [Execution of methods]

1. if $\mathbf{T E}=\phi,\{\mathrm{C}:=\mathrm{T}$; Every method $o p$ in $A R Q$ is moved to $R Q$; ROsort $(R Q)$; goto $\mathbf{1 ;}$ \}
2. if conflict (op, E), return;
else $\{o p:=\operatorname{dequeue}(R Q)$;

$$
\begin{aligned}
& \text { if } \operatorname{Tr}(o p) \notin \mathrm{TE}, \mathbf{T E}:=\mathrm{TE} \operatorname{cup}\{\operatorname{Tr}(o p)\} ; \\
& \mathbf{E}:=\mathbf{E} \cup\{o p\} \text { if } \operatorname{Tr}(o p) \prec \mathbf{C}, \mathbf{C}:=\operatorname{Tr}(o p) ; \\
& \text { perform }(o p) ;\}
\end{aligned}
$$

Let $o p$ be a method on an object $o$, which is the top in $R Q$. If the method op is compatible with every method being currently performed, the top method $o p$ is dequened from $R Q$ and then is performed on the object $o$ in $O B$. Otherwise, no method in $R Q$ is dequeued.

If a method op completes, the following procedure is performed :
[Completion of method $o p$ ]

1. $\mathbf{E}:=\mathbf{E}-\{o p\}$;
2. TE $:=\mathrm{TE}-\{\operatorname{Tr}(o p)\}$ if $o p=c$ or $o p=a$;
3. Methods in $R Q$ are performed in the execution procedure presented here.

If a top method $o p_{1}$ conflicts is kept waited in $R Q$, every other method in $R Q$ is required to be waited. Here, suppose there is another method $o p_{2}$ following the method $o p_{1}$ in $R Q$. If $o p_{2}$ is compatible with $o p_{1}, o p_{2}$ can be performed by jumping ever $o p_{1}$ in $R Q$.
[Definition] A method $o p$ is referred to as ready in a receipt queue $R Q$ iff $o p$ is compatible with every method preceding $o p$ in $R Q$ and with every method in $\mathbf{E}$.

In the execution procedure, if the top method $o p(=$ $\operatorname{top}(R Q)$ ) cannot be performed, ready methods in $R Q$ are taken in the significantly dominant relation $\succeq$ and then performed. We introduce the following procedures :

- ready $(o p, R Q, \mathbf{E})$ : true if a method $o p$ is ready in the receipt queue $R Q$, else false.
- $o p_{1}:=\operatorname{next}(o p, R Q): o p_{1}$ is a method in the receipt queue $R Q$ which directly follows an method op.
Let $o p$ be a top method in the reccipt quene $R Q$. If op conflicts with some method being performed, i.e. conflict $(o p, \mathbf{E})$ is true, the following procedure is performed:

```
\(o p:=\operatorname{top}(R Q)\);
if conflict \((o p, \mathbf{E}),\{\)
\(o p:=\operatorname{next}(o p, R Q)\);
while \((o p \neq\) NULL \()\) \{
    if ready \((o p, R Q, \mathbf{E})\), \{
            \(o p\) is removed from \(R Q ; \mathbf{E}:=\mathbf{E} \cup\{o p\} ;\)
                \(\mathrm{TE}:=\mathrm{TE} \cup\{\operatorname{Tr}(o p)\}\) if \(\operatorname{Tr}(o p) \notin \mathrm{TE} ;\)
                if \(\operatorname{Tr}(o p) \prec \mathbf{C}, \mathbf{C}:=\operatorname{Tr}(o p)\);
        perform \((o p)\); break; \}
    else \(o p:=\operatorname{next}(o p, R Q) ;\}\}\)
[Theorem] A schedule of a transaction set \(T\) obtained by the RO scheduler is RO-serializable.
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[Proof] A subschedule obtained from the receipt queue $R Q$ is RO subschedule. A schedule of the transaction set $T$ is RO partitioned into the subsequences.

### 5.2 Distributed object model

In a distributed model, there are multiple objects $o_{1}$, $\ldots, o_{m}(m>1)$ distributed in servers and multiple transactions $T_{1}, \ldots, T_{l}(l>1)$ on multiple clients $c_{1} \ldots, c_{n}(n>$ 1). Each object $o_{i}$ receives methods from multiple transactions on clients $c_{1} \ldots, c_{n}$ while each transaction issues methods to multiple objects.

There are local receipt queues $R Q_{i 1}, \ldots, R Q_{i n}$ in each object $o_{i}(i=1, \ldots, m)$. Transactions are initiated on a client $c_{s}$ and issue methods to objects in servers. Methods issued from transactions on a client $c_{s}$ to an object $o_{i}$ are stored in each local receipt queue $R Q_{i s}(s=1, \ldots, n)$. We assume a communication network supports every pair of an object $o_{i}$ and a client $c_{s}$ with a reliable communication channel, i.e. an object $o_{i}$ receives every message from each client $c_{s}$ in the sending order and with neither message loss nor duplication.

Requests in local receipt queues $R Q_{i 1}, \ldots, R Q_{i n}$ are moved to a global receipt queue $R Q_{i}$ in an object $o_{i}$ [Figure 4]. Here, requests in the global receipt queue $R Q_{i}$ are sorted in the significantly dominant relation $\succeq$. Then, the top method in the global receipt queue $R Q_{i}$ is dequeued and then is performed if no method conflicting with the top method is currently being performed. Question is when the top method in the global receipt queue $R Q_{i}$ can be dequeued. Let us consider a pair of transactions $T_{1}$ and $T_{2}$ as shown in Figure 4. The transaction $T_{1}$ issues a pair of methods $o p_{11}$ and $o p_{12}$ to the objects $o_{1}$ and
$o_{2}$, respectively. The transaction $T_{2}$ issues a pair of methods $o p_{21}$ and $o p_{22}$ to the objects $o_{1}$ and $o_{2}$, respectively. Suppose a pair of the methods $o p_{11}$ and $o p_{21}$ conflict on the object $o_{1}$ and a pair of the methods $o p_{12}$ and $o p_{22}$ also conflict in the other object $o_{2}$. Suppose a method $o p_{12}$ is delayed and another method $o p_{22}$ is also delayed due to congestions and faults. In the object $o_{1}$, the method $o p_{11}$ is enqueued into the global receipt queue $R Q_{1}$ from the local receipt queue $R Q_{11}$, and then performed. On the other hand, the method $o p_{22}$ is performed in the object. $o_{2}$ as well. Eventually, a pair of the delayed methods $o p_{21}$ and $o p_{12}$ arrive at the objects $o_{1}$ and $o_{2}$, respectively, and then are performed. Here, a pair of the transactions $T_{1}$ and $T_{2}$ are not serializable.


Figure 4. Schedulers.
The following conditions have to be satisfied for a collection of global receipt queucs $R Q_{1}, \ldots, R Q_{m}$ for objects $o_{1}, \ldots, o_{m}$, respectively, to realize the serializability of multiple transactions :
[Role-based serializability (RBS) conditions]

1. Methods in every global receipt queue $R Q_{i}$ are sorted in the significantly dominant relation $\succeq$ of transactions ( $i=1, \ldots, m$ ).
2. For a top method $o p_{s}$ from a transaction $T_{s}$ in each global receipt queue $R Q_{i}$, if there is a method $o \dot{p}_{t}$ from the transaction $T_{t}$ in $R Q_{i}$ which the method $o p_{s}$ precedes and conflicts with $o p_{t}, o p_{s}$ precedes $o p_{t}$ in every global receipt queue $R Q_{j}$ where $o p_{t}$ and $o p_{s}$ are methods form $T_{t}$ and $T_{s}$, respectively, and $o \dot{p}_{s}$ and $o p_{t}$ conflict with one another
The second RBS condition shows the traditional serializability in a distributed database system [3]. The first condition means that every pair of conflicting methods are performed in the significantly dominant relation $\succeq$ of the transactions.

In order to satisfy the RBS conditions, we take the following approach :

1. Each client $c_{s}$ periodically sends a fence message $k_{s}$ to every object $o_{i}$.
2. In an object $o_{i}$, if there is a fence message $k_{s}$ in every local receipt queuc $R Q_{i s}$, methods preceding a fence massage $k_{s}$ in every local receipt queue $R Q_{i s}$ are moved to the global reccipt queue $R Q_{i s}$. Then, a fence message $k_{s}$ is dequeue from the local receipt quene $R Q_{i s}$. Finally, a fence message $k_{s}$ is enqueued into the global receipt queue $R Q_{i}$.
3. Methods from the fence method or the top method to the fence message just enqueued are sorted in the significantly dominant relation $\succeq$.
4. A top method in the global receipt queue $R Q_{i}$ is performed according to the execution procedure.

## 6 Evaluation

We implemented the RO scheduler and the locking system with deadlock detection. We evaluate the role ordering (RO) scheduler for a single object in terms of computation time of each method compared with the traditional
two-phase locking (2PL) protocol. Transactions in clients issue methods to the RO scheduler and the locking module on an object base.

In the evaluation, an object o supports ten types of methods. We assume it takes same time to perform every method. We assume one method can be performed for one time unit if there is no other transaction. If multiple conflicting methods are concurrently performed, a method $o p$ has to wait until methods conflicting with op complete. If deadlock is detected in the locking protocol, methods performed in a transaction are undone if the transaction is aborted to release the deadlock. This means, it takes longer to perform a method than one time unit. The computation ratio $\tau$ is defined to be the ratio of the total number of methods effectively performed to the total processing time units. If all the transactions are serially performed, the computation ratio $\tau$ is 1.0 which is the maximum. $\tau=0$ if no method is performed, e.g. every transaction is deadlocked and aborted. A conflicting relation on the methods is randomly defined so that each method averagely conflicts with $10 \%$ of the other methods. There are five roles $R_{1}, \ldots, R_{5}$. Each role $R_{i}$ includes three access rights, which are randomly selected out of ten possible access rights on the object $o$.

There are three subjects $s_{0}, s_{1}$, and $s_{2}$. The subject $s_{0}$ is an owner of the roles $R_{1}, \ldots, R_{5}$. The subject $s_{0}$ grants each role to the other subjects. That is, $s_{0} \succeq_{R_{i}} s_{1}, s_{0}$ $\succeq_{R_{i}} s_{2}$, and $s_{0} \|_{R_{i}} s_{2}$ for every role $R_{i}(i=1, \ldots, 5)$. The roles are ordered as $R_{1} \succeq R_{2} \succeq R_{3}, R_{1} \succeq R_{4} \succeq R_{5}, R_{2}$ $\equiv R_{4}, R_{2} \equiv R_{5}, R_{3} \equiv R_{4}$, and $R_{3} \equiv R_{5}$.


Figure 5. Evaluation of one-object model.
A transaction issues five methods randomly selected from the ten methods of the object, where some method may be invoked multiple times. A role is also randomly assigned to each transaction.

For each configuration, i.e. object, roles and transactions generated based on the random number, the computation ratio $\tau$ is calculated multiple times in the simulation until the average value of the computation ratio is saturated. Figure 5 shows the computation ratio $\tau$ for the number of transactions. The computation ratio $\tau=1.0$ shows the maximum ratio. As shown in Figure 5, the RO scheduler implies higher throughput than the 2PL protocol. For example, the RO scheduler implies six times and ten times higher throughput than the 2PL protocol for 20 and 40 transactions, respectively.

Figures 6 and 7 show average values of processing time of the RO scheduler and the 2PL protocol, respectively, for the total number of transactions. The processing time shows time units from time when a method in each transaction which is assigned with a role $R_{i}(i=1, \ldots, 5)$ issued to time when the method completes. In the RO scheduler, a transaction $T_{i}$ which is assigned with a more significant
role than another transaction $T_{j}$ can manipulate an object o earlier than transactions with less significant roles. On the other hand, the computation order of transactions is independent of the significancy of roles in the 2PL protocol.


Figure 6. RO scheduler.


Figure 7. Two-phase locking (2PL) protocol.

## 7 Concluding Remarks

We discussed a role ordering (RO) scheduler based on role concept in this paper. The role is a central concept to design, implement, and operate information systems. In this paper, multiple conflicting transactions are serializable according to the significantly dominant relation of roles. We also discussed the role ordering (RO) scheduler for single-server and multi-server models and how to implement the $R O$ scheduler. Conflicting methods from multiple transactions are performed in the significantly dominant relation. That is, the more significant role a transaction is assigned, the earlier methods from the transaction are performed.

We evaluated the RO scheduler compared with the traditional two-phase locking protocol (2PL). In the evaluation, we showed the RO scheduler can support higher throughput than the 2PL protocol.

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