# Causally Ordered Delivery of Multimedia Objects

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In distributed applications like teleconferences and teleclassrooms, a group of multiple processes are cooperating, where messages exchanged among the processes are required to be causally delivered. The processes are exchanging kinds of multimedia objects in addition to traditional text data. The multimedia messages are longer than traditional messages and are structured. In this paper, we discuss new types of causally precedent relations among multimedia objects transmitted in the network. We discuss a protocol to causally deliver multimedia objects in a group of multiple processes. We also show the evaluation of the protocol.

### 1 Introduction

In distributed applications like teleconferences, a group of multiple processes are cooperating. Various kinds of group protocols [3, 12] are discussed so far. In the group communication, a group is first established among multiple processes and then messages sent by the processes are causally, totally delivered to the destination processes in the group [3, 5]. A message  $m_1$  causally precedes another message  $m_2$  if a sending event of  $m_1$  happens before a sending event of  $m_2$ . In the totally ordered delivery, even messages not to be causally ordered are delivered to every common destination of the messages in a same order. In the protocols, messages transmitted at the network level are ordered independently of what kinds of information are included in the messages.

In distributed applications, various kinds of multimedia objects like image and video are exchanged among multiple processes in the group. Thus, multimedia objects are structured and are larger and more complex than the traditional data messages. In addition to causally delivering objects, a multimedia object received has to satisfy quality of service (QoS) like frame rate and number of colors required by the destination processes. For example, a destination process is allowed to receive only some part of an object as far as the part satisfies QoS requirement of the application. Some objects may have to be delivered to the applications in predetermined time units after the objects are sent. The papers [1, 2, 15] discuss the  $\Delta$ -causality where  $\Delta$  is the maximum delay time in the system. Tachikawa and Takizawa [13] define the  $\Delta$ - $\epsilon$  causality among messages where  $\Delta_{st}$  is the maximum delay time and  $\epsilon_{st}$  is the maximum ratio of messages between every pair of processes  $p_s$  and  $p_t$ .

The object o is decomposed into a sequence of messages. A message is a unit of data transmitted in the network. If a pair of objects  $o_1$  and  $o_2$  are transmitted by processes  $p_1$  and  $p_2$ , respectively, the messages decomposed from  $o_1$  and  $o_2$ are causally delivered in every common destination process  $p_3$  of  $o_1$  and  $o_2$  according to the traditional group protocols [3]. In an application, the messages of  $o_1$  can be delivered independently of  $o_2$ . The object  $o_1$  is also manipulated independently of  $o_2$ . In another application, the top message of  $o_1$  is required to be delivered before the top of  $o_2$  while the other messages can be delivered in any order. Thus, we define new types of precedent relations of messages based on the object concept. According to the precedent relations, the destination process delivers messages of objects to the application. A pair of messages not to be ordered in the precedent relations can be delivered in any order even if one of them causally precedes the other according to the traditional network-level destination. We discuss a protocol which supports the types of causally precedent relations, named causally ordered multimedia (COM) group protocol, where a fewer number of messages are causally ordered than the traditional network-level group protocols.

In section 2, we present a system model and multimedia objects. In section 3, types of causally precedent relations among multimedia objects are discussed. In section 4, we present the COM protocol for exchanging multimedia objects in a group of processes. In section 5, we show the evaluation of the COM protocol.

### 2 System Model

Distributed applications are realized by cooperation of a group of application processes  $A_1, ..., A_n$   $(n\geq 1)$ . Application processes exchange objects including multimedia data with the other processes in the group by using the network.



Figure 1: Layers.

An application process  $A_t$  is supported by a system process  $p_t$  (t = 1, ..., n) as shown in Figure 1. A system process  $p_s$  takes an object from the application process  $A_s$  and then delivers the object to the system processes supporting the destination application processes by using the basic communication service supported by the network. From here, let a term *process* mean a system process. A data unit exchanged by the processes in the network is referred to as *message*. We assume that the network supports processes with synchronous communication. That is, messages are not lost and delay time between a pair of processes is bounded in the network.

An object is decomposed into a sequence of messages by a source process and the messages are delivered to the destination processes. A destination process  $p_t$  assembles received messages into an object and then delivers the object to the application process  $A_t$ . The cooperation of the processes supporting the group of the application processes is coordinated by a group protocol which supports the reliable, efficient communication service by taking usage of the network service. We discuss a group protocol for delivering multimedia objects to processes in a group.

# **3** Causality of Objects

### 3.1 Causality of messages

Let  $s_t(m)$  and  $r_u(m)$  denote sending and receipt events that processes  $p_t$  and  $p_u$  send and receive a message m, respectively. By using the happen-before relation  $(\prec)$ , the causally precedent relation among messages is defined as follows:

• A message  $m_1$  causally precedes another message  $m_2$  iff  $s_t(m_1)$  happens before  $(\prec)$  $s_u(m_2)$ .

Suppose three processes  $p_s$ ,  $p_t$ , and  $p_u$  are exchanging messages. The process  $p_s$  sends a message  $m_1$  to a pair of processes  $p_t$  and  $p_u$ . The process  $p_t$  sends a message  $m_2$  to  $p_s$  and  $p_u$  after receiving  $m_1$ . Since  $s_t(m_1) \prec s_u(m_2)$ ,  $m_1$  causally precedes  $m_2$ . The process  $p_u$  has to deliver  $m_1$  before  $m_2$ . In order to causally order the messages, the vector clock [5] is widely used in the group protocols [3]. Suppose there are n(>1) processes  $p_1, \ldots, p_n$  in a group G. Each process  $p_t$  manipulates a vector clock  $V = \langle V_1, \ldots, V_n \rangle$  where each element  $V_u$  is initially 0 for  $u = 1, \ldots, n$ . When  $p_t$  sends a message m,  $V_t := V_t + 1$  and m carries the vector clock m.V(=V) of  $p_t$ . On receipt of a message m,  $V_u := \max(V_u, m.V_u)$  for  $u = 1, \ldots, n$  in each destination process of m. For pair of vectors  $A = \langle A_1, \ldots, A_n \rangle$  and  $B = \langle B_1, \ldots, B_n \rangle$ , A < B iff  $A_j \neq B_j$  for  $i = 1, \ldots, n$  and  $A_j < B_j$  for some j. A message  $m_1$  causally precedes another message  $m_2$  iff  $m_1.V < m_2.V$ .

The traditional group protocols [3, 5-9] discuss how to causally and totally deliver *network-level* messages, independently of what kinds of application data are carried by the messages.

### 3.2 Causality of objects

We discuss how a process sends and receives multimedia objects in a group G of multiple processes  $p_1, \ldots, p_n$  (n > 1). Suppose a process  $p_s$ sends an object o to another process  $p_t$ . It takes a longer time to send and receive the multimedia object since the multimedia object is larger and more complex than a traditional message. In order to increase the throughput and reduce the response time, the sending and receiving events of objects are interleaved if there is no precedent relation among the objects. Figure 2 shows three processes  $p_s$ ,  $p_t$ , and  $p_u$  exchanging objects  $o_1$  and  $o_2$ . In Figure 2(3), the process  $p_t$  starts sending messages of an object  $o_2$  after receiving all the messages of another object  $o_1$ . According to the traditional causality theory [5],  $o_1$  causally precedes  $o_2$ . In Figure 2(1),  $p_t$  starts sending a message of the object  $o_2$  before receiving all the messages of  $o_1$ . Here,  $o_1$  does not causally precede  $o_2$ . In Figure 2(2),  $p_t$  sends  $o_2$  while receiving  $o_1$ . On the other hand,  $p_t$  sends  $o_2$  after receiving all the messages of  $o_1$ . Here,  $o_1$  does not causally precede  $o_2$  either.



Figure 2: Precedency of objects.

**[Example 1]** Let us consider an example of a teleconference where the participants are distributed on three remote sites  $S_s$ ,  $S_t$ , and  $S_u$ . The teleconference is realized by a group of three processes  $p_s$ ,  $p_t$ , and  $p_u$ , which support the sites  $S_s$ ,  $S_t$ , and  $S_u$ , respectively, as shown in Figure 2. Each process supports a remote conference site where remote participents join the conference and exchanges messages with the other processes. Participants in the conference share a virtual conference space Cwhich is composed of three subspaces  $C_s$ ,  $C_t$ , and  $C_u$ . Each subspace shows participants attending the conference at each site. The virtual space Cis displayed at each site. Each site  $S_i$  distributes its subspace object  $C_i$  including the image of the site, voice of participants, and manuscripts to be handed out to all the processes in the group (i =

s, t, u). Suppose some participant at the site  $S_s$ supported by the process  $p_s$  expresses some opinion which is shown by a voice and image object  $o_1$ . The process  $p_s$  distributes messages of the object  $o_1$ . After listening to the participant of  $p_s$ , another participant of  $p_t$  expresses a counter opinion for  $o_1$ , which is carried by a multimedia object  $o_2$ . Here, the process  $p_u$  receives messages of the objects  $o_1$  and  $o_2$ . The process  $p_t$  starts sending  $o_2$  after receiving all the messages of  $o_2$ . Hence, the process  $p_u$  has to receive  $o_2$  after  $o_1$  as shown in Figure 2(2).

Next, suppose some participant supported by the process  $p_{i}$  is expressing the opinion which is shown by an object  $o_1$ . While listening to the participant of  $p_s$ , another participant of  $p_t$  is leaving the conference. This image object  $o_2$  showing his leaving the conference is distributed to the processes in the group. The process  $p_u$  has to start delivering  $o_2$  after starting delivering  $o_1$  as shown in Figure 2(1).

Suppose the process  $p_s$  is distributing a music object  $o_1$  which shows that the conference will be closed soon. The music is stopped being played only after every participant leaves the conference. The process  $p_t$  is sending an object showing the participants. Hence, the process  $p_u$  has to deliver  $o_2$  before finishing delivering  $o_1$  as shown in Figure  $2(2).\Box$ 

As presented here, a pair of objects  $o_1$  and  $o_2$ are interrelated with respect to when processes  $p_s$ and  $p_t$  start and finish sending objects as shown in Figures 2. We discuss how a pair of objects  $o_1$  and  $o_2$  can be causally ordered. Let  $ss_t(o)$  and  $es_t(o)$ denote events that  $p_t$  starts sending and finishes sending an object o, respectively. In fact,  $ss_t(o)$ and  $e_{s_t}(o)$  show events that the top message and the last message of the object o are sent by  $p_t$ , respectively.  $sr_t(o)$  and  $er_t(o)$  also mean the receipt events of the top and last messages of the object o, respectively. Let  $sr_t(o)$  and  $er_t(o)$  denote events that  $p_t$  starts and finishes receiving the object  $o_1$ , respectively.

Suppose a precess  $p_t$  receives an object  $o_1$ and sends another object  $o_2$ . An object  $o_1$  is interleaved with another object  $o_2$  if  $sr_t(o_1) \prec$  $ss_t(o_2) \prec er_t(o_1)$  or  $sr_t(o_2) \prec er_t(o_1) \prec es_t(o_2)$  in a source process  $p_t$  of  $o_2$ . Here, the process  $p_t$  is receiving messages of the object  $o_1$  while sending messages of  $o_2$ . Next, suppose  $p_t$  sends  $o_1$  and  $o_2$ .  $o_1$  is interleaved with  $o_2$  if  $ss_t(o_1) \prec ss_t(o_2)$  $\prec es_t(o_1) \text{ or } ss_t(o_2) \prec ss_t(o_1) \prec es_t(o_2).$ 

We now define new types of precedent relations among objects as follows:

**[Definition]** Let  $o_1$  and  $o_2$  be a pair of objects  $o_1$ and  $o_2$  sent by processes  $p_s$  and  $p_t$ , respectively:

- 1  $o_1$  top-precedes  $o_2$   $(o_1 \rightarrow o_2)$  iff
  - $\diamond$  sr<sub>t</sub>(o<sub>1</sub>) happens before (≺) ss<sub>t</sub>(o<sub>2</sub>) if p<sub>s</sub>  $\neq p_t$ .
- $\diamond \ ss_s(o_1) \prec ss_t(o_2) \text{ if } p_s = p_t.$ 2  $o_1$  tail-precedes  $o_2$   $(o_1 \rightarrow o_2)$  iff  $\diamond er_t(o_1) \prec es_t(o_2)$  if  $p_s \neq p_t$ .
  - $\diamond es_s(o_1) \prec es_t(o_2)$  if  $p_s = p_t$ .
- 3  $o_1$  fully precedes  $o_2$   $(o_1 \Rightarrow o_2)$  iff

- $\diamond er_s(o_1) \prec ss_t(o_2)$  if  $p_s \neq p_t$ .
- $\diamond es_s(o_1) \prec ss_t(o_2)$  if  $p_s = p_t$ .
- 4 o<sub>1</sub> inclusively precedes  $o_2$  ( $o_1 \supset o_2$ ) iff  $o_1 \rightarrow o_2$ and  $o_1 \rightarrow o_2$
- 5  $o_1$  exclusively precedes  $o_2$   $(o_1 \sqsupset o_2)$  iff  $o_1 \dashv o_2$ and  $o_2 \rightarrow o_1$
- 6  $o_1$  partially precedes  $o_2$   $(o_1 \rightarrow o_2)$  iff  $o_1 \rightarrow o_2$ ,  $o_1 \rightarrow o_2$ , and  $o_1$  is interleaved with  $o_2 \square$

The top, tail, fully, partially, inclusively, and exclusively precedent relations are referred to as object-causally precedent (o-precedent) relations. Here,  $o_1 \sim o_2$  shows that  $o_1$  object-causally precedes  $o_2$ , i.e.  $\neg \in \{ \rightarrow, \neg, \Rightarrow, \rightarrow, \supset, \exists \}$ . The process  $p_u$  is required to deliver messages of objects  $o_1$  and  $o_2$  so as to satisfy the o-precedent relation  $\rightsquigarrow$  between  $o_1$  and  $o_2$ .

The following properties hold for the types of the object-causally precedent relations:

[**Properties**] Let  $o_1$ ,  $o_2$ , and  $o_3$  be objects.

- **P1**:  $o_1 \Rightarrow o_2$  if  $o_1 \Rightarrow o_3$  and  $o_3 \Rightarrow o_2$ .
- **P2**:  $o_1 \rightarrow o_2$  if  $o_1 \rightarrow o_3$  and  $o_3 \rightarrow o_2$ .
- **P3**:  $o_1 \rightarrow o_2$  if  $o_1 \rightarrow o_3$  and  $o_3 \rightarrow o_2$ . **P4**:  $o_1 \Rightarrow o_3$  if  $o_1 \Rightarrow o_3$  and  $o_3 \rightarrow o_2$ .
- **P5**:  $o_1 \Rightarrow o_2$  if  $o_1 \rightarrow o_3$  and  $o_3 \Rightarrow o_2$ .
- **P6**:  $o_1 \rightarrow o_2$  and  $o_1 \rightarrow o_2$  if  $o_1 \Rightarrow o_2$ .
- **P7**:  $o_1 \Rightarrow o_2$  if  $o_1 \rightarrow o_2$ .
- **P8**:  $o_1 \rightarrow o_2$  and  $o_1 \rightarrow o_2$  if  $o_1 \rightarrow o_2$ .
- **P**9:  $o_1 \supset o_2$  if  $o_1 \supset o_3$  and  $o_3 \supset o_2$ .
- **P10**:  $o_1 \sqsupset o_2$  if  $o_1 \sqsupset o_3$  and  $o_3 \sqsupset o_2$ .
- **P**11:  $o_1 \rightarrow o_2$  if  $o_1 \supset o_2$ .
- **P**12:  $o_1 \rightarrow o_2$  if  $o_1 \sqsupset o_2$ .
- **P**13:  $o_1 \Rightarrow o_2$  if  $o_1 \sqsupset o_3$  and  $o_3 \Rightarrow o_2$ .
- **P**14:  $o_1 \rightarrow o_2$  if  $o_1 \sqsupset o_3$  and  $o_3 \rightarrow o_2$ .
- **P**15:  $o_1 \rightarrow o_2$  if  $o_1 \supset o_3$  and  $o_3 \rightarrow o_2$ .
- **P**16:  $o_1 \rightarrow o_2$  if  $o_1 \rightarrow o_3$  and  $o_3 \rightarrow o_2$ .

The o-precedent relations  $\Rightarrow$ ,  $\rightarrow$ ,  $\rightarrow$ ,  $\rightarrow$ ,  $\rightarrow$ ,  $\supset$ , and  $\Box$  are transitive according to the properties **P**1, **P**2, **P**3, **P**9, **P**10, and **P**16.

#### COM Protocol 4

We present a causally ordered multimedia (COM) protocol for supporting the objectcausally ordered (OCO) delivery of multimedia objects for a group G of multiple processes  $p_{1_1}$ ...,  $p_n$  (n > 1).

#### 4.1 **Object transmission**

A message m sent by a process  $p_s$  carries a sequence number seq. seq is incremented by one each time  $p_s$  sends a message. Here, the processes can simultaneously send multiple objects. Two types of vectors of variables  $V = \langle V_1, ..., V_n \rangle$  and  $A = [A_1, ..., A_n]$  are manipulated for each process in the group G. The vectors V and A are manipulated in a way similar to the vector clock [5]. Each pair of elements  $V_t$  and  $A_t$  are used to show the number of sending events and the number of sending and receipt events occurring in  $p_t$ , respectively (t = 1, ..., n).

Initially, V = (0, ..., 0) and A = [0, ..., 0]. The vectors V and A are manipulated in every process  $p_t$ . First, suppose a process  $p_t$  starts sending an object o. Here, the t-th elements  $V_t$  and  $A_t$  of the vectors V and A are incremented by one:

- $V_t := V_t + 1;$   $A_t := A_t + 1;$

The process  $p_t$  eventually finishes sending the object o. Only the variable  $A_t$  is incremented by one when  $p_t$  finishes sending an object o. However,  $V_t$  is not changed.

•  $A_t := A_t + 1;$ 

Thus,  $V_t$  shows how many sending events of objects occur in  $p_t$ .  $A_t$  shows how many sending and receiving events occur in  $p_t$ . Here, let o.SAand o.SV show values of the vectors A and V, respectively, when  $p_t$  starts sending an object o. Let o.EV and o.EA show the values of the vectors V and A, respectively, when  $p_t$  finishes sending the object o. Hence, let o.V and o.A indicate the values of the vector V and A of the object o, respectively. While  $p_t$  is sending the object o, o.V and o.A are changed if  $p_t$  starts and finishes sending other objects. The object o carries the vector information o.V and o.A to the destina-tion processes. If each message of the object o carries the current values of  $o_1.V$  and  $o_1.A$ , the communication overheads are increased. In order to reduce the communication overheads, the values o.SV and o.SA are carried by a top message of the object o. That is, m.V = o.SV and m.A= o.SA. Every message m following the top message is considered to carry m.V = o.SV and m.A= o.SA. The value o.EA is carried by a last message of the object o. Some messages may be lost due to unexpected delay of the network. In order to increase the reliability, o.SV and o.SA can be carried by multiple messages, e.g. the top message and one message after the top. o.EV and o.DA can also be carried by multiple messages.

On receiving a top message of an object o from a process  $p_s$ , the variables V and A are manipulated in the process  $p_t$  as follows:

- $V_s := \max(V_s, o.SV_s) \ (s = 1, ..., n, s \neq t);$
- $A_s := \max(A_s, o.SA_s) \ (s = 1, ..., n, s \neq t);$

On receiving a last message of the object o, the variables are changed as follows:

•  $A_s := \max(A_s, o.EA_s) \ (s = 1, ..., n, s \neq t);$ 

The following properties among the *object-causally precedent* relations and the vectors hold: **[Theorem]** Suppose that a process  $p_s$  sends an object  $o_1$  to other processes  $p_t$  and  $p_u$ , and another process  $p_t$  sends an object  $o_2$  to a process  $p_u$ .

- $o_1 \Rightarrow o_2$  iff  $o_1.EA_v \leq o_2.SA_v$  (v=1, ..., n,  $v \neq s$ ).
- $o_1 \rightarrow o_2$  iff  $o_1.SV_v \leq o_2.SV_v$  ( $v=1, ..., n, v \neq s$ ).
- $o_1 \rightarrow o_2$  iff  $o_1 \cdot EA_v \leq o_2 \cdot EA_v (v=1, \dots, n, v_n)$  $v \neq s$ ).
- $o_1 \rightarrow o_2$  iff  $o_1.EA_v \ge o_2.SA_v$ ,  $o_1.EA_v < o_2.EA_v$ , and  $o_1.SV_v \le o_2.SV_v$  (v=1, ..., n,  $v \neq s$ ).
- $o_1 \supset o_2$  iff  $o_1.SV_v \leq o_2.SV_v$  and  $o_2.EA_s \leq o_1.EA_s$   $(v=1, ..., n, v \neq s)$ .
- $o_1 \sqsupseteq o_2$  iff  $o_1 . EA_v \le o_2 . EA_v$  and  $o_1 . SV_s > o_2 . SV_s$ .  $(v=1, ..., n, v \ne s).\square$

The objects received are ordered by using the vectors V and A according to the rules on the vectors presented in the theorem.

**[Example 2]** Figure 3 shows three processes  $p_s$ ,

 $p_t$ , and  $p_u$  exchanging objects  $o_1$ ,  $o_2$ , and  $o_3$ . First, the process  $p_s$  starts sending  $o_1$  to  $p_t$  and  $p_u$ . Here,  $o_1.SV = \langle 1, 0, 0 \rangle$  and  $o_1.SA = [1, 0, 0]$ . The process  $p_t$  starts sending the object  $o_2$  while  $p_t$  is receiving the object  $o_1$  from  $p_s$ , i.e.  $o_1 \rightarrow o_2$ . Here,  $o_2.SV = \langle 1, 1, 0 \rangle$  and  $o_2.SA = [1, 1, 0]$ .  $o_1.SV < o_2.SV$ . Then, the process  $p_u$  starts sending an object o3 while receiving the object  $o_2$ . Here,  $o_3.SV = \langle 1, 1, 1 \rangle$  and  $o_3.SA = [1, 1, 1]$ . Since  $o_1.SV < o_3.SV$ ,  $o_1 \rightarrow o_3.\Box$ 



Figure 3: Object-causally ordered delivery.

#### 4.2**Fine synchronization**

In Figure 3, the object  $o_1$  top-precedes  $o_2$  ( $o_1$  $\rightarrow o_2$ ). The process  $p_u$  delivers the messages of  $o_2$ after starting delivering  $o_1$ . The process  $p_u$  can deliver the messages of  $o_2$  just after delivering a top message of  $o_1$ . The process  $p_u$  can also deliver the object  $o_2$  just before  $p_u$  delivers a last message of  $o_1$ . Thus, the object-causally precedent relation does not define the definition of the process of  $o_1$ . dent relation does not define how different it is between the starting times when the objects  $o_1$ and  $o_2$  are started to be transmitted. A special type of message named a synchronization message is sent for each object o to relate  $o_1$  and  $o_2$  at a smaller granularity level. Each time a synchronization message m of the object o is sent,  $V_t$  and  $A_t$  are incremented by one. The top and last messages are also synchronization ones. A sequence of messages of the object o is divided to subsequences. Each subsequence of messages starts at a synchronization message and ends at a next synchronization one. The subsequence is referred to as segment  $s_1$  of the object o. The object o is considered to be a sequence of segments. In Figure 4, an object  $o_s$  is decomposed into seven messages. The messages 1, 4, and 7 are synchronization mes-sages of the object  $o_s$ . The first segment of  $o_s$  is a sequence of messages 1,2, and 3. The second segment  $s_2$  is a sequence of messages 4, 5, 6, and 7. The object  $o_s$  is a sequence of the segments  $s_1$ and  $s_2$ . Here, suppose that the process  $p_t$  starts sending messages of an object  $o_t$  after  $p_t$  starts receiving the object  $o_s$ . If  $p_t$  starts sending  $o_t$  before the synchronization message 4 of o,, every common destination  $p_u$  of  $o_s$  and  $o_t$  starts delivering  $o_t$  before the synchronization message 4 of  $o_s$ . If  $p_t$  starts sending  $o_t$  after receiving the synchronization message 4,  $p_u$  starts delivering  $o_t$  after receiving the first segment  $s_1$  of  $o_s$ . By using the synchronization messages, segments of objects can be causally ordered.



Figure 4: Synchronization messages.

Each segment s of an object o is a sequence of messages. Here, let g(s) shows the number of messages included in the segment s. Let us consider a pair of objects  $o_1$  and  $o_2$  where  $o_1 \rightsquigarrow o_2$ and  $o_2$  is sent by a process  $p_t$  while  $o_1$  is received by  $p_t$ , i.e. interleaving. A segment  $s_1$  of  $o_1$  is referred to as directly precedes a segment  $s_2$  of  $o_2$ iff the top synchronization message of  $s_2$  is sent after receiving the top synchronization message of  $s_1$ .  $p_t$  sends a synchronization message of  $o_2$  if  $p_t$ receives a synchronization message of  $o_1$ .

**[Definition]** An object  $o_1$  *Q*-precedes  $o_2$  iff  $o_1 \rightsquigarrow o_2$ ,  $o_1$  and  $o_2$  are interleaved, and  $g(s_1)/g(s_2) = Q$  for every pair of segments  $s_1$  and  $s_2$  where  $s_1$  directly precedes  $s_2.\square$ 



Figure 5: Quality precedence.

# 5 Evaluation

We evaluate the causally ordered multimedia (COM) group protocol in terms of number of network-level messages to be causally ordered compared with the traditional network-level causality. Suppose that a process  $p_t$  receives messages  $m_{21}, \ldots, m_{2l}$  after sending  $m_1$  and before sending  $m_2$  [Figure 6]. Here, each message  $m_{2i}$ is referred to as properly causally precede the message  $m_2$  ( $i=1, \ldots, l$ ) since there is no message which the process  $p_t$  sends after receiving  $m_{2i}$  before sending  $m_2$ . Let  $D_t(m)$  be a set of messages which properly causally precede a message m in a process  $p_t$ .  $D_t(m_2) = \{m_{21}, ..., m_{2l}\}$  in Figure 6. In the COM protocol, the top and last messages of each object carry the vectors V and A. There is no causal precedency between a pair ob messages  $m_2$  and  $m_{2i}$  unless  $m_2$  or  $m_{2j}$  is the top or last message of an object. Let  $O_t(m)$  be a set of messages which properly causally precede m and are to be ordered in the COM protocol. Let  $N_G$ be the average number of  $|D_t(m)|$  and  $N_{COM}$  be the average number of  $|O_t(m)|$  for every message m.  $N_G$  and  $N_{COM}$  are considered to be metrics to evaluate the protocols because  $N_G$  and  $N_{COM}$ show numbers of messages to be compared with each message in order to causally order messages in the traditional protocol and the COM protocol, respectively. The larger  $N_G$  and  $N_{COM}$  are, the longer it takes to deliver messages.  $N_G$  and  $N_{COM}$  are measured through the simulation.

We make the following assumptions:

- 1. There are n (>1) processes  $p_1, ..., p_n$  in a group G.
- 2. Each process  $p_t$  sends one object at a time and sends totally 1000 objects.
- 3. A process sends an object to all the other processes in the group G.
- 4. Each object is decomposed into one segment composed of  $h (\geq 1)$  messages. Each message carries data of only one object.
- 5. Each process sends one message every  $\tau$  time units.  $\tau$  is a random variable between mint and maxt.  $\bar{\tau}$  is (mint + maxt)/2.
- 6. It takes  $\delta$  time units for a message to arrive at the destination.



Figure 6: Proper precedence.

Figure 7 shows the ratio of  $N_{COM}$  to  $N_G$  for number *n* of the processes in the group *G*. The ratio  $N_{COM}/N_G$  shows how much the COM protocol can reduce the computation and communication overheads. The larger  $\delta/\bar{\tau}$  is, the more distant a pair of processes are.  $\delta/\bar{\tau} = 0.25$  shows a situation when workstations are interconnected in a local area network. The processes exchange objects by using the local area network. Here, each object is transmitted by twenty messages (h = 20). The ratio  $N_{COM}/N_O$  is almost independent of the size *n* of the group. For example,  $N_{COM}/N_O$  is about 0.35, i.e. only 35% of the messages received are handled to be causally ordered in the COM protocol for  $\delta/\bar{\tau} = 0.25$ ,  $\delta/\bar{\tau} = 0.1$  shows a wide area network. Here, about half% of the messages which are causally ordered in the COM protocol.

Figure 8 shows the ratio.  $N_{COM}/N_G$  for number h of messages of an object where  $\delta/\bar{\tau} = 0.25$ ,

 $\delta/\bar{\tau} = 0.1$ , and n = 10. *h* shows the size of each object. The larger an object is, the less ratio of messages are causally preceded in the COM protocol than the traditional one.



Figure 7: Evaluation.



Figure 8: Evaluation.

# 6 Concluding Remarks

This paper discussed a group protocol named COM protocol where multiple processes exchange multimedia objects in a group of the processes. We defined novel types of causally precedent relations among multimedia objects, i.e. top  $(\rightarrow)$ , tail  $(\neg)$ , partially  $(\rightarrow)$ , fully  $(\Rightarrow)$ , inclusive  $(\supset)$ , and exclusive  $(\supset)$  precedent relations. We also designed the COM protocol to support the ordered delivery of objects in the types of the causalities, which uses two types of vector clocks. We showed how the COM protocol can reduce the number of network-level messages to be causally preceded. The COM protocol is now being implemented as processes of Unix operating system by using Sun workstations.

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