# 大規模レンジデータのロバストな同時位置合わせ

西野 恒 池内 克史

東京大学大学院理学系研究科情報科学専攻

{kon, ki}@cvl.iis.u-tokyo.ac.jp

## 概要

文化財の電子的保存を目指すプロジェクトの一貫として、複数枚の距離画像を位置合わせする新たな手法を提案する。特に位置合わせの精度と入力データに含まれるノイズに対する頑健性に重点を置き、M推定を用いた共役勾配法により、すべての距離画像を同時に扱う誤差関数の最小化により同時位置合わせをおこなう。さらに、対応点探索を効率良くより正確におこなうべく、k-d tree データ構造の利用とレーザー反射輝度の誤差尺度への導入をおこなう。また、提案する手法を用いた実験結果を示す。

キーワード: 位置合わせ、レンジデータ、共役勾配法、 M 推定、 k-d tree

# Robust Simultaneous Registration of Multiple Range Images Comprising A Large Number of Points

Ko Nishino Katsushi Ikeuchi

Department of Information Science, Graduate School of Science The University of Tokyo

{kon, ki}@cvl.iis.u-tokyo.ac.jp

#### Abstract

The registration problem of multiple range images is fundamental for many applications that rely on precise geometric models. As part of a project to digitally preserve cultural heritages, we propose a robust registration method that can align multiple range images comprised of a large number of data points. The proposed method minimizes an error function that is constructed to be global against all range images, providing the ability to diffusively distribute errors instead of accumulating them. The minimization strategy is designed to be efficient and robust against outliers by using conjugate gradient search utilizing M-estimator. Also, for "better" point correspondence search, the laser reflectance strength is used as an additional attribute of each 3D data point. For robustness against data noise, the framework is designed not to use secondary information, i.e. surface normals, in its error metric. We describe the details of the proposed method, and present experimental results applying the proposed method to real data.

Key word: registration, range image, conjugate gradient, M-estimator, k-d tree

## 1 Introduction

Registration of multiple point cloud range images is an important and fundamental research topic in both computer vision and computer graphics. Many applications and algorithms can be (are) developed on top of the assumption that accurate geometric models are obtained a priori, i.e. recognition, localization, tracking, appearance analysis, texture-mapping, metamorphis, virutal/mixed reality systems in general etc. Additionally, projects to construct precise geometric models based on observation of real world objects for digital preservation of cultural heritages have drawn attention recently. Because of its objective, these projects require very precise registration of multiple range images.

Recently, we have started a project to digitally archive ancestral heritages in Japan. In addition to natural decay, Japanese cultural heritages are jeopardized to catastophes such as frequent earth quakes and typhoons that can easily deconstruct the national treasures we have inhereted from our anscestors. For these reasons, digitally preserving the precise geometry of those cultural heritages is an urgent demand, so that we can safely pass on our social treasures to the future generations. Also, we plan to acheive detailed analysis of the appearance of those important objects and buildings, not only for preservation but also for restoration of the original states of their appearance and for building multimedia contents that can be shared remotely, i.e. virtually visiting temples in Kyoto without getting on the plane.

In this paper, as a part of the project mentioned above, we propose a framework to register multiple range images robustly. Taking the point cloud images obtained through a laser range scanner as the input, we simultaneously register all range images to sit in one common world coordinate. Considering our purpose, we highly prioritize our efforts to make the resulting registered geometric model accurate compared to making the whole procedure computationally fast. For this reason, we design our registration procedure to be a simultaneous registration method based on an error metric computed from point-point distance including additional laser reflectance attribute in its metric. Also for robustness and efficiency, we adopt a conjugate gradient framework utilizing M-estimator to solve the least-square problem of minimizing the total errors through registration. Since we target large objects like the Great Buddha in Kamakura, the data size of each range image becomes huge. Thus, we employ k-d tree data structure for efficient point-point correspondence search.

The remainder of this paper consists as follows. In section 2, we overview related work and represent our framework. Section 3 describes how point correspondence search will be accomplished efficiently, and we describe the details of how least-square minimization of the

objective function, the core of our simultaneous registration framework, will be done in section 4. We show results of applying our approach to real data in section 5, and section 6 concludes the paper.

## 2 Overview

#### 2.1 Related Work

Past work on range image registration can be roughly classified with respect to the following three aspects.

Strategy: simultaneous or sequential. The basic strategy of registering multiple range images can be representated by two different approaches. The straightforward strategy is to focus on only two range images at a time, and register each range image to another [18]. After one range image pair is registered, a new pair including either range image in the former pair, positioned in the resulting coordinate, is registered. This will be repeated till all range images are used. Since this sequential strategy requires only two range images for each registration stage, it can be implemented with less memory and the overall computatinal cost tends to be cheap. Also, the computatinal cost for each registration stage will not be affected with the number of range images to be registered consequently.

However, this straightforward strategy is well known to be less accurate. In each range image pair registraion stage, some error will be introduced due to data noise etc. Since each range image will be fixed in the resulting position for each registrion stage, this unavoidable error will be propageted to the latter registration stage and it will result in unaffordable error accumulated in the last range image position. Although the "gap" developed by this error accumulation can be small enough depending on the use of the resulting geometric model, it is much preferable to avoid this thoeretically, especially when the geometric model will be used as a basis of texture-mapping or appearance analysis and so on.

Simultaneous registration solves this error accumulation problem by aligning all range images at once [1, 2, 4, 5, 7, 11, 15, 16, 17]. This can be accomplished by defining an error minimization problem by using an error metric common among all range images. This approach can diffusively distribute the registration error over all overlaps of each range image. The drawback is its large computatinal cost compared to sequential approaches.

Matching unit: features or points On registering range images, usually the problem is redesigned as a error (distance) minimization problem. The basis of the error to be measured can be features derived from the range images or points consisting the range data. Feature-based

<sup>&</sup>lt;sup>1</sup>Commonly referred to as "global registration" and "multi-view registration", especially in the graphics community

methods extract some signatures around 3D points, invariant to Euclidean transformation, in each target range image and make correspondences among those features [5, 12, 13]. Based on the assumption that all correspondences are matched correctly, the transformation for registration can be computed in a closed form manner. On the other hand, if the signatures computed from the range images do not provide enough information and the matching of them cannot be done correctly, the registration stage can fail terribly. Point-based methods directly use the 3D points in an iterative manner. The point mates, the point correspondences to compute the error metric, are dynamically updated and several iterative steps are used to minimize the total error. One drawback of this point-based approach is that it requires an initial estimation of the rough transformation between the target range images, which is normally provided by human hand or interaction, while most feature-based approaches do not.

Error metric: point-point distance or point-plane distance Originally, point-based approaches, such as ICP algorithm [3, 21], set the error metric basis on the Euclidean distance between two points corresponding each other [8, 15]. However, since this error metric does not take the surface information into account, the point-based approaches based on point-point distance suffer from the inability to "slide" overlapping range images. An alternative to this distance metric is to use point-plane Euclidean distance, which can be computed by evaluating the distance between the point and its mate's tangent plane [5, 16]. By embedding the surface information into the error metric in this way, point-based approaches utilizing point-plane distance metric tend to be robust against local minima and converge fast. However, computing the point-plane distance is computationally expensive compared with point-point distance computation; thus, methods using viewing direction to find the correspondence are also proposed for efficiency [1, 4, 16].

## 2.2 Our Approach

Based on the consideration described above, we have designed a registration algorithm which is i) based on the simultaneous strategy, ii) using points as matching units, iii) with the point-point distance metric. The framework is inspired by the work of Wheeler et al [19, 20], that applied similar techniques for object recognition and localization.

Since our aim of the underlying project is to digitally preserve cultral heritages, we want to construct the geometric model as accurate as possible. Also we would like to accomplish appearance analysis making heavy use of the geometry. For this reason, as a priliminary step, we attach more importance on robustness and accuracy than computational expence in the registration method. This makes us choose a simultaneous strategy, which is accu-

rate in principle.

We employ points as matching units. Although laser range scanner we use is quite accurate, still the distance to the object is large and the measurement condition is poor in many cases. Because the scanned range images include noise, the information computed from them will be corrupted by that noise even more. Thus, we avoid using any secondary features derived from raw range data; instead, we directly use data points as matching units.

We use the point-point distance metric. Due to the noise problem, as mentioned above, we have to avoid obtaining secondary features, surface normals in this case, and thus, cannot use the point-plane metric that requires us to calculate surface normals. It is also true that point-point metric is less expensive in computational cost than the point-plane metric, and is preferable when the data set is very large.

The overall simultaneous registration framework can be described as an iteration of the following procedure till it converges.

Procedure Simultaneous Registration

Array KDTrees, Scenes, PointMates

foreach r in AllRangeImages KDTrees[r] = BuildKDTree(r)

foreach r in AllRangeImages

foreach s in AllRangeImage-r Scenes[s] = s

foreach i in Pointsof(r) foreach s in Scenes

PointMates[i] += CorrespondenceSearch(i, KDTree[s])

Transformations[r] = TransformationStep(PointMates)

TransformAll(AllRangeImages, Transformations)

We basically extend the framework of pairwise ICP algorithm to handle multiple range images simultaneously. This is achieved by setting up an objective function to minimize globally with respect to each range images. Defining model as the particular range image in interest and scene as one of the range images in the rest of range images set, in one simultaneous registration loop, each range image becomes a model once. Point mate search (search for nearest neighbor point) for each point in the model will be done against all scene range images (M-1)if we have M range images), and they will be stored in a global array. Rigid transformation for the current model will be computed in a conjugate gradient search framework utilizing M-estimator, and will be stored in a global array. After each range image has become a model once. all range images are transformed using the transformation stored in the global array. Note each range image is

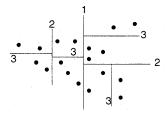


Figure 1: K-d tree subdivision of 2D points. The number indicates which level of the tree at which the split occurs.

not transformed immediately. Considering that each step transformation evaluated inside one simultaneouse registration procedure will not be so large, this latency of transformation will not cause a problem. Furthermore, this timing of transformation saves us a large amount of computational time, since construction of k-d trees are required only once per range image in one simultaneous registration procedure. Details will be discussed in the following sections.

## 3 Point Mate Search

#### 3.1 K-D Tree

As we try to register range images that consist of a large amount of 3D points, finding correspondences for each point in each range image can easily dominate a critical portion of the overall computational time. To obtain point correspondences efficiently, we employ k-d tree structure to store the range images [9]. K-d tree's k-d abbreviates k-dimensional and it is a generalization of binary-search tree for efficient search in high dimension space. The k-d tree is created by recursively splitting a data set down the middle of its dimension of greatest variance. The splitting continues until the leaf nodes contain a small enough number of data points. For instance, Figure 1 shows how 2D data point set is split and separated into leaf nodes.

The k-d tree constructed will become a tree of depth  $O(\log N)$  where N is the number of points stored. Nearest-neighbor search can be accomplished by following the appropriate branches of the tree until a leaf node is reached. A hyper-sphere centered at the key point with radius of the distance to the current closest point can be used to determine which, if any, neighboring leaf nodes in the k-d tree must be checked for closer points. Once we tested all the data in leaf nodes which could possibly be closer, we are guaranteed to have found the closest point in the tree. Though its worst case complexity is O(N), the expected number of operations for nearest-neighbor search is  $O(\log N)$ , which will be the case if the data is

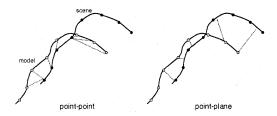


Figure 2: Point correspondences using point-point and point-plane distance metric.

evenly distributed. For the cases of storing surfaces in 3D space in k-d tree, usually this even distribution assumption holds. The largest overhead involved in using k-d trees is that the k-d tree of range-image points must be built prior to the search. This operation costs  $O(N\log N)$ . To avoid making this computational expence critical, we update each range image positions only once in one simultaneous registration procedure as listed in the psuedo code in section 2.2, requiring only M times of k-d tree rebuilts in one global iteration where M is the number of range images.

#### 3.2 Distance Metric

To utilize nearest-neighbor search based on k-d tree structure, we need a measure of dissimilarity between a pair of points. The dissimilarity,  $\Delta$ , between k-d points  $\mathbf x$  and  $\mathbf y$  must have the form

$$\Delta(\mathbf{x}, \mathbf{y}) = F(\sum_{i=1}^{k} f_i(\mathbf{x}_i, \mathbf{y}_i))$$
 (1)

where the functions  $f_i$  are symmetric functions over a single dimension and functions  $f_i$  and F are monotonic. All distances satisfy these conditions including the Euclidean distance  $\|\mathbf{x} - \mathbf{y}\|$ . As mentioned in section 2.1, using point-plane distance as the error metric provides faster convergence. However, the point-plane distance, which can be computed by

$$\Delta(\mathbf{x}, \mathbf{y}) = (\mathbf{x} - \mathbf{y}) \cdot \mathbf{N_v} \tag{2}$$

does not satisfy the monotonic condition. To take advantage of the efficiency of k-d tree structure, we use the point-point Euclidean distance as the dissmilarity measure. Also, we prefer point-point distance for the sake of robustness; avoiding the usage of secondary information derived from raw data, such as surface normals in point-plane, which can be sensitive to noise in the raw data points.

Figure 2 depicts an example of point correspondences in the case of using point-point distance metric and point-



Figure 3: Images using laser reflectance strength as pixel values.

plane distance metric. While the point-point distance metric searches for the nearest neighboring point, meaning estabilishing a discrete mapping of one surface to another, the point-plane distance metric can be considered as a way to find the continuous mapping of one surface to another. In cases like Figure 2, where the *model* surface has to be "slided" to fit the *scene* surface, the point-plane approach succeeds to find the correspondencs that enables us to compute the rigid transformation close to the sliding direction, while the point-point approach tends to get stuck in a local minima because of the inability to find point mates in the sliding direction. This sliding ablity of point-plane approaches provides faster convergence compared to using point-point distance metric.

To compensate the inablity of sliding in point-point based distance measurement, we need some information to be attached to the 3D points that suggest better matches. For this purpose, we use the laser reflectance strength value (refered to as RSV in the rest of this paper) as an attribute of each 3D point. Most laser range finders return the strength of the laser reflected at each surface point that it measured as an additional output value. Figure 3 shows two images with RSVs used as the pixel values. For better visualization the images are histogram equalized. As it can be seen, the RSVs are mostly invariant against Euclidean transformation, since the dominant factor of the power of laser reflected at an object surface is its surface material. One common method to utilize two different sources of information in distance measurement, in this case the position distance and RSV distance, is to set up a combined metric, such as

$$\Delta(\mathbf{x}, \mathbf{y}) = [(x_{\mathbf{x}} - x_{\mathbf{y}})^2 + (y_{\mathbf{x}} - y_{\mathbf{y}})^2 + (z_{\mathbf{x}} - z_{\mathbf{y}})^2 + \lambda(r_{\mathbf{x}} - r_{\mathbf{y}})^2]^{\frac{1}{2}}$$
(3)

where r is RSV and  $\lambda$  is a constant scalar. However, this scalar introduces a tedious and ad hoc effort in finding the "best"  $\lambda$ . Instead, we use the reflectance to determine the best pair among candidates of closest points. Namely,

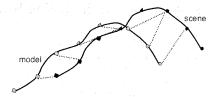


Figure 4: Point mates using point-point distance metric with reflectance strength values. Different shape marks indicate different reflectance strength values.

we first search for multiple (m) closest points in the k-d tree, and then evaluate the RSV distance for each of them to get the closest point with respect to laser reflectance strength value. We gradually reduce the number of the candidates m along the iteration so as to make it inversely proportional to the number of iterations. This utilization of the laser reflectance is similar to [14], which uses color attribute to narrow down the closest point candidates. Figure 4 depicts how the point-point distance metric utilizing RSV as additional attribute works in the example case depicted in Figure 2 (m=4) in this example).

## 3.3 Random Sampling

Even we employ k-d tree structure for efficient point correspondence search, when the number of points in the target range images get large, the computational cost becomes massive. In early stages of the simultaneous registration, when the range images are distributed apart, it is more important to get them close to each other than accurately computing the rigid transformation for each registration step. To provide a way to speed up the registration, we subsample each range image to reduce the number of points used in the registration process. The points in each range images are given a sequential identification number m = 0, ..., M - 1 and a uniformly distributed random number within the interval [0, M-1] is generated to pick up the points to be used. The seed number to generate the random numbers are common for all range images in one simultaneous registration procedure and updated once per one global registration step. In current implementation, we let the user determine the percentile of points to be used in each range image intaractively. In future implementation, this can be done automatically; first using small percentage and gradually increased to reach one hundred percent.

## 4 Least-square Minimization Strategy

## 4.1 Representing Transformation

Given a set of corresponding points  $(\mathbf{x}_i, \mathbf{y}_i)$  where i = 0, ..., N-1, the registration problem is to compute the rigid transformation which registers the *model* points  $\mathbf{x}_i$  with their corresponding *scene* points  $\mathbf{y}_i$ . The rigid transformation can be specified by a pair of a  $3 \times 3$  rotation matrix  $\mathbf{R}$  and a 3D translation vector  $\mathbf{t}$ . When the corresponding points are aligned each other  $\mathbf{y}_i$  can be written as

$$\mathbf{y}_i = \mathbf{R}\mathbf{x}_i + \mathbf{t} \tag{4}$$

Since range data points will be contaminated by noise, the range image registration problem can be described as a error minimization problem with the error funtion as follows

$$f(\mathbf{R}, \mathbf{t}) = \sum_{i} \|\mathbf{R}\mathbf{x}_{i} + \mathbf{t} - \mathbf{y}_{i}\|^{2}$$
 (5)

to minimize with regards to  $(\mathbf{R} \ \mathbf{t})$ . As mentioned in section 2.2, i will stand for all point mates established from all pairs of range images (if there is M range images, i will include all point mates from  $M \times (M-1)$  range image pairs). Although it is convenient for vector computation to represent the rotation as a  $3 \times 3$  matrix  $\mathbf{R}$ ,  $\mathbf{R}$  will be constrained in a non-linear way as follows (T stands for transpose).

$$\mathbf{R}\mathbf{R}^T = \mathbf{I}$$
$$|\mathbf{R}| = 1$$

It is difficult to take advantage of the linear matrix representation of rotation while satisfying these constraints. For this reason, we will use the quaternion representation for rotation, which is a well known solution to this rotation problem. The benefits of using quaternion will be described later. Thus, the position parameters of each range image and the rigid transformation to register all of them will be represented with seven element vectors as follows.

$$\mathbf{p} = [\mathbf{q}^T \mathbf{t}^T]^T$$

$$where \mathbf{q} = [u v w s]^T$$
(6)

### 4.2 M-Estimator

As seen in section 4.1, the registration problem can be described as a least-square minimization problem with the objective function equation (5). Point correspondences are acquired using the techniques described in section 3. On solving this error minimization problem, we will have to deal with two problems,

**Poor initial correspondences** We must assume that the point correspondences established in the beginning will include a lot of mismatches.

Outliers Even when most of the point correspondences are correct, we still have to deal with outliers resulting from mismatches and noise corrupted data points.

The underlying problem here is how to robustly reject outliers. The following three representative classes of solutions can be found in the field of robust statics. The first class of solutions, outlier thresholding, is the simplest and most computationaly cheap technique thus the most prominent techinque used in vision applications. The basic idea is to estimate the standard deviation  $\sigma$  of the errors in the data and eliminate data points which have errors larger than  $|k\sigma|$  where k is typically greater than or equal to 3. The problem of outlier thresholding is that a hard threshold is determined to eliminate the outliers. This means regardless of where the threshold is chosen, some number of valid data points will be classified as outliers and some number of true outliers will be classified as valid. In this sense, it is unlikely that a perfect method for selecting the threshold exists unless the outliers are all known a priori. The second class of robust estimators is the median/rank estimation methods. The basic idea is to select the median or kth value (for some percentile k) with respect to the errors for each observation and use that value as our error estimate. The logic behind this is that the median is almost guaranteed not to be an outlier as long as half of the data is valid. An example of median estimators is the least-median-of-squares method (LMedS). LMedS computes the parameters of interest which minimizes the median of the squared error computed from all data pairs using that parameter. Essentially, this requires an exhaustive search of possible values of the parameters by testing least-squares estimates using that parameter for all possible combinations of point correspondences. While these median-based techniques can be very robust, this exhaustive search remains a large drawback.

The third class of robust techniques is M-estimation; the one we use. The general form of M-estimators allows us to define a probability distribution which can be maximized by minimizing a funtion of the form

$$E(z) = \sum_{i} \rho(z_i) \tag{7}$$

where  $\rho(z)$  is an arbitrary function of the errors  $z_i$  in the data set. The M-estimate is the maximum-likelihood estimate of the probability distribution P equivalent to E(z). Least-squares estimation, such as minimizing (5), corresponds to M- estimation with  $\rho(z)=z^2$ .

$$P(z) = e^{-E(z)} = e^{-\sum_{i} z_{i}^{2}}$$
 (8)

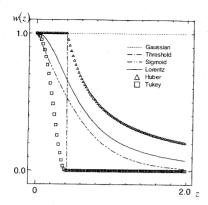


Figure 5: Weight values corresponding to several Mestimation functions.

We can find the parameters p that minimize E by taking the derivative of E with respect to p and setting it to 0.

$$\frac{\partial E}{\partial \mathbf{p}} = \sum_{i} \frac{\partial \rho}{\partial z_{i}} \cdot \frac{\partial z_{i}}{\partial \mathbf{p}} = \sum_{i} w(z_{i}) z_{i} \frac{\partial z_{i}}{\partial \mathbf{p}} = 0 \quad (9)$$

where  $w(z) = \frac{1}{z} \frac{\partial \rho}{\partial z}$ 

As can be seen in (9), M-estimation can be interpreted as weighted-least square minimization with the weight function w being a function of data points  $z_i$ . Figure 5 shows the plots of the respective weight functions corresponding to several M-estimation functions. In our current implementation, we use the Lorentz's function as the M-estimator, which we found to work best with our range image data.

## 4.3 Putting It Together

Now, we can redefine our registration problem as follows. Given a set of corresponding points  $(\mathbf{x}_i, \mathbf{y}_i)$  (i=0,...,N-1), we will minimize

$$E(\mathbf{p}) = \frac{1}{N} \sum_{i}^{N} \rho(z_i(\mathbf{p}))$$
 (10)

where 
$$z_i(\mathbf{p}) = \|\mathbf{R}(\mathbf{q})\mathbf{x}_i + \mathbf{t} - \mathbf{y}_i\|$$
 (11)

and 
$$\rho(z_i) = \log(1 + \frac{1}{2}z_i^2)$$
 (12)

The minimization of function E can be accomplished in a conjugate gradient search framework. Conjugate gradient search is a variation of gradient descent search, which constrains each gradient step to be conjugated to the former gradient step. This constraint avoids much of the zigzagging that pure gradient descent will often suffer from, and consequently provides faster convergence.

On applying conjugate gradient search to our minimization problem, we need to compute the gradient of function E with respect to pose parameter p which can be described as equation (9). For the following deriviations, we redefine  $z_i$  to be

$$z_i(\mathbf{p}) = \|\mathbf{R}(\mathbf{q}\mathbf{x}_i) + \mathbf{t} - \mathbf{y}_i\|^2$$
 (13)

A priori to the computation of the gradient, we pre-rotate the model points, so that the current quaternion is  $\mathbf{q}_I = [0\ 0\ 0\ 1]^T$  which has the property that  $\mathbf{R}(\mathbf{q}_I) = \mathbf{I}$ . This allows us to take advantage of the fact that the gradient of  $\mathbf{R}(\mathbf{q})\mathbf{x}$  can easily be evaluated at  $\mathbf{q} = \mathbf{q}_I$ :

$$\frac{\partial (\mathbf{R}\mathbf{x})}{\partial \mathbf{q}} \mathbf{x} = 2\mathbf{C}(\mathbf{x})^T \tag{14}$$

where C(x) is the 3 × 3 skew-symmetric matrix of the vector x which has the useful characteristic as follows.

$$\mathbf{C}(\mathbf{x})\mathbf{y} = \mathbf{x} \times \mathbf{v} \tag{15}$$

where  $\times$  is the cross product. With these facts,  $\frac{\partial z_i}{\partial \mathbf{p}}$  in equation (9) can be derived as

$$\frac{\partial z_i}{\partial \mathbf{p}} = 2(\mathbf{R}(\mathbf{q})\mathbf{x}_i + \mathbf{t} - \mathbf{y}_i) \frac{\partial (\mathbf{R}(\mathbf{q})\mathbf{x}_i + \mathbf{t} - \mathbf{y}_i)}{\partial \mathbf{p}}$$

$$= \begin{bmatrix} 2(\mathbf{x}_i + \mathbf{t} - \mathbf{y}_i) \\ 4\mathbf{C}(\mathbf{x})^T (\mathbf{x}_i + \mathbf{t} - \mathbf{y}_i) \end{bmatrix}$$

$$= \begin{bmatrix} 2(\mathbf{x}_i + \mathbf{t} - \mathbf{y}_i) \\ 4\mathbf{x}_i \times (\mathbf{t} - \mathbf{y}_i) \end{bmatrix} \tag{16}$$

## 5 Results

We have applied the proposed method to register real data. the Great Buddha in Kamakura. The Great Buddha was scanned from fourteen different directions using Cyrax 2000<sup>2</sup>, a time-of-flight laser range scanner that can scan up to 100m with  $\pm 6$ mm error at 50m distance. Each point cloud image consists of approximately three to four million vertices. Since registering all range images with full resolution requires massive computational resource and time, we registered only eight of those range images in 1/25 resolution as a priliminary experiment. Figure 6 shows the resulting registered Great Buddha. First the input range images were registered in a pairwise manner with occasional human interaction for initial alignment, and then registered simultaneously. The variance of Lorentz's function was set large in the beginning and then gradually decreased each time the registration procedure converged with a particular variance value. Each stage took about five to ten iterations for convergence.

<sup>&</sup>lt;sup>2</sup>Cyra Technologies Inc.



Figure 6: Registered Great Buddha. Different color indicates different range image.

## 6 Conclusion and Future Work

We have proposed a framework to simultaneously register multiple range images. The simultaneous registration problem is redefined as a least-square problem with an objective function globally constructed with respect to each range image. For efficiency, we employ k-d tree structure for fast point correspondence search and apply conjugate gradient search in minimizing the least-square problem for faster convergence. For robustness, we employ the laser reflectance strength as an additional attribute of the 3D points and search for "better" point mates based on their distance. Also, M-estimator is used for robust outlier rejection.

For future work, we definitely have to compare our methods quantatitavely with other existing range image registration methods. Also we plan to automate initial estimation of the rigid transformations to pass to the simultaneous registration program, which is currently done by human interaction.

## Ackknowledgment

This research was, in part, supported under CREST Ikeuchi project by Japan Science and Technology Corporation (JST).

## References

- [1] R. Benjemma and F. Schmitt. Fast global registration of 3d sampled surfaces using a multi-z-buffer technique. In *Proc. Int. Conf. On Recent Advances in 3-D Digital Imaging and Modeling*, pages 113–120, May 1997.
- [2] R. Bergevin, M. Soucy, H. Gagnon, and D. Laurendeau. Towards a general multi-view registration technique. *IEEE Trans. Patt. Anal. Machine Intell.*, 18(5):540–547, May 1996.

- [3] P.J. Besl and N.D. McKay. A method for registration of 3-d shapes. IEEE Trans. Patt. Anal. Machine Intell., 14(2):239–256. Feb 1992.
- [4] G. Blais and M.D. Levine. Registering multiview range data to create 3d computer objects. *IEEE Trans. Patt. Anal. Machine Intell.*, 17(8):820–824. Aug 1995.
- [5] Y. Chen and G. Medioni. Object modeling by registration of multiple range images. *Image and Vision Computing*, 10(3):145–155, Apr 1992.
- [6] C. Dorai, G. Wang, A.K. Jain. and C. Mercer. From images to models: Automatic 3d object model construction from multiple views. In Proc. of the 13th IAPR International Conference on Pattern Recognition, pages 770–774, 1996.
- [7] D.W. Eggert, A.W. Fitzgibbon, and R.B. Fisher. Simultaneous registration of multiple range views for use in reverse engineering. Technical Report 804, Dept. of Artificial Intelligence. University of Edinburgh, 1996.
- [8] O.D. Faugeras and M. Hebert. The representation, recognition, and locating of 3-d objects. *International Journal of Robotic Research*, 5(3):27–52, Fall 1986.
- [9] J.H. Friedman, J.L. Bentley, and R.A. Finkel. An algorithm for finding best matches in logarithmic expected time. ACM Trans. On Mathematical Software, 3(3):209–226, 1997.
- [10] G. Godin, M. Rioux, and R. Baribeau. Three-dimensional registration using range and intensity information. In *Proc. SPIE vol.2350: Visionmetrics III*, pages 279–290, 1994.
- [11] H. Jin, T. Duchamp, H. Hoppe, J.A. McDonald, K. Pulli, and W. Stuetzle. Surface reconstruction from misregistered data. In Proc. SPIE vol. 2573: Vision Geometry IV, pages 324–328, 1995.
- [12] A. Johnson. Spin-Images: A Representation for 3-D Surface Matching. PhD thesis, Robotics Institute, Carnegie Mellon University, Pittsburgh, PA, Aug 1997.
- [13] A. Johnson and M. Hebert. Surface registration by matching oriented points. In *Proc. Int. Conf. On Recent Advances in 3-D Digital Imaging and Modeling*, pages 121–128, May 1997.
- [14] A. Johnson and S.B. Kang. Registration and integration of textured 3-d data. In Proc. Int. Conf. On Recent Advances in 3-D Digital Imaging and Modeling, pages 234–241, May 1997.
- [15] T. Masuda, K. Sakaue, and N. Yokoya. Registration and integration of multiple range images for 3-d models construction. In Proc. IEEE Conf. on Computer Vision and Pattern Recognition, pages 879–883, Jun 1996.
- [16] P. Neugebauer. Geometrical cloning of 3d objects via simultaneous registration of multiple range images. In Proc. Int. Conf. on Shape Modeling and Application, pages 130–139, Mar 1997.
- [17] K. Pulli. Multiview registration for large data sets. In Second Int. Conf. on 3D Digital Imaging and Modeling, pages 160–168, Oct 1999.
- [18] G. Turk and M. Levoy. Zippered polygon meshes from range images. In SIGGRAPH 94, pages 311–318, Jul 1994.
- [19] M.D. Wheeler. Automatic modeling and localization for object recognition. PhD thesis, Robotics Institute, Carnegie Mellon University, Pittsburgh, PA, Oct 1996.
- [20] M.D. Wheeler and K. Ikeuchi. Sensor modeling, probablistic hypothesis generation, and robust localization for object recognition. *IEEE Trans. Pattern Analysis and Machine Intelligence*, 17(3):252–265, 1995.
- [21] Z. Zhang. Iterative point matching for registration of free form curves and surfaces. *International Journal of Computer Vision*, 12(2):119–152, 1994.