

# オプティカルフローと独立成分分析によるドミナントプレーン検出

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**あらまし** ドミナントプレーンとは画像の最大領域を占める平面であり、それを検出することはロボットナビゲーションなどにおいて有益である。本論文では、移動するカメラから得られるオプティカルフローに対して独立成分分析を行うことで、ドミナントプレーンを検出するアルゴリズムを提案する。障害物が含まれないシーンから得られるオプティカルフローと、障害物が含まれたシーンから得られるオプティカルフローを独立成分分析の入力値として用いる。出力結果に統計的な処理を施し、ドミナントプレーンの領域を検出する。実画像を用いた実験結果を示す。

## Dominant plane detection using optical flow and Independent Component Analysis

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**Abstract** Dominant plane is an area which occupies the largest domain in the image. The dominant plane estimation is an essential task for the autonomous navigation and the path planning of the mobile robot equipped with a vision system, since the robot moves on the dominant plane. In this paper, we develop an algorithm for dominant plane detection using optical flow and Independent Component Analysis. Since the optical flow field is a mixture of flows of the dominant plane and the other area, we separate the dominant plane using Independent Component Analysis. Using the initial data as a supervisor signal, the robot detects the dominant plane. For each image in a sequence, the dominant plane corresponds to an independent component. This relation provides us a statistical definition of the dominant plane. Experimental results using real image sequence show that our method is robust against the non-unique velocity of the mobile robot.

## 1 Introduction

In this work, we aim to develop an algorithm for dominant plane detection using the optical flow observed by means of a vision system mounted on a mobile robot. The dominant plane is a planar area which occupies the largest domain in the image observed by a camera. Assuming that the robot moves on the dominant plane (e.g., floors and ground areas), dominant plane estimation is an essential task for the autonomous navigation and the path planning of the mobile robot.

For the autonomous navigation of mobile robots, vision sensors and sonar or laser sensors are generally used. Sonar and laser sensors [1] provide simple methods of obstacle detection. These sensors are effective in obstacle detection for collision avoidance, since these methods can obtain range information to an ob-

ject. On the other hand, stationary vision sensors have difficulty in obtaining range information. However, vision sensors mounted on a mobile robot can obtain an image sequence from the camera motion. The image sequence provides the motion and structure from correspondences of points on successive images [2]. Additionally, vision sensors are fundamental devices for the understanding of the environment, since the robot collaborates with a human being. Moreover, visual information is valid for the path planning of the mobile robot in a long sequence, because the vision system can capture environmental information quickly for a large area compared to present sonar- and laser-based systems.

There are many methods for the detection of obstacles or planar areas using vision systems [3]. For example, the edge detection of omni and monocular

camera systems [4] and the observation of landmarks [5] are the classical ones. However, since these methods are dependent on the environment around a robot, they are difficult to apply in general environments. If a robot captures an image sequence of moving objects, the optical flow [6] [7] [8], which is the motion of the scene, is obtained for the fundamental features in order to construct environment information around the mobile robot. Additionally, the optical flow is considered as fundamental information for the obstacle detection in the context of biological data processing [9]. Therefore, the use of optical flow is an appropriate method from the viewpoint of the affinity between the robot and human being.

The obstacle detection using optical flow is proposed in [10] [11]. Enkelmann [10] proposed an obstacle-detection method using the model vectors from motion parameters. Santos-Victor and Sandini [11] also proposed an obstacle-detection algorithm for a mobile robot using the inverse projection of optical flow to ground floor, assuming that the motion of the camera system mounted on a robot is pure translation with a uniform velocity. However, even if a camera is mounted on a wheel-driven robot, the vision system does not move with uniform velocity due to mechanical errors of the robot and unevenness of the floor.

Independent Component Analysis(ICA) [12] provides a powerful method for texture analysis, since ICA extracts dominant features from textures as independent components [13][14]. Optical flow is a texture yielded on surfaces of objects in an environment observed by a moving camera. Therefore, it is possible to extract independent features from flow vectors on pixels dealing with flow vectors as textures. Consequently, we use ICA to separate the dominant plane and the other area.

In Section 2, we briefly present ICA, and we show that separation of pixels in a scene applies ICA to flow vectors of pixels. Section 3 presents an algorithm for the detection of the dominant plane from optical flow. In Section 4, we show experiments for the detection of the dominant plane using a real image sequence observed by the camera mounted on a mobile robot. we show the validity of own method for a robot navigation.

## 2 Application of ICA to optical flow

ICA [12] is a statistical technique for the separation of original signals from mixture signals. Assume that the mixture signals  $x_1(t)$  and  $x_2(t)$  are expressed as a linear combination of the original signals  $s_1(t)$  and  $s_2(t)$ , that is,

$$x_1(t) = a_{11}s_1(t) + a_{12}s_2(t), \quad (1)$$

$$x_2(t) = a_{21}s_1(t) + a_{22}s_2(t), \quad (2)$$

where  $a_{11}$ ,  $a_{12}$ ,  $a_{21}$ , and  $a_{22}$  are weight parameters of the linear combination. Using only the recorded signals  $x_1(t)$  and  $x_2(t)$  as an input, ICA can estimate the original signals  $s_1(t)$  and  $s_2(t)$  based on the statistical properties of these signals.

We apply ICA to the optical flow observed by a camera mounted on a mobile robot for detection of the feasible region on which the robot can move. The optical-flow fields are suitable for the input signals to ICA, since the optical flow observed by the moving camera is expressed as the linear combination of the motion field of the dominant plane and the other objects, as shown in Fig.1. Assuming that the motion field of the dominant plane and the other objects are spatially independent components, ICA enables us to detect the dominant plane on which robot can moves. For each image in a sequence, we assume that optical flow vectors in the dominant plane corresponds to an independent component. as shown in Fig.2.

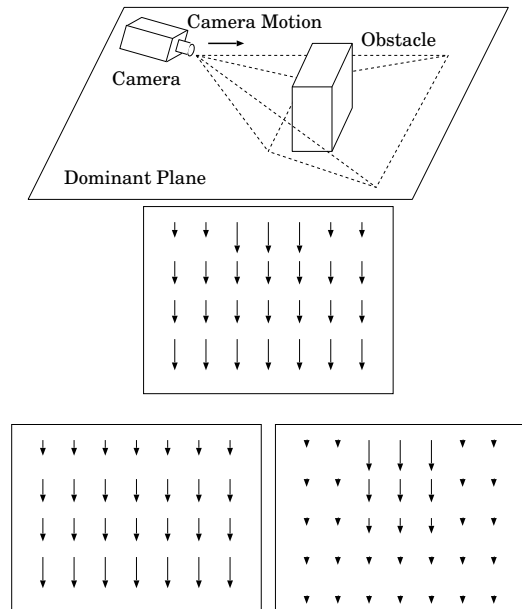


Figure 1: Top-left: Example of camera displacement and the environment with obstacles. Top-right: Optical flow observed through the moving camera. Bottom-left: The motion field of the dominant plane. Bottom-right: The motion field of the other objects. The optical flow(top-right) is expressed as the linear combination of bottom motion fields.

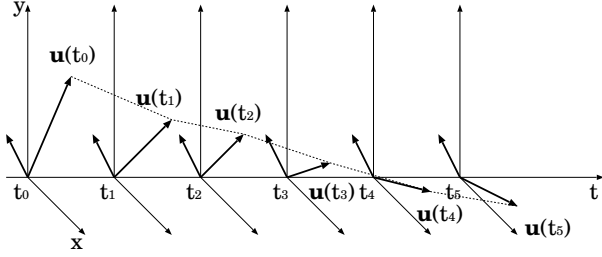


Figure 2: Dominant vector detection in a sequence of images.  $\mathbf{u}(t_i)$  corresponds to the dominant vector which defines the dominant plane at time  $t_i$ .

### 3 Algorithm for dominant plane detection from image sequence

In this section, we develop an algorithm for the detection of the dominant plane from the image sequence observed by a camera mounted on a mobile robot. When the camera mounted on the mobile robot moves on the ground plane, we obtain successive images which include a dominant plane area and obstacles. Assuming that the camera is mounted on a mobile robot, the camera moves parallel to the dominant plane. Since the computed optical flow from the successive images describes the motion of the dominant plane and obstacles on the basis of the camera displacement, the difference between these optical flow vectors enables us to detect the dominant plane area. The difference of the optical flow is shown in Fig.3.

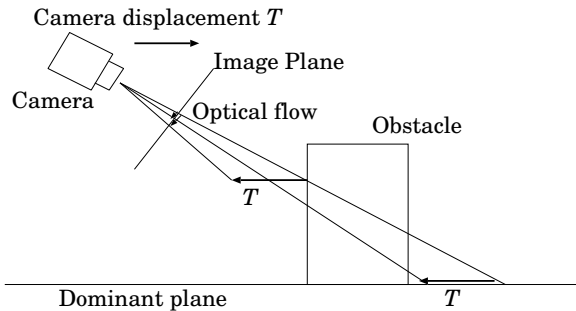


Figure 3: The difference of the optical flow between the dominant plane and obstacles. If the camera moves in the distance  $T$  parallel to the dominant plane, optical flow vector at the obstacles area in the image plane shows that the obstacle moves in the distance  $T$ , or optical flow vector at the dominant plane area in the image plane shows that the dominant plane moves in the distance  $T$ . Therefore, the camera observes difference optical flow vector between the dominant plane and obstacles.

### 3.1 Learning supervisor signal

First, we capture image sequence  $\hat{I}(x, y, t)$  at time  $t$  without obstacles as shown in Fig.4 and compute optical flow  $\hat{\mathbf{u}}(t) = (\frac{dx}{dt}, \frac{dy}{dt})$  as

$$\hat{\mathbf{u}}(t)^\top \nabla \hat{I}(x, y, t) + \hat{I}_t = 0, \quad (3)$$

where  $x$  and  $y$  are the pixel coordinates of a image. For the detail of the computation of this equation, see [6][7][8].

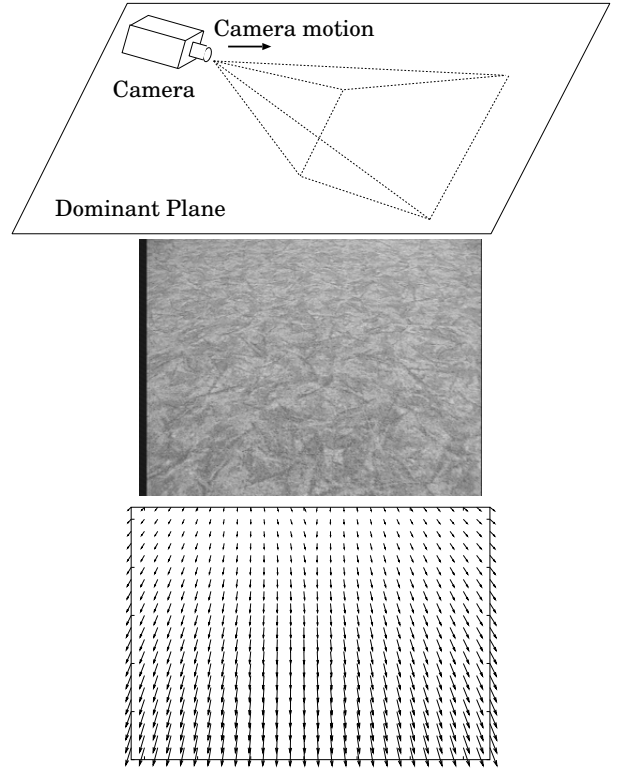


Figure 4: Captured image sequence without obstacles. Top: Example of camera displacement and the environment without obstacles. Bottom-left: An image of the dominant plane  $\hat{I}(x, y, t)$ . Bottom-right: Computed optical flow  $\hat{\mathbf{u}}(t)$ .

After we compute the optical flow  $\hat{\mathbf{u}}(t)$ , frame  $t = 0 \dots n$ , we create the supervisor signal  $\hat{\mathbf{u}}$ ,

$$\hat{\mathbf{u}} = \frac{1}{n} \sum_{t=0}^n \hat{\mathbf{u}}(t). \quad (4)$$

### 3.2 Dominant plane detection using ICA

Next, we capture image sequence  $I(x, y, t)$  with obstacles as shown in Fig.5 and compute optical flow  $\mathbf{u}(t)$  in the same way.

The optical flow  $\mathbf{u}(t)$  and the supervisor signal  $\hat{\mathbf{u}}$  are used as an input signal for ICA. Setting  $\mathbf{v}_1$  and  $\mathbf{v}_2$  to

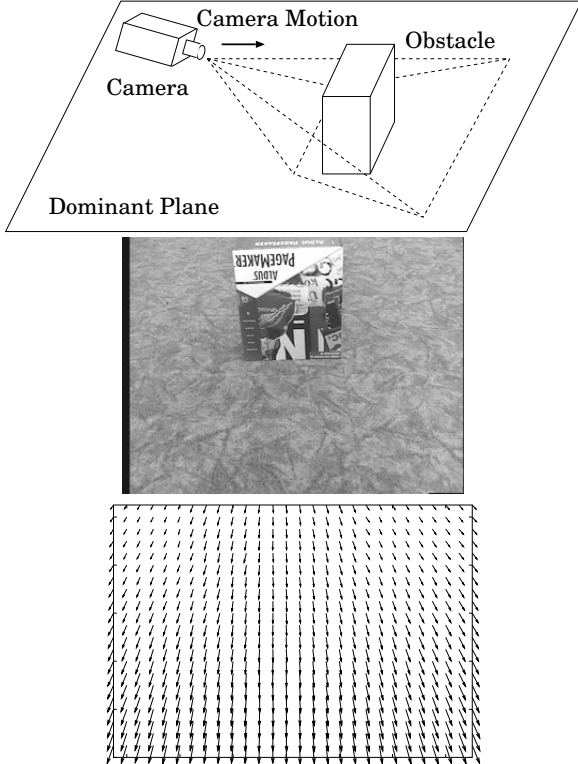


Figure 5: Optical flow of the image sequence. Top: Example of camera displacement and the environment with obstacles. Bottom-left: An image of the dominant plane and obstacles  $I(x, y, t)$ . Bottom-right: Computed optical flow  $\mathbf{u}(t)$ . In a top-middle area, where exists the obstacle, the lengths of optical flow vectors are longer than the flow vectors in the other area.

be the output signals of ICA,  $\mathbf{v}_1$  and  $\mathbf{v}_2$  are ambiguity of the order of the each components. We solve this problem using the difference between the variance of the length of  $\mathbf{v}_1$  and  $\mathbf{v}_2$ .

Setting  $l_1$  and  $l_2$  to be the length of  $\mathbf{v}_1$  and  $\mathbf{v}_2$ ,

$$l_j = \sqrt{\mathbf{v}_{xj}^2 + \mathbf{v}_{yj}^2}, \quad (j = 1, 2) \quad (5)$$

where  $\mathbf{v}_{xj}$  and  $\mathbf{v}_{yj}$  are arrays of  $x$  and  $y$  axis components of output  $\mathbf{v}_j$ , respectively, the variance  $\sigma_j^2$  are

$$\sigma_j^2 = \frac{1}{xy} \sum_{i \in xy} (l_j(i) - \bar{l}_j)^2, \quad \bar{l}_j = \frac{1}{xy} \sum_{i \in xy} l_j(i), \quad (6)$$

where  $l_j(i)$  is the  $i$ th data of the array  $l_j$ . Since the motions of the dominant plane and obstacles in the image is different, the output which expresses the obstacle-motion has larger variance than the output which expresses the dominant plane motion. Therefore, if  $\sigma_1^2 > \sigma_2^2$ , we detect dominant plane using output signal  $\mathbf{l}$  as  $\mathbf{l} = \mathbf{l}_1$ , else we use output signal  $\mathbf{l} = \mathbf{l}_2$ .

Since the dominant plane occupies the largest domain in the image, we compute the distance between  $\mathbf{l}$  and the median of  $\mathbf{l}$ . Setting  $m$  to be the median value of the elements in the vector  $\mathbf{l}$ , the distance  $\mathbf{d} = (d(1), d(2), \dots, d(xy))^T$  is

$$d(i) = |l(i) - m|. \quad (7)$$

We detect the area on which  $d(i) \approx 0$ , as the dominant plane.

### 3.3 Procedure for dominant plane detection

Our algorithm is summarized as follows. Learning phase is,

1. Robot moves on the dominant plane in the small distance.
2. Robot captures a image  $\hat{I}(u, v, t)$  of dominant plane.
3. Compute the optical flow  $\hat{\mathbf{u}}(t)$  between the images  $\hat{I}(u, v, t)$  and  $\hat{I}(u, v, t - 1)$ .
4. If time  $t > n$ , compute the supervisor signal  $\hat{\mathbf{u}}$  using Eq.(4). Else go to step 1.

Next, dominant plane recognition phase is,

1. Robot moves in the environment with obstacles in the small distance.
2. Robot captures a image  $I(u, v, t)$ .
3. Compute the optical flow  $\mathbf{u}(t)$  between the images  $I(u, v, t)$  and  $I(u, v, t - 1)$ .
4. Input the optical flow  $\mathbf{u}(t)$  and the supervisor signal  $\hat{\mathbf{u}}$  to ICA, and output the signal  $\mathbf{v}_1$  and  $\mathbf{v}_2$ .
5. Detect the dominant plane using the algorithm Section 3.2.

Figure 6 shows the procedure for dominant plane detection using optical flow and ICA.

## 4 Experiment

We show experiment for the dominant plane detection using the procedure in Section 3.

First, the robot equipped with a single camera moves forward with uniform velocity on the dominant plane and capture the image sequence without obstacles until  $n = 20$ . For the computation of optical flow, we use the Lucas-Kanade method with pyramids [15]. Using Eq.(4), we compute the supervisor signal  $\hat{\mathbf{u}}$ . Figure 7 shows the captured image and the computed supervisor signal  $\hat{\mathbf{u}}$ .

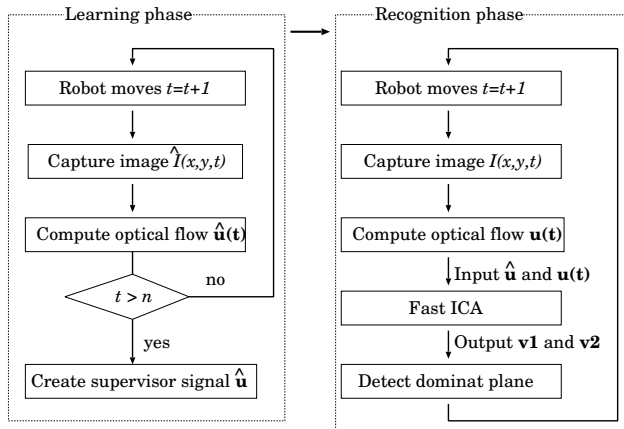


Figure 6: Procedure for dominant plane detection using optical flow and ICA.

Next, the mobile robot moves on the dominant plane toward the obstacle, as shown in Fig.8. The captured image sequence and computed optical flow  $\mathbf{u}(t)$  is shown in the first and second rows in Fig.9, respectively. The optical flow  $\mathbf{u}(t)$  and supervisor signal  $\hat{\mathbf{u}}$  are used as an input signal for fast ICA. We use the *Fast ICA package for MATLAB* [16] for the computation of ICA. The result of ICA is shown in the third row in Fig.9.

## 5 Conclusion

We developed an algorithm for the dominant plane detection from a sequence of images observed through a moving uncalibrated camera. The use of the ICA for the optical flow enables the robot to detect a feasible region in which robot can move without requiring camera calibration. These experimental results support the application of our method to the navigation and path planning of a mobile robot with a vision system. For each image in a sequence, the dominant plane corresponds to an independent component. This relation provides us a statistical definition of the dominant plane.

The future work is autonomous robot navigation using our algorithm of dominant plane detection. If we project the dominant plane of the image plane onto the ground plane using a camera configuration, the robot detects the movable region in front of the robot in an environment. Since we can obtain the sequence of the dominant plane from optical flow, the robot can move the dominant plane in a space without collision to obstacles.

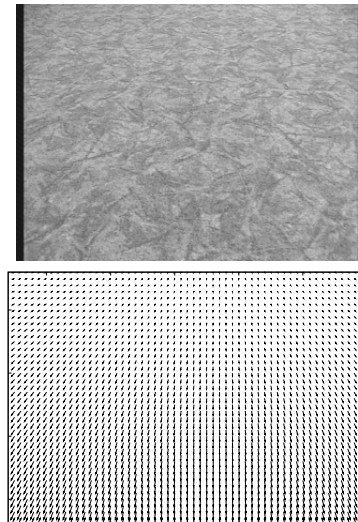


Figure 7: Left: Image sequence  $\hat{I}(x, y, t)$  of the dominant plane. Right: Optical flow  $\hat{\mathbf{u}}$  used for the supervisor signal.



Figure 8: Experimental environment. The obstacle exists in front of the mobile robot. The mobile robot moves toward the obstacle.

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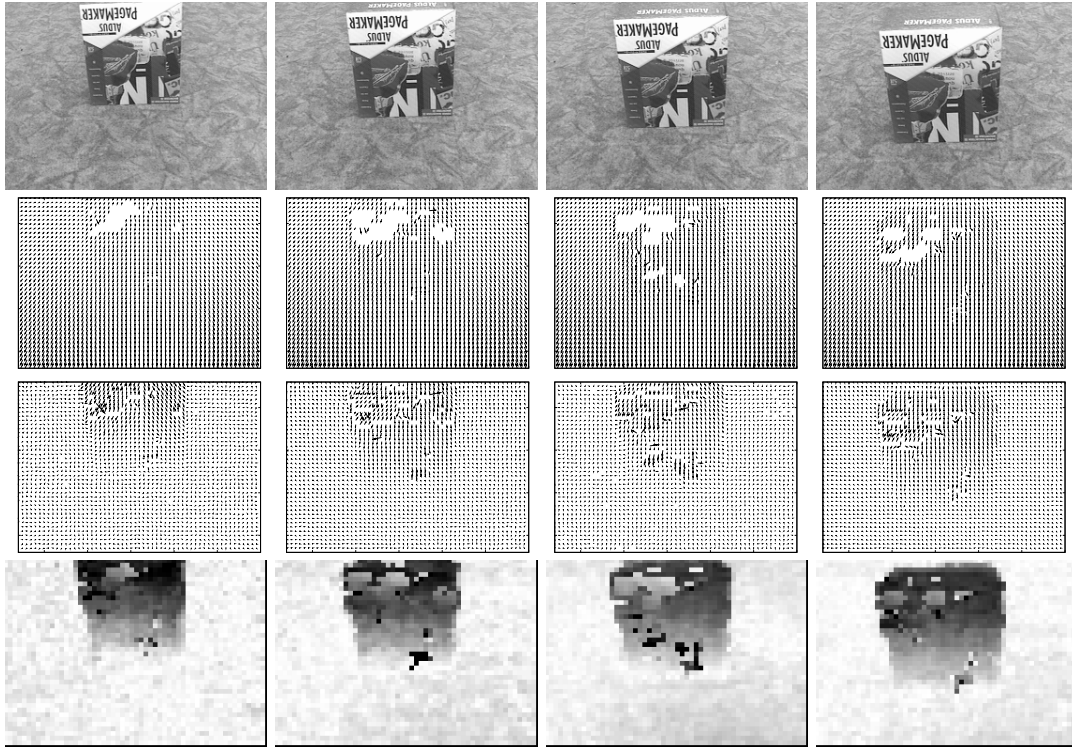


Figure 9: The first, second, third, and fourth rows show observed image  $I(x, y, t)$ , computed optical flow  $\mathbf{u}(t)$ , output signal  $\mathbf{v}(t)$ , and image of the dominant plane  $D(x, y, t)$ , respectively. In the image of the dominant plane, the white areas are the dominant planes and the black areas are the obstacle areas. Starting from the left column,  $t = 340, 359, 374, \text{ and } 393$ .

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