

# A Dynamic Extension for the Specifications of Distributed Systems

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In this paper, we describe an approach for extending distributed system specifications. These specifications are structured as a parallel composition of subsystem specifications. The approach consists of building a new specification *Snew* by adding a new behavior described by a specification *Sadded* to a specification *Sold* with preservation of the properties of *Sold* and *Sadded* as well as the structure of *Sold*. *Snew* has all the properties of *Sold* and *Sadded*, if *Snew* can perform whatever *Sold* (and *Sadded*) can perform, and it does not block where *Sold* (or *Sadded*) does not block. We apply our approach for extending the functionality of a basic Automatic Teller Machine.

## 分散システム仕様のための動的拡張

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本論では、分散システムの仕様を拡張するためのアプローチについて述べる。これらの仕様は、サブシステム仕様の並列的な構成として構造化される。このアプローチでは、仕様*Sold*に対して、仕様*Sadded*によって記述される新たな振る舞いを追加することにより、新たな仕様*Snew*を構築する。仕様*Snew*では、*Sold*と*Sadded*のプロパティは、*Sold*の構造と同様に維持される。もし、*Sold*（かつ*Sadded*）が実行可能なもの全てを*Snew*が実行できるものとし、*Sold*（または*Sadded*）がブロック化しない場所で、*Snew*がブロック化しないとすれば、*Snew*は*Sold*と*Sadded*のプロパティの全てを持つことになる。我々は、上記のアプローチを、基本的なAutomatic Teller Machineの機能性の拡張に適用する。

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## 1 Introduction

The design of a distributed system goes through many phases. The initial phase allows the capturing of functional requirements in a specification with a high level of abstraction. This specification describes the functionalities of the system, but not how to realize them. In the next phases, it is refined into specifications with a lower level of abstraction where some design decisions are taken and a structure is chosen. The specification obtained after each step should remain correct with respect to the initial specification. The service specification and protocol specification for a given OSI layer are typical examples of two different levels of abstraction [Viss 85].

The step-wise refinement approach allows the methodical production of a specification with a low level of abstraction from a specification with a high level of abstraction. The distributed system specification task, however, still remain very complex, particularly when many functions have to be handled simultaneously. A complementary approach to deal with this complexity is the divide-and-conquer methodology. It consists of building specifications for the different features of the required system independently and of combining them to obtain the desired specification. From another point of view, this approach allows the enrichment of a system specification by adding new behaviors required by the user, such as adding a new functions to a given telecommunication system.

The combination should preserve the semantics properties of each single specification. For instance, the addition of a new function to a telephone system specification should not disturb the semantics properties of the telephone system specification and the semantics properties of the new function. In the context of distributed systems, preserving semantic properties may, for instance, mean that the combined specification exhibits at least the behaviors of the original ones without introducing additional failures for these behaviors. This is captured by the formal relation between specifications, called extension, introduced in [Brin 86]. Informally, a specification  $S_2$  extends a specification  $S_1$ , if and only if,  $S_2$  allows any sequence of actions that  $S_1$  allows, and  $S_2$  can only refuse what  $S_1$  can refuse, after a given sequence of actions allowed by  $S_1$ .

In this paper, we propose an incremental specification approach, which consists of merging two given specifications  $S_{old}$  and  $S_{added}$  into a specification  $S_{new}$ , such that  $S_{new}$  extends  $S_{old}$  and  $S_{new}$  extends  $S_{added}$ . Moreover, in the case of minimal cyclic traces of  $S_{old}$  or  $S_{added}$ ,  $S_{new}$  transforms into  $S_{new}$ , and may exhibit, in a recursive manner, behaviors of  $S_{old}$  and  $S_{added}$ . We consider distributed system specifications, which may consist of a parallel combination of subsystem specifications. The incremental specification approach preserves such structure. Therefore, the designer does not

have to redesign it. The approach for merging structured specifications described in this paper, is based on our approach for merging monolithic specifications described in [Hami 95].

The remainder of the paper is structured as follows. Section 2 introduces the labelled transition systems model [Kell 76] and some definitions used in this paper. In Section 3, we summarize the principle and properties of the approach for merging monolithic specifications. In Section 4, our approach for merging structured specifications is described. In Section 5, we apply our approach for extending the functionality of a basic Automatic Teller Machine. In Section 6 our approach is compared to related ones. In Section 7, we conclude.

## 2 Labelled Transition Systems

We view the specification of a distributed system and its subsystems as processes, which are expressed by labelled transition systems (LTS for short). In this section, we introduce the LTS model [Kell 76] and some definitions, such as the definition of a cyclic trace, a minimal cyclic trace, and the definition of the extension relation [Brin 86].

### 2.1 Definitions

An LTS is a graph in which nodes represent states, and edges, also called transitions, represent state changes, labelled by actions occurring during the change of state. These actions may be observable or not.

**Definition 2.1** [Kell 76]

An LTS TS is a quadruple  $\langle S, L, T, So \rangle$ , where

- $S$  is a (countable) nonempty set of states,
- $L$  is a (countable) set of observable actions.
- $T: S \times L \cup \{\tau\} \rightarrow S$  is a transition relation, where a transition from a state  $S_i$  to state  $S_j$  by an action  $\mu$  ( $\mu \in L \cup \{\tau\}$ ) is denoted by  $S_i - \mu \rightarrow S_j$ .
- $\tau$  represents the internal, nonobservable action.
- $So$  is the initial state of TS.

A finite LTS (FLTS for short) is an LTS in which  $S$  and  $L$  are finite. In the remainder of this paper, we may refer to an LTS by its initial state and vice versa. We may also write  $act(TS)$ , instead of  $L$ , to denote the set of observable actions of TS. Some notations for LTSs are summarized in Table 1.

A trace, of a given state  $S_i$  in the LTS TS, is a sequence of actions that TS can perform starting from state  $S_i$ . A cyclic trace in TS is a trace of the initial state  $So$  that reaches only the initial state  $So$  and the states that can be reached by the empty trace from  $So$ . In other words, a cyclic trace always brings back TS to its initial state. TS may then move to an other state by the nonobservable action  $\tau$ . A minimal cyclic trace is a cyclic trace that is not prefixed by a nonempty cyclic trace.

**Definition 2.2 (Cyclic Trace)**

Given an LTS TS =  $\langle S, L, T, So \rangle$ , a trace  $s$  is cyclic, iff  $(So \text{ after } \sigma) = \{S_i \in S \text{ such } So \xrightarrow{\sigma} S_i\}$ .

### Definition 2.3 (Minimal Cyclic Trace)

Given an LTS  $TS = \langle S, L, T, So \rangle$ ,  $\sigma$  is a minimal cyclic trace, iff  $\sigma$  is a cyclic trace, and  $\exists \sigma' (\neq \epsilon)$  and  $\sigma'' (\neq \epsilon)$  such that  $\sigma = \sigma' \cdot \sigma''$  and  $\sigma'$  is cyclic trace in  $TS$ .

$P \rightarrow \mu_1 \dots \mu_n \rightarrow Q$ :  $\exists P_i (0 \leq i \leq n)$  such that

$$P = P_0 \rightarrow \mu_1 \rightarrow P_1 \dots P_{n-1} \rightarrow \mu_n \rightarrow P_n = Q$$

$P \rightarrow \mu_1 \dots \mu_n \rightarrow$ :  $\exists Q$  such that  $P \rightarrow \mu_1 \dots \mu_n \rightarrow Q$

$P \equiv \epsilon \Rightarrow Q$ :  $P \equiv Q$  or  $\exists n \geq 1 P \rightarrow \tau^n \rightarrow Q$

$P \xrightarrow{a} Q$ :  $\exists P_1, P_2$  such that  $P \xrightarrow{\epsilon} P_1 \xrightarrow{a} P_2 \xrightarrow{\epsilon} Q$

$P \xrightarrow{a_1 \dots a_n} Q$ :  $\exists P_i (0 \leq i \leq n)$  such that

$$P = P_0 \xrightarrow{a_1} P_1 \xrightarrow{a_2} \dots \xrightarrow{a_n} P_n = Q$$

$P \xrightarrow{\sigma} Q$ :  $\exists Q$  such that  $P \xrightarrow{\sigma} Q$

$P \not\xrightarrow{\sigma} Q$ : not  $(P \xrightarrow{\sigma} Q)$

$Tr(P)$ :  $\{\sigma \in L^* \mid P \xrightarrow{\sigma}\}$

$out(P, s)$ :  $\{a \in L \mid \sigma a \in Tr(P)\}$

$initials(P)$ :  $out(P, \epsilon)$

$P$  after  $\sigma$ :  $\{Q \mid P \xrightarrow{\sigma} Q\}$

$Acc(P, \sigma)$ :  $\{X \mid \exists Q \in (P \text{ after } \sigma), \text{ such that}$

$initials(Q) \subseteq X \subseteq out(P, \sigma)\}$

where  $\mu, \mu_i \cup L (\tau)$ ;  $a, ai \in L$ ;  $P, Q, P_i, Q_i$

represent states;  $\epsilon$  represents the empty trace;

$\sigma = a_1 a_2 \dots a_n$ , where "." denotes the concatenation of actions or sequence of actions (traces).

Table 1. LTS notations

## 2.2 Operations on Labelled Transition Systems

The specification of a distributed system may be considered as a composition of its subsystem specifications. Among the possible compositions, the parallel composition operator and the action hiding operator are of special interest in this paper. The parallel composition operator ( $B1 \parallel \{a_1, \dots, a_n\} B2$ ) allows one to express the parallel execution of the behaviors  $B1$  and  $B2$ .  $B1$  and  $B2$  synchronize on actions in  $\{a_1, \dots, a_n\}$  and interleave with respect to other actions. The hiding operator allows the hiding of actions, which then will be considered internal actions. We write  $B \backslash A$  to denote the hiding of the actions in  $A$  in the behavior  $B$ . The inference rules for these operators are as follows (adapted from [ISO 8807]).

Parallel composition:  $B1 \parallel \{a_1, \dots, a_n\} B2$

If  $B1 \xrightarrow{a} B1'$  and  $a \in \{a_1, \dots, a_n\}$ , then  $B1 \parallel \{a_1, \dots, a_n\} B2 \xrightarrow{a} B1' \parallel \{a_1, \dots, a_n\} B2$ ,

If  $B2 \xrightarrow{a} B2'$  and  $a \in \{a_1, \dots, a_n\}$ , then  $B1 \parallel \{a_1, \dots, a_n\} B2 \xrightarrow{a} B1 \parallel \{a_1, \dots, a_n\} B2'$ ,

If  $B2 \xrightarrow{a} B2'$  and  $B1 \xrightarrow{a} B1'$  and  $a \in \{a_1, \dots, a_n\}$ , then  $B1 \parallel \{a_1, \dots, a_n\} B2 \xrightarrow{a} B1' \parallel \{a_1, \dots, a_n\} B2'$ .

Hiding operator:  $B \backslash \{a_1, \dots, a_m\}$

If  $B \xrightarrow{a} B'$  and  $a \in \{a_1, \dots, a_m\}$ , then  $B \backslash \{a_1, \dots, a_m\} \xrightarrow{a} B' \backslash \{a_1, \dots, a_m\}$ ,

If  $B \xrightarrow{a} B'$  and  $a \in \{a_1, \dots, a_m\}$ , then  $B \backslash \{a_1, \dots, a_m\} \xrightarrow{\tau} B' \backslash \{a_1, \dots, a_m\}$ .

## 2.3 The extension relation

Intuitively, different LTSs may describe the same

observable behavior. Therefore different equivalence relations have been defined based on the notion of observable behavior. They range from the relatively coarse trace equivalence to the much finer strong bisimulation equivalence [DeNi 87]. However, for our considerations, one does not need equivalence relations, but rather ordering relationships. Among them, we note the reduction and extension relation as defined in [Brin 86]. These relations may serve different purposes during the specification life cycle. The extension relation is most appropriate for our purpose of compatible enrichment of specifications. Informally,  $S2$  extends  $S1$ , if and only if,  $S2$  allows any sequence of actions that  $S1$  allows, and  $S2$  can only refuse what  $S1$  can refuse, after a given sequence of actions allowed by  $S1$ .

### Definition 2.4 [Brin 86]

$S2$  extends  $S1$ , written  $S2 \text{ ext } S1$ , iff

(a)  $Tr(S1) \subseteq Tr(S2)$ , and

(b)  $\forall \sigma \in Tr(S1), \forall A \subseteq L$ ,

if  $S2 \xrightarrow{\sigma} S2'$  and  $S2' \not\xrightarrow{a}$ ,  $\forall a \in A$ ,

then  $S1' \xrightarrow{\sigma} S1'$  and  $S1' \not\xrightarrow{a}$ ,  $\forall a \in A$ .

## 3 Merging monolithic specifications

In this section, we consider monolithic specifications [Viss 88]. A monolithic specification has no internal structure and is defined directly in terms of some allowed ordering of actions. A monolithic specification is represented by a single LTS.

Given two LTSs,  $S1$  and  $S2$ , we want to construct systematically an LTS  $S3$ , such that  $S3$  extends  $S1$ , and  $S3$  extends  $S2$ . Moreover, in the case of minimal cyclic traces of  $S1$  or  $S2$ ,  $S3$  transforms into  $S3$ , and may exhibit, in a recursive manner, behaviors of  $S1$  and  $S2$ . Note that the usual choice operators defined for LOTOS [ISO 8807] and CCS [Miln 89] for instance, do not allow such combination of specifications as shown in Figure 1.

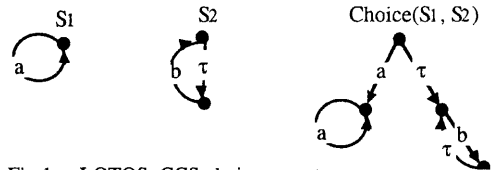


Fig 1. LOTOS, CCS choice operator

We assume that the LTSs are finite. Our FLTSs merging algorithm, called Merge, uses an intermediate representation, the Acceptance Graphs (AGs for short).

### Definition 3.1

An AG  $G$  is 5-tuple  $\langle Sg, L, Ac, Tg, Sgo \rangle$ , where

-  $Sg$  is a (countable) nonempty set of states.

-  $L$  is a (countable) nonempty set of events.

-  $Ac: Sg \rightarrow P(P(L))$  is a mapping from  $Sg$  to sets of subsets of  $L$ .

$Ac(Sgi)$  is called the acceptance set of  $Sgi$ .

-  $Tg: Sg \times L \rightarrow Sg$  is a transition function, where a

transition from

state  $S_{gi}$  to state  $S_{gj}$  by an action  $a$  ( $a \in L$ ) is denoted by  $S_{gi} \xrightarrow{a} S_{gj}$ .

-  $S_{go}$  is the initial state of  $G$ .

The mappings  $Ac$  and  $Tg$  should satisfy the consistency constraints defined for Acceptance Trees in [Henn 85]. A finite AG (FAG for short) is an AG in which  $Sg$  and  $L$  are finite. The LTS notations in Table 1 remain valid for the AGs. A cyclic trace for an AG  $G = \langle Sg, L, Ac, Tg, Sgo \rangle$ , is a trace of the initial state  $Sgo$  that reaches the initial state  $Sgo$ . As for an LTS, a minimal cyclic trace for an AG is a cyclic trace that is not prefixed by a nonempty cyclic trace. In the following, we define a relation, denoted  $AGR$ , between AGs and LTSs.

### Definition 3.2

Given an AG  $G = \langle Sg, L, Ac, Tg, Sgo \rangle$  and an LTS  $S = \langle St, L, T, So \rangle$ , we say that  $G$  is a corresponding AG of  $S$ , written  $\langle G, S \rangle \in AGR$ , iff

-  $Tr(G) = Tr(S)$ ,

-  $\forall \sigma \in Tr(S)$ , if  $Sgo = \sigma \Rightarrow S_{gi}$ , then  $Ac(S_{gi}) = Acc(So, \sigma)$ ,

- Any minimal cyclic trace in  $S$  is a minimal cyclic trace in  $G$ , and

- Any minimal cyclic trace in  $G$  is a minimal cyclic trace in  $S$ .

Given two FLTSs  $S1 = \langle St1, L1, T1, S1o \rangle$  and  $S2 = \langle St2, L2, T2, S2o \rangle$ , the algorithm Merge consists, first, of transforming the FLTSs  $S1$  and  $S2$  into FAGs  $G1 = \langle Sg1, L1, Ac1, Tg1, Sg1o \rangle$  and  $G2 = \langle Sg2, L2, Ac2, Tg2, Sg2o \rangle$ , respectively, such that  $Sg1 \cap Sg2 = \emptyset$  and  $\langle G1, S1 \rangle \in AGR$  and  $\langle G2, S2 \rangle \in AGR$ . The FAGs  $G1$  and  $G2$  are then merged by an FAG merging algorithm into the FAG  $G3 = \langle Sg3, L1 \cup L2, Ac3, Tg3, \langle Sg1o, Sg2o \rangle \rangle$ , which is transformed back to an FLTS  $S3$  such that  $\langle G3, S3 \rangle \in AGR$ .

The algorithm for the transformation of an FLTS to an FAG is similar to the "subset construction" algorithm defined in [Hopce 79]. The transformation of an FAG to an FLTS, in the last step, is the converse transformation. This transformation eliminates the information redundancy concerning the failure possibilities. The FLTS generated by this transformation is the canonical representative of a class of testing equivalent LTSs with the same set of minimal cyclic traces. In the following, we describe, informally, the FAG merging algorithm.

A state  $S_{gi}$  in  $Sg3$  may be either a tuple  $\langle Sg1i, Sg2j \rangle$  consisting of state  $Sg1i$  from  $Sg1$  and  $Sg2j$  from  $Sg2$  (as for the initial state  $\langle Sg1o, Sg2o \rangle$ ), or a simple state  $Sg1i$  from  $Sg1$ , or a simple state  $Sg2j$  from  $Sg2$ . These states and the transitions which reach them are added by the FAG merging algorithm step by step into  $Sg3$  and  $Tg3$ , respectively, except for the two initial states  $Sg1o$  and  $Sg2o$ , each of these is replaced by the initial state  $\langle Sg1o, Sg2o \rangle$  of  $G3$ .

Initially,  $Sg3$  contains only the initial state  $\langle Sg1o, Sg2o \rangle$ . The definition of the transitions from state  $\langle Sg1i, Sg2j \rangle$  in  $Sg3$  depends on the transitions from  $Sg1i$  in  $Sg1$  and from  $Sg2j$  in  $Sg2$ . For instance, for a given state  $\langle Sg1i, Sg2j \rangle$ , if there is a transition  $Sg1i \xrightarrow{a} Sg1k$  in  $Tg1$  and a transition  $Sg2j \xrightarrow{a} Sg2m$  in  $Tg2$ , then the state  $\langle Sg1k, Sg2m \rangle$  is added into  $Sg3$  and the two transitions are combined into one transition  $\langle Sg1i, Sg2j \rangle \xrightarrow{a} \langle Sg1k, Sg2m \rangle$  in  $Tg3$ . This is the situation when  $G1$  and  $G2$  have a common trace from their initial state to  $Sg1k$  and  $Sg2m$ , respectively.

Another case of this construction, if for a given state  $\langle Sg1i, Sg2j \rangle$ , there exists a transition  $Sg1i \xrightarrow{a} Sg1k$  in  $Tg1$ , with  $Sg1k \neq Sg1o$ , but there is no transition labelled by  $a$  from  $Sg2j$  in  $Tg2$ , then the state  $Sg1k$  is added into  $Sg3$  and the transition  $Sg1i \xrightarrow{a} Sg1k$  in  $Tg1$  yields the transition  $\langle Sg1i, Sg2j \rangle \xrightarrow{a} Sg1k$  in  $Tg3$ . Reciprocally, if there exists a transition  $Sg2j \xrightarrow{a} Sg2m$  in  $Tg2$ , with  $Sg2m \neq Sg2o$ , but there is no transition labelled by  $a$  from  $Sg1i$  in  $Tg1$ , then the state  $Sg2m$  is added into  $Sg3$  and the transition  $Sg2j \xrightarrow{a} Sg2m$  in  $Tg2$  yields the transition  $\langle Sg1i, Sg2j \rangle \xrightarrow{a} Sg2m$  in  $Tg3$ . In the case where  $Sg1k = Sg1o$  (respectively  $Sg2m = Sg2o$ ), instead of the transition  $\langle Sg1i, Sg2j \rangle \xrightarrow{a} Sg1o$  (respectively  $\langle Sg1i, Sg2j \rangle \xrightarrow{a} Sg2o$ ), the transition  $\langle Sg1i, Sg2j \rangle \xrightarrow{a} \langle Sg1o, Sg2o \rangle$  is added into  $Tg3$ .

The transitions from a simple state in  $Sg3$ , like state  $Sg1k$  or  $Sg2m$  above, for instance, remain the same as defined in  $G1$  and  $G2$ , respectively. The states reached by these transitions are added into  $Sg3$ , except for the two initial states  $Sg1o$  and  $Sg2o$ , each of these is replaced by the initial state  $\langle Sg1o, Sg2o \rangle$  of  $G3$ .

The mapping  $Ac3$  is defined as follows: For every state  $S_{gi}$  in  $Sg3$ , we have:

- if  $S_{gi} = \langle Sg1i, Sg2j \rangle$ , then  $Ac3(S_{gi}) = \{X1 \cup X2 \mid X1 \in Ac1(Sg1i) \text{ and } X2 \in Ac2(Sg2j)\}$ ,

- if  $S_{gi} = Sg1i$ , with  $Sg1i \in Sg1$ , then  $Ac3(S_{gi}) = Ac1(Sg1i)$ ,

- if  $S_{gi} = Sg2j$ , with  $Sg2j \in Sg2$ , then  $Ac3(S_{gi}) = Ac2(Sg2j)$ .

Given the FLTSs  $S1, S2$ , the following propositions have been proved in [Hami 95] concerning the FLTS  $S3$  constructed by the algorithm Merge:

### Proposition 1

$S3$  extends  $S1$  and  $S3$  extends  $S2$ .

Merge satisfies our first requirement as stated above in Proposition 1. However, the second requirement about the recursive exhibition of behaviors of  $S1$  and behaviors of  $S2$ , in the case of minimal cyclic traces of  $S1$  or  $S2$ , is not always satisfied. This requirement is satisfied, if and only if all the minimal cyclic traces in  $S1$  and all the minimal cyclic traces in  $S2$  remain minimal cyclic traces in  $S3$ . Unfortunately, there are some situations where a minimal cyclic trace in  $S1$  (respectively  $S2$ ) does not remain a minimal cyclic trace in  $S3$ . This is the case,

when a given trace  $s$  is a minimal cyclic trace in  $S1$  (respectively  $S2$ ), but  $s$  is a noncyclic trace in  $S2$  (respectively  $S1$ ). After executing such a minimal cyclic trace,  $S3$  reaches a state, which is different from its initial state. Therefore, after performing such a minimal cyclic trace,  $S3$  does not transform into  $S3$ , and  $S3$  may not exhibit again the behaviors of  $S1$  and the behaviors of  $S2$ . Figure 2 illustrates such kind of situations. After performing  $a$ , which is a minimal cyclic trace in  $S1$ ,  $S3$  does not transform into  $S3$ , because the trace  $a$  belongs to  $S2$  and it is not a cyclic trace in  $S2$ .  $S3$  does not offer the behavior  $a.b$  of  $S2$ , after the minimal cyclic trace  $a$ . Note that, the minimal cyclic trace  $a.b$  in  $S2$  remains a minimal cyclic trace in  $S3$ . In Proposition 2, we determined a necessary and sufficient condition, for which a minimal cyclic trace in  $S1$  (respectively  $S2$ ) remains a minimal cyclic trace in  $S3$ .

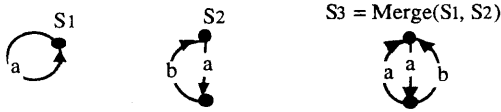


Fig 2. Counterexample for the minimal cyclic traces

#### Proposition 2

- A minimal cyclic trace  $s$  in  $S1$ , is a minimal cyclic in  $S3$ , iff ( $s \in \text{Tr}(S2)$  or  $s$  is cyclic in  $S2$ ).
- Reciprocally, for a minimal cyclic trace  $s$  in  $S2$ .

Any trace of  $S3$  is either a trace of  $S1$ , or a trace of  $S2$ , or results from the concatenation of traces of  $S1$  and  $S2$ . The following proposition shows how a trace  $s.a$  of  $S3$  may be decomposed into its subtraces in  $S1$  and  $S2$ , when  $s$  is a trace of  $S1$  (respectively  $S2$ ).

#### Proposition 3

$\forall a \in L1 \cup L2$ , if  $s \in \text{Tr}(S1)$  and  $s.a \in \text{Tr}(S3)$ , then  $\sigma.a \in \text{Tr}(S1)$ , or  $\sigma.a \in \text{Tr}(S2)$ , or  $(\exists \sigma1, \sigma2$  such that  $\sigma = \sigma1.\sigma2$ ,  $S1=\sigma1 \Rightarrow S1$ ,  $S1=\sigma2 \Rightarrow S1' \neq a \Rightarrow$ ,  $S2=s2 \Rightarrow S2'=a \Rightarrow)$ .  
Reciprocally, for  $s \in \text{Tr}(S2)$  and  $s.a \in \text{Tr}(S3)$ .

#### 4 Merging Structured Specifications

In this section, we consider distributed system specifications, which consist of a parallel composition of subsystem specifications as shown in Figure 3. Such specifications have the following form:  $S = (S1 \parallel_A S2) \setminus B$ , where  $A$  and  $B$  represent sets of actions. The subsystem specifications  $S1$  and  $S2$  may also have the same form as  $S$  and so on, until a level where the specifications have no structure and are defined directly in terms of some allowed ordering of actions as monolithic specifications. These specifications are called basic components, they may be nondeterministic, but are assumed to be finite. For instance, these specifications are represented by the streaked boxes in Figure 3.

Given a distributed system specification  $Sold$ , which consists of a parallel composition of subsystem specifications and so on until the basic components, and a

specification  $Sadded$ , we want to construct a specification  $Snew$ , such that  $Snew$  extends  $Sold$ , and  $Snew$  extends  $Sadded$ .

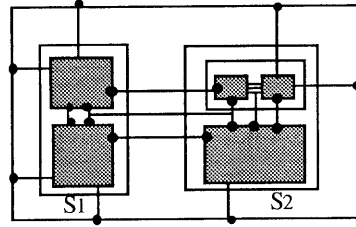


Fig 3. Structure of a Distributed System Specification

The specification  $Snew$  should preserve the internal structure of  $Sold$ . As for the merging of monolithic specifications, in the case of minimal cyclic traces of  $Sold$  or  $Sadded$ ,  $Snew$  transforms into  $Snew$ , and may exhibit, in a recursive manner, behaviors of  $Sold$  and  $Sadded$ .

#### 4.1 Identical Structure for $Sold$ and $Sadded$

We assume that the specifications  $Sold$  and  $Sadded$  are both structured according to the form  $(S1 \parallel_A S2) \setminus B$  described above, and  $S1$  and  $S2$  are either basic components or again structured by parallel composition. Moreover, we assume that  $Sold$  and  $Sadded$  have an identical structure. In other words, the form of the expression  $Sold$  is identical to the form of the expression  $Sadded$ . To every subsystem specification in  $Sold$  corresponds a subsystem specification in  $Sadded$  and vice versa. To every basic component  $Ciold$  in  $Sold$ , corresponds a basic component  $Ciadded$  in  $Sadded$  and vice versa.

The following algorithm for merging structured specifications, called  $\text{Structured\_Merge}$ , is recursive over the structure of  $Sold$  and  $Sadded$ . It is based on the algorithm  $\text{Merge}$ , for merging monolithic specifications, described in Section 3.

#### Merging Algorithm for Structured Specifications

$\text{Structured\_Merge}(S1, S2) =$   
if  $S1 = (S11 \parallel_A S12) \setminus B$ ,  $S2 = (S21 \parallel_C S22) \setminus D$ ,  
then  $(\text{Structured\_Merge}(S11, S21) \parallel_{(A \cup C)} \text{Structured\_Merge}(S12, S22)) \setminus (B \cup D)$   
else  $\text{Merge}(S1, S2)$  (\*  $S1$  and  $S2$  are basic components \*)

$Snew$ , obtained by  $\text{Structured\_Merge}(Sold, Sadded)$ , has a structure identical to the structure of  $Sold$  and  $Sadded$ . As basic component, instead of  $Ciold$  or  $Ciadded$ , it has  $Cinew$  which results from the merging of  $Ciold$  and  $Ciadded$  by the algorithm  $\text{Merge}$ .

Unfortunately,  $Snew$  does not always extend  $Sold$  and  $Sadded$ . The extension of the basic components of  $Sold$  and  $Sadded$  is not sufficient to insure the extension of  $Sold$  and  $Sadded$ , respectively. Consider the counterexample in Figure 4, where  $Sold = (C1old \parallel_{\{g1\}} C2old) \setminus \{g1\}$ ,  $Sadded$

$= (C1_{added} \setminus \{g2\} \setminus C2_{added}) \setminus \{g2\}$ . The structure of the specification  $S_{new}$  is identical to the structure of  $S_{old}$  and  $S_{added}$ , but  $S_{new}$  does neither extend  $S_{old}$  nor  $S_{added}$ . Indeed,  $S_{old}$  never refuses the action  $b$  after trace  $a$ , whereas  $S_{new}$  may refuse action  $b$  after trace  $a$ . The same observation holds for action  $c$  after trace  $a$ . The trace  $a$  is common for  $C1_{old}$  and  $C1_{added}$  and it is followed by a hidden action  $g1$  in  $C1_{old}$  and  $g2$  in  $C1_{added}$ . The merging of  $C1_{old}$  and  $C1_{added}$  leads to a choice between the two hidden actions  $g1$  and  $g2$  after the trace  $a$ , in  $C1_{new}$ . The components  $C1_{new}$  and  $C2_{new}$  may, internally, choose to synchronize on action  $g1$  or  $g2$ , after a trace  $a$ , and offer only action  $b$  or only action  $c$ , respectively.

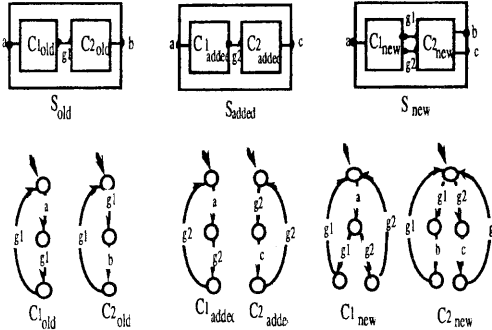


Fig 4. Counterexample

In Theorem 1, we have stated sufficient conditions for  $S_{old}$  and  $S_{added}$  such that  $S_{new}$  extends  $S_{old}$  and  $S_{new}$  extends  $S_{added}$ . We denote by  $HG_{old}$  the set of hidden action names in  $S_{old}$ , and by  $HG_{added}$  the set of hidden action names in  $S_{added}$ . The proof of Theorem 1 is given in the Appendix.

#### Theorem 1

Given  $S_{old}$  in the form of a hierarchical structure with the basic components  $C1_{old}, C2_{old}, \dots, Cn_{old}$ ,  $S_{added}$  with an identical structure and the basic components  $C1_{added}, C2_{added}, \dots, Cn_{added}$ , and  $S_{new} = \text{Structured\_Merge}(S_{old}, S_{added})$  as defined by the merging algorithm defined above,

we have that  $S_{new} \text{ ext } S_{old}$  and  $S_{new} \text{ ext } S_{added}$ , if the following conditions are satisfied:

- (a)  $\forall i, i = 1, \dots, n, \text{act}(C1_{old}) \cap (HG_{added} = \emptyset, \text{ and } \text{act}(C1_{added}) \cap (HG_{old} = \emptyset,$
- (b)  $\forall i, j, i \neq j, (\text{act}(C1_{old}) \cup \text{act}(C1_{added})) \cap ((\text{act}(Cj_{old}) \cup \text{act}(Cj_{added})) \cap ((\text{act}(S_{old}) \cup \text{act}(S_{added})) = \emptyset,$
- (c) For  $x = \text{old}, \text{added},$

$Ci_x$  and  $Cj_x$ , with  $i \neq j$ , such that for some  $g \in HG_x$ ,  $g \in \text{initials}(Ci_x)$  and  $g \in \text{initials}(Cj_x)$ ,

(d) For  $i = 1, \dots, n,$

1 -  $\forall \sigma \in \text{Tr}(C1_{old}), \text{ if } s.g \in \text{Tr}(C1_{added}) \text{ with } g \in HG_{added}, \text{ then } \sigma \text{ is cyclic in } C1_{old} \text{ and } C1_{added}, \text{ and reciprocally,}$

2 -  $\forall a \in (\text{act}(S_{old}) \setminus \text{initials}(C1_{old})), \text{ if } \sigma.a \in \text{Tr}(C1_{added}) \text{ for some } \sigma, \text{ then } \sigma \text{ is cyclic in } C1_{added}, \text{ and}$

reciprocally.

Condition (a) says that the names of hidden actions in  $S_{added}$  should not conflict with the names of observable or hidden actions in  $S_{old}$ . Reciprocally, the names of hidden actions in  $S_{old}$  should not conflict with the names of observable or hidden actions in  $S_{added}$ . Note that the names of the hidden actions in both specifications are not important. These actions may be renamed without any observable effect, in order to satisfy this condition.

Condition (b) says that there is no observable action of  $S_{old}$  and  $S_{added}$  shared by two (or more) basic components of  $S_{old}$  (respectively  $S_{added}$ ). A basic component  $C1_{old}$  in  $S_{old}$  may have common observable actions only with the corresponding basic component  $C1_{added}$  in  $S_{added}$ , and reciprocally. Consider the example in Figure 5, where  $C1_{old}$  and  $C2_{added}$  have the action  $a$  in common, but they are not merged together.  $C1_{new} = \text{Merge}(C1_{old}, C1_{added})$ ,  $C2_{new} = \text{Merge}(C2_{old}, C2_{added})$ ,  $C1_{new}$  extends  $C1_{old}$  and  $C1_{added}$ , and  $C2_{new}$  extends  $C2_{old}$  and  $C2_{added}$ . The constructed specification  $S_{new}$  may refuse action  $b$  or action  $c$ , after trace  $a$ , whereas  $S_{old}$  and  $S_{added}$  never refuses  $b$  or  $c$  after  $a$ , respectively.  $S_{new}$  does neither extend  $S_{old}$  nor  $S_{added}$ . In order to prevent such situations, for each observable action, we may assign a "place" and the components with common observable actions have to be merged together, as stated by Condition (b).

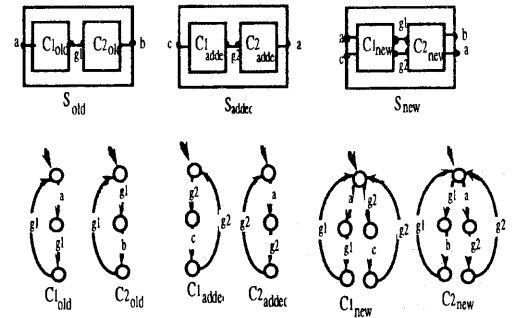
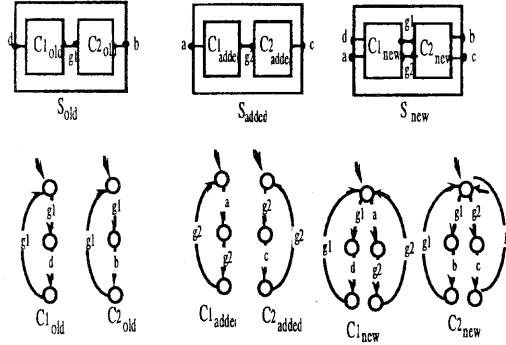


Fig 5. An illustration for Condition (b)

Condition (c) prevents  $S_{old}$  and  $S_{added}$  from performing a hidden action from  $HG_{old}$  or from  $HG_{added}$ , respectively, before interacting with the environment. Consider the example in Figure 6, in which  $C1_{new} = \text{Merge}(C1_{old}, C1_{added})$ ,  $C2_{new} = \text{Merge}(C2_{old}, C2_{added})$ ,  $C1_{new}$  extends  $C1_{old}$  and  $C1_{added}$ , and  $C2_{new}$  extends  $C2_{old}$  and  $C2_{added}$ . However  $S_{new}$  does not extend  $S_{added}$ . After an internal move by executing the hidden action  $g1$ , it refuses the action  $a$ , whereas  $S_{added}$  never refuses action  $a$  after an empty trace.

Condition (d-1) prevents from any new nondeterminism which may be introduced by the hidden actions in  $HG_{added}$  with respect to behavior in  $S_{old}$  and reciprocally, as shown in Figure 4. For a given pair of basic components  $C1_{old}$  and  $C1_{added}$ , a common trace, which is not cyclic in both components, should not be followed by hidden

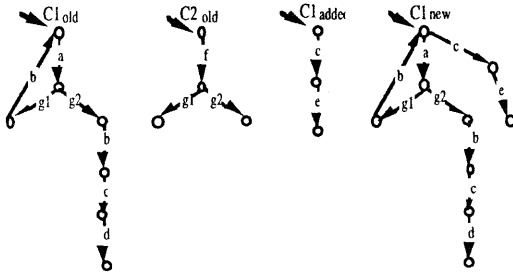
actions from HGold or HGadded.



**Figure 6.** An illustration for Condition (c)

Condition (d-2) is introduced in order to prevent situations similar to the one shown in Figure 7. Assume that  $Sold = (C1old \mid \{g1, g2\} C2old) \setminus \{g1, g2\}$  and  $Sadded = (C1added \mid \{g1, g2\} C2added) \setminus \{g1, g2\}$ . The merging algorithm for structured specifications leads to  $Snew = (C1new \mid \{g1, g2\} C2new) \setminus \{g1, g2\}$ , where  $C1new$  is shown in Figure 7 and  $C2new = C2old$ . We have  $C1new \text{ ext } C1old$  and  $C1new \text{ ext } C1added$  as well as  $C2new \text{ ext } C2old$  and  $C2new \text{ ext } C2added$ . However,  $Snew$  does not extend  $Sold$ . For instance, after the trace  $f.a.b.c$ ,  $Snew$  may refuse to perform action  $d$ , whereas  $Sold$  never refuses to perform action  $d$  after trace  $f.a.b.c$ . This is due to the fact that we have two traces  $s1 = a.g1.b$  and  $s2 = a.g2.b$  in  $C1old$ , such that  $s1 \neq s2$ ,  $s1 \setminus HGold = s2 \setminus HGold$ ,  $s1$  is cyclic,  $s2$  is not cyclic,  $s2.c$  is a trace in  $C1old$ , and  $c$  is a trace in  $C1added$ . It is possible to prevent such situations with a weaker condition than Condition (d-2) as explained in this example. However the verification of such conditions may be complex, whereas Condition (d-2) can be checked very easily.

Theorem 2 states that under certain conditions on the basic components of  $Sold$  and  $Sadded$ , a minimal cyclic trace  $\sigma$  in  $Sold$  (respectively  $Sadded$ ) remains cyclic in  $Snew$ . Therefore, after performing  $\sigma$ ,  $Snew$  reaches its initial state, and may exhibit again behaviors of  $Sold$  and behaviors of  $Sadded$ , without any new failure for these behaviors, since  $Snew$  extends  $Sold$  and  $Sadded$ .



**Fig 7.** Illustration for Condition (d-2).

**Theorem 2**

Given specifications  $Sold$ ,  $Sadded$ , and  $Snew$  as in Theorem 1, and assume that the conditions of Theorem 1 are satisfied, we have

- For any minimal cyclic trace  $\sigma$  in  $Sold$ , if for  $i = 1, \dots, n$ ,  $\sigma_i$  is a minimal cyclic trace in  $C1old$  and  $(\sigma_i \setminus Tr(C1added) \text{ or } \sigma_i \text{ is a cyclic trace in } C1added)$ , where  $\sigma_i$  represents the sequence of actions performed by  $C1old$ , when  $Sold$  performs the trace  $\sigma$ , then  $\sigma$  is a cyclic trace in  $Snew$ .
- Reciprocally, for any minimal cyclic trace  $\sigma$  in  $Sadded$ .

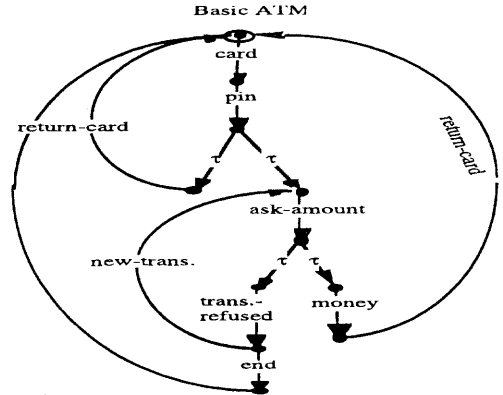
## 5 Application

In the following, we illustrate our approach by an application. We start with a basic Automatic Teller Machine (ATM) which provides only the withdrawal function as described by the LTS in Figure 8. After inserting his card a customer is prompted for the Personal Identification Number (PIN) which may be valid or invalid. In case of invalid PIN, the card is rejected and the customer can retry again. If the PIN is valid, the customer can ask for a certain amount. The transaction is refused if the amount is higher than the balance. The customer can try with another amount or end the process and get back his card. In the other case, the money is delivered and the card is rejected. This function is implemented by three components as shown in Figure 9. The composition of these components, using the LOTOS parallel and hiding operators, yields the LTS in Figure 8.

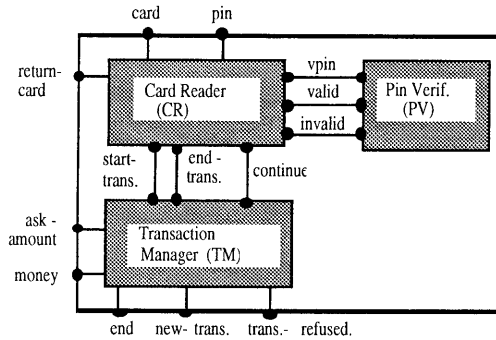
We want to enrich the basic ATM with a new function, money deposit described by the LTS in Figure 10. This function allows the customer to deposit money into his account.

Similarly to the decomposition of the withdrawal function, the deposit function is implemented by three components as shown in Figure 11. The behavior of each of these three components is described by an LTS.

In order to obtain a new ATM providing both of the above functions without any interference among them and preserving the structure of the basic ATM, we apply our algorithm for merging structured specifications. This



**Figure 8.** Basic Automatic Teller Machine.



algorithm will couple and merge the card readers together, the PIN verifiers together and the transaction managers together. The structure of the enriched ATM as well as the behavior of the new components are shown in Figure 12. The behavior of the new ATM is described by the LTS in Figure 13. The sufficient conditions of Theorem 1 and Theorem 2 are satisfied. The behavior of the new ATM is an extension of the basic ATM and *deposit* function, and the new ATM is able to provide, alternatively, the *deposit* and the *withdrawal* function.

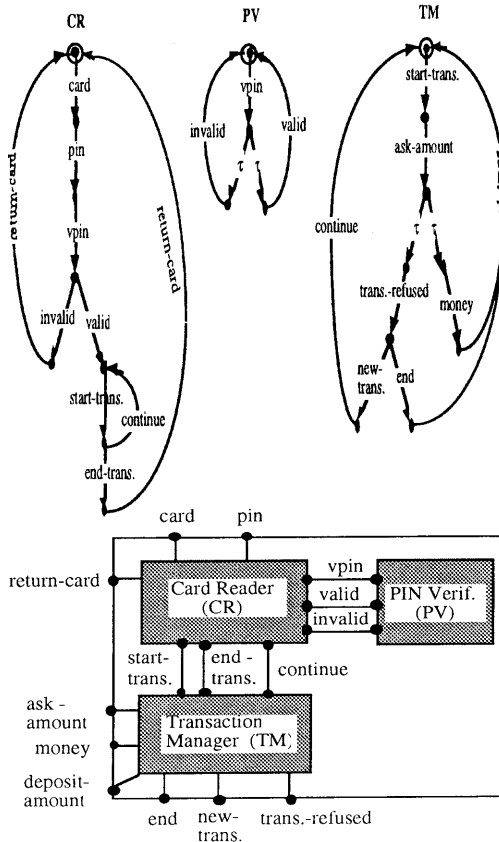


Fig. 9. Structure of the Basic Automatic Teller Machine.

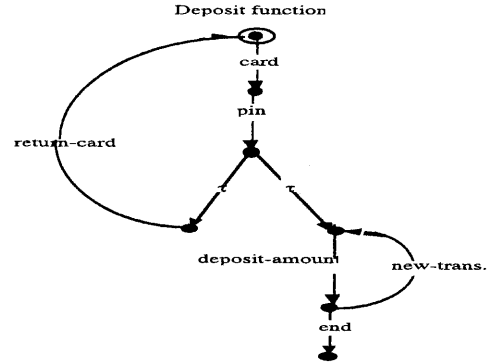


Fig. 10. Deposit function.

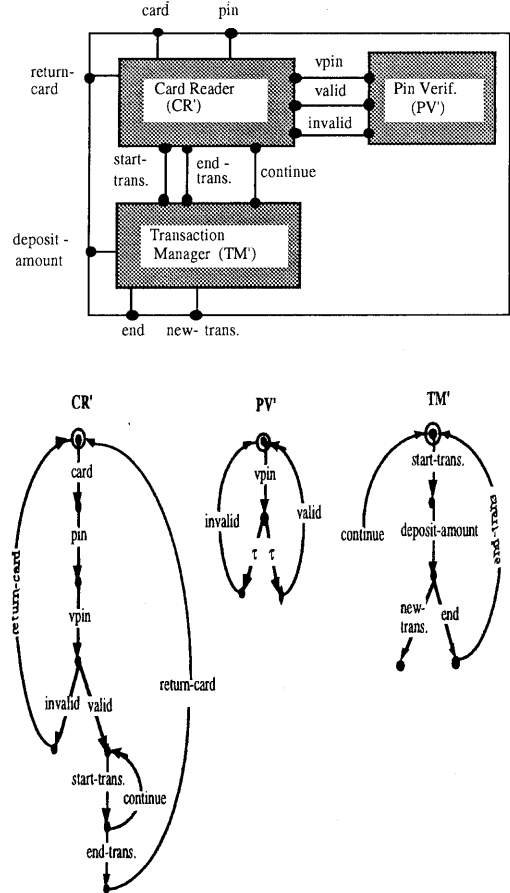


Fig. 11. Decomposition of deposit function.

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