# Detecting Fake QR Codes Using Information from Error-Correction 

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#### Abstract

In 2018, Takita et al. proposed a construction method of a fake $Q R$ code by adding stains to a target $Q R$ code, that probabilistically leads users to a malicious website. The construction abused the error-correction of errorcorrecting code used in the QR code, namely, the added stains induce decoding errors in black and white detection by a camera, so that the decoded URL leads to the malicious website. Also, the same authors proposed a detection method against such fake QR codes by comparing decoded URLs among multiple QR code readings since the decoded URLs may differ because of its probabilistic property. However, the detection method cannot work well over a few readings. Moreover, the proposed detection method does not consider the environmental or accidental changes such as sudden sunshine or reflection, nor recognizes the fake QR code as non-fake when the probability is low. This paper proposes new detection methods for such fake QR codes by analyzing information obtained from the error-correcting process. This paper also reports results from implementing the new detection methods on an Android smartphone. Results show that a combination of these detection methods works very well compared to when using only a single detection method.


Keywords: phishing, QR code, fake, detection, error-correcting code

## 1. Introduction

The spread of the Internet has made cyber attacks a powerful threat all over the world. Among these cyberattacks, the phishing website is popular for attackers to collect IDs and passwords [16]. In the old days, URLs of such phishing websites were directly included in emails to prompt users to access malicious sites but nowadays few users will click on such dangerous links. Then the attackers embed the URLs of the phishing websites in emails, by using HTML email, shorten URL or QR code to make such URLs invisible to users [11] so that users click these links without being aware that they are accessing a phishing website.
QR code [8] is a two-dimensional barcode developed by the DENSO Corporation in 1994, and an international standard in ISO. QR code has become popular because it can handle large amounts of data compared to previous one-dimensional barcodes, and can be easily used with camera-equipped mobile devices so that it is widely used in many applications such as cashless payment services, airline tickets and accessing websites because of its convenience.
The security threats posed by QR codes have been investigated [4]. Among these, leading to phishing websites [17] and distributing malwares [19] are realistic [2]. The naive approach is to prepare the QR code embedding the link to a malicious web-

[^0]site, and use it to replace a legitamate QR code. In fact, a legitimate QR code was covered by a sticker with a malicious QR code on it [15] and a legitimate ticket with a legitimate QR code (issued by a police officer) was replaced by a forged ticket with a malicious QR code [5]. Stickers can be detected physically, but when QR codes are printed on paper or embedded in signboards, detecting such malicious QR codes requires further information beyond the QR code itself. Some countermeasures based on the usable security are studied [1].
A more sophisticated approach is to modify the legitimate QR code printed on a public poster into a malicous one. Kieseberg et al. proposed a construction method by changing white parts to black that deterministically leads users to malicious websites [3]. In 2018, Takita et al. proposed a construction method for a QR code that probabilistically leads users to malicious websites (fake QR code) [6], [12], [14]. The proposed construction abused the error-correction of the error-correcting code used in the QR code, namely, the construction adds stains on a target QR code that induce errors in black and white detection by a camera so that decoding errors are likely (but not always) to occur and the stained QR code may lead users to malicious websites probabilistically. This means that the stains change the luminosity of the center pixels of the modules from the original QR code.

Takita et al. also showed that the probability can be controlled

[^1]by changing the luminosity of the stains and that the probability can be small enough, say $0.6 \%$, experimentally. Since the fake QR code generated by the proposed construction allows users to access legitimate (non-malicious) websites in most cases and malicious websites with a low probability, such fake QR codes will be left without being recognized as "fake". Even if a user is tricked by the fake QR code, accesses the malicious site and then reports the fake QR code, it will prove difficult to find the fake QR code among the many legitimate QR codes because of the low probability of the fake QR code actually functioning.
The proposed construction adds stains around the center pixels of modules in the target QR code, so that the stains can be recognized visually [6], [12], [14]. In order to avoid being noticed visually, the same authors also proposed to use the designed QR code [9], in which colorful images and texts are allowed, since the stains become less conspicuous in such designed QR code [7]. In addition, the same authors proposed another trick by shifting the positions of modules rather than by adding stains to the QR code in order to cause probabilistic decoding error efficiently [13].

The same authors also proposed a detection method against such fake QR codes by comparing decoded URLs obtained from multiple QR code readings from the same camera [13], [14]. If one reading is different from others, then the QR code is recognized as fake because of its probabilistic property. The increase in the processing time is small so that this detection is very convenient for users in the sense that users can avoid fake codes by themselves. However, some problems occur. The proposed detection method does not work well over a few readings. The proposed detection method does not take the environmental (accidental) change such as sudden sunshine or reflection. Especially, the proposed detection method even recognizes the fake QR code as non-fake when the probability is low. Thus, the fake code might still remain without being recognized as fake by the proposed detection method.

This paper proposes new detection methods to determine whether a QR code is fake or not by using the error-correcting process used in the QR code. Specifically, three detection methods are introduced: (1) a detection method using the number of errors (2) a detection method using the locations of errors and (3) a detection method using the symmetry and locality of errors. In addition, this paper reports results from implementing these detection methods on an Android smartphone. The results show that a combination of these detection methods works very well compared to the cases where a single detection method is used.

The rest of the paper is organized as follows: Section 2 introduces specifications of the QR code, and the detailed construction mechanism of a fake code and a previous detection method are described in Section 3. Then in Section 4, the proposed three detection methods are described while taking some considerations into account. Implementation details and experimental results are described in Section 5, and further discussions are summarized in Section 6.

## 2. QR Code

This section briefly describes the specifications of the QR code [8]. The QR code is a two-dimensional barcode for embed-
ding information, and is composed of 2-dimensional cells, called modules, which represent 1-bit information for each.

### 2.1 Module Descriptions

Each QR code has three types of modules: main modules, information modules and supporting modules. Main modules embed the data to be sent to receivers with redundant data for errorcorrection. Information modules embed the format information and the version information defined in the QR code specifications. The format information (such as L (low), M, Q, H, and S (high)) specifies the error correction level used by the errorcorrecting code used in the QR code, namely, Reed-Solomon code ( RS code), while the version information specifies the number of modules in the QR code and takes a value from 1 (small) to 40 (large). For example, version 2 allows $25 \times 25$ modules in a QR code. Supporting modules, such as positioning detection markers, alignment markings, and timing pattern, are modules with fixed patterns for adjusting the direction of the QR code and obtaining the scanning lines of the module when it is scanned. Since we are interested in the data body in this paper, we concentrate on this part in the following.

The data body consists of six individual data, Mode Indicator (MI), Character Count Indicator (CCI), Data Sequence (DS), Terminator $(T)$, and Padding Code (PC), and the redundant data Error Correction Word (ECW) for error-correction. For example, the data body in 2-M type (with version 2 and error correction level M) QR code consists of the following six individual data:

- MI (4-bit): the type of data such as numeric data (0001), alphanumeric data (0010), byte data (0100), or Chinese character data (1000),
- $C C I$ (8-bit): the length of $D S$ in binary,
- $D S$ (at most 26-byte): the body of the data with the size specified by $C C I$,
- $T$ : a padding by 0 s for making $D S$ as a multiple of 8 in binary,
- $P C$ : a padding by repetitions of 236 and 17 if $D S$ is smaller than 26-byte,
- $E C W$ (16-byte): the redundant data computed by RS code from the above five individual data.
In this case, the data body is represented by $M I\|C C I\| D S \| T$ (if necessary) $\| P C$ (if necessary) $\| E C W$, where $\|$ denotes the concatenations.

Figure 1 shows locations of modules corresponding to the above data body, where D1...D28 denotes the first five individual data (in 28-byte), and E1...E16 denotes the error correction words for the 2-M type QR code. Note that each byte has eight modules as shown in the figure. Also note that black and white modules are assigned to information modules and supporting modules.

### 2.2 Reed-Solomon (RS) Code

The QR code uses the Reed-Solomon (RS) code to correct data, which works well against the burst error since the RS code corrects in a symbol-wise way where each symbol consists of bits. In the QR code, each byte is treated as a symbol in the RS code, and modules corresponding to a symbol are placed next to each other


Fig. 1 Module location in a 2-M type QR code.
as in Fig. 1, so that even if multiple adjacent modules are stained by a felt-pen, for example, the errors can be corrected by errorcorrections of a small number of symbols. The message length $k$ is the number of symbols in the information part protected by the RS code, and the block length $n$ is the number of symbols in the entire codeword including the redundant symbols added by the code. In an $[n, k] \mathrm{RS}$ code, the number of correctable errors is computed by the design distance $d=n-k+1$ using the Euclidean decoding, namely, the number of correctable symbols is bounded by $t=\left\lfloor\frac{d-1}{2}\right\rfloor=\left\lfloor\frac{n-k}{2}\right\rfloor$.

The RS code used by the QR code is an RS code over $G F\left(2^{8}\right)$, a finite field with $2^{8}$ elements, using $p(x)=x^{8}+x^{4}+x^{3}+x^{2}+1$ as the primitive polynomial. The elements of $G F\left(2^{8}\right)$ are all the binary polynomials of degree 7 or less. The number of binary polynomials of degree 7 or less is $2^{8}$ since eight coefficients of binary polynomials are 0 or 1 . The list of coefficients of the 7th order, 6th order, ..., and 0th order of a polynomial is called the vector representation of the polynomial. Since the vector representation consists of a binary sequence of length 7 , it is associated with 1 byte of data. Let $\alpha$ be a root of $p(x)$. Using the equation $\alpha^{8}=\alpha^{4}+\alpha^{3}+\alpha^{2}+1$, all polynomials in $G F\left(2^{8}\right)$ are represented by $0, \alpha^{0}, \alpha^{1}, \alpha^{2}, \ldots, \alpha^{254}$. Here, 0 (zero) represents the polynomial 0 (vector representation is 00000000 ), $\alpha^{0}$ represents the polynomial 1 (00000001), $\alpha^{1}$ represents the polynomial $\alpha$ ( 00000010 ), $\ldots, \alpha^{7}$ represents the polynomial $\alpha^{7}(10000000), \alpha^{8}$ represents the polynomial $\alpha^{4}+\alpha^{3}+\alpha^{2}+1(00011101)$, and so on.

Encoding is done by using a generator polynomial. The generator polynomial is given by the following formula;

$$
\begin{equation*}
g(x)=\prod_{i=0}^{2 t-1}\left(x-\alpha^{i}\right) \tag{1}
\end{equation*}
$$

When encoding $k$ message symbols ( $m_{0}, m_{1}, \ldots, m_{k-1}$ ), where the message symbols are in $G F\left(2^{8}\right)$, the message polynomial is the following;

$$
\begin{equation*}
c(x)=m(x) x^{n-k}+\left(m(x) x^{n-k} \bmod g(x)\right) \tag{2}
\end{equation*}
$$

Here, $c(x)$ is a polynomial of degree $n-1$, and the series of $n$ coefficients is the codeword.


Fig. 2 Error correction, error detection, and decoding error.

The Euclidean decoding is generally used for decoders of QR code.

For a 2-M type QR code, the message is $M I\|C C I|\mid D S \| T$ (if necessary) $\| P C$ (if necessary) and the entire codeword is the concatenation of $E C W$ to the above. We have $n=44$ and $k=28$ so that $t=8$ is obtained from the above discussion. In a QR code with $t$ error-correction capability, up to $t$ errors can be corrected, while only error detection or decoded error will occur with more than $t$ error symbols (see Fig. 2). More precisely, if there are more than $t$ symbol errors, a word will be decoded as a wrong symbol if such a codeword exists. If no codeword exists, only error detection is possible.

### 2.3 Example

Let us represent a legitimate URL http://www.u-tokai.ac.jp/ in a 2-M type QR code. The length of the data is 25 , which is smaller than 26, so that Padding Code $(P C)$ is necessary and the number of the message symbols is 28 . Individual data in the data body are as follows:

- MI (4-bit): 0100 (byte data)
- CCI (8-bit): 00011001 (25 in decimal)
- DS (25-byte): http://www.u-tokai.ac.jp/
- $T$ (4-bit): 0000
- PC (1-byte): 236

16-byte ECW are computed from the above message symbols by RS code as described in the previous section. Thus we have the final encoded data as in Table 1, and the corresponding QR code as in Fig. 3.

## 3. Constructing Fake QR Codes

This section describes how to construct a fake QR code that can probabilistically lead users to malicious websites proposed by Takita et al. [6], [12], [14].

### 3.1 Principle

Let $c_{1}$ be a codeword for the QR code corresponding to a legitimate URL, $c_{2}$ be a codeword for the QR code corresponding to a malicious URL, and $d\left(c_{1}, c_{2}\right)$ be the distance (the number of different symbols) between these codewords.

Table 1 QR code example.



Fig. 3 Legitimate QR code.


Fig. 4 Fake QR code.
Firstly, we construct a new sequence $c_{1}^{\prime}$ with $d\left(c_{1}^{\prime}, c_{2}\right)=$ $d\left(c_{1}, c_{2}\right)-a$ for a pre-determined parameter $a(\leq t)$ by adding $a$ errors to the sequence $c_{1}$. Though the error tolerance of the QR code corresponding to the sequence $c_{1}^{\prime}$ becomes low, the sequence $c_{1}^{\prime}$ will be decoded as $c_{1}$ since $a$ is smaller than $t$, so that, as QR code, embedded URL will be decoded successfully if there are no other environmental errors. Furthermore, we construct another new sequence $c_{1}^{\prime \prime}$ with $d\left(c_{1}^{\prime \prime}, c_{2}\right)=d\left(c_{1}^{\prime}, c_{2}\right)-b$ for a predetermined parameter $b$ satisfying $d\left(c_{1}, c_{2}\right)-t \leq a+b \leq d\left(c_{1}, c_{2}\right)$, where a fake QR code is constructed by the sequence $c_{1}^{\prime \prime}$. Then, the sequence $c_{1}^{\prime \prime}$ will be decoded as $c_{2}$ by error correction (decoding error), and thus, as QR code, embedded malicious website will be provided to the user probabilistically. Figure 5 shows relations among these sequences. With this approach, users can be led to a legitimate website in some cases, and to a malicious website in other cases.
Takita et al. add $a$ errors by reversing the black and white of the corresponding modules deterministically, and $b$ errors by changing the luminosity of the center pixel in a module in order to make errors probabilistically [14]. In particular, Takita et al. provide an experimental result in which the relation between the error prob-


Fig. 5 Fake QR code principle.
ability and the degree of the luminosity is shown. The probability of the error is $65.8 \%$ for the luminosity 0 , while the probability is $0.6 \%$ for the luminosity 160 , where 255 corresponds to white. Since the error probability depends on not only the luminosity but the medium on which the QR code is printed or displayed, the brightness of the surroundings, and the performance of the camera, the result does not hold for all circumstances. However, the fact that the error probability may be low makes it difficult for the user to detect such fake QR codes.

### 3.2 Example of a Fake QR Code

As an example, we embed a malicious URL http://www.uyokai.ac.jp/ into a QR code corresponding to a legitimate URL http://www.u-tokai.ac.jp/. As introduced in Section 2, the corresponding sequence for the legitimate URL is

$$
\begin{aligned}
c_{1}= & (65,150,135,71,71,3,162,242, \\
& 247,119,119,114,231,82,215,70 \\
& 246,182,22,146,230,22,50,230 \\
& 167,2,240,236 \\
& 36,111,113,168,84,82,21,223 \\
& 143,148,4,29,86,247,145,151)
\end{aligned}
$$

where the last row is the redundant data for the error-correction. Similarly, the sequence corresponding to the malicious website is

$$
c_{2}=(65,150,135,71,71,3,162,242
$$

$247,119,119,114,231,82,215,150$,
$246,182,22,146,230,22,50,230$,
167, 2, 240, 236,
207, 252, 132, 239, 96, 205, 117, 61,
$\mathbf{3 8}, 171,42,232,175,206,111,215)$,
where bold symbols are different from $c_{1}$ ( 17 symbols). Since 1 letter is different in the URLs and thus all 16 error-correction symbols are changed, the distance between $c_{1}$ and $c_{2}$ is $d\left(c_{1}, c_{2}\right)=$ $1+16=17$, which coincides with the design distance $d=$ $n-k+1=28-12+1=17$, namely the distance is minimum as RS code, so that this sequence pair is likely to provide decoding errors.
Next, we determine locations to set $a$ deterministic errors and $b$ probabilistic errors in order to construct a fake QR code. In the following, we use $a=8$ and $b=1$. Since we need to change more modules when the Hamming distance between the corresponding symbols is large, we want to find a symbol pair between $c_{1}$ and $c_{2}$ whose Hamming distance is minimum ( $>0$ ). Because of this condition, we set deterministic errors on E1 to E8, while the probabilistic error on E16 (whose Hamming distance is 1). In fact, E16 of $c_{1}$ is $151=(10010111)$ and E16 of $c_{2}$ is $215=(11010111)$. Thus, we set $X=(1 ? 010111)$ for E16 of $c_{2}$, where ? denotes the probabilistic bit. Then the sequence $c_{1}^{\prime \prime}$ for the fake QR code is given as shown below.

$$
\begin{aligned}
c_{1}^{\prime \prime}= & (65,150,135,71,71,3,162,242, \\
& 247,119,119,114,231,82,215, \underline{70}, \\
& 246,182,22,146,230,22,50,230, \\
& 167,2,240,236,
\end{aligned}
$$

$\underline{207}, \underline{252}, \underline{132}, \underline{239}, \underline{96}, \underline{205}, \underline{117}, \underline{61}$,
$143,148,4,29,86,247,145, \underline{X})$
Note that the underlined symbols are different from $c_{1}$.
By then encoding this sequence into the QR code, we obtain the false QR code as shown in the example in Fig. 4. Here, the probabilistic error is provided by changing the luminosity of a module, namely, a pixel with the given luminosity is placed at the center of a white module so that this (almost) white module (0) can be misidentified as black (1) probabilistically.
In the above example, only one probabilistic error was added in order to occur the decoding error surely. When more probabilistic errors are added, the generated sequence is likely to be out of the sphere with center $c_{1}$ or $c_{2}$, and the decoding error may not work. However, since some QR code readers are designed to retry when the error is detected, it is possible to construct a fake QR code even if probabilistic errors are added to multiple symbols. On the other hand, more reading time will be needed.

### 3.3 Detection Methods by Takita et al.

A naive countermeasure for fake QR codes is to erase recognized stains by image processing. However, this approach cannot counter other tricks such as shifting module positions rather than adding stains to the QR code as proposed in Ref. [13]. In addition, since this cannot distinguish whether the stains came from
the fake QR code or other reasons, we cannot detect the fake QR code.

Takita et al. also proposed detection methods for a fake QR code [13], [14]. The first detection method utilizes additional information in addition to the QR code. For example, when a QR code is printed on a brochure, the embedded URL will be also printed in letters. Takita et al. proposed comparing the decoded URL and the printed URL, where the fake code can be detected manually. This may work to a certain degree but is a very limited method. Especially, the detection will not be possible when no additional information is provided.

Another detection method is scanning the QR code multiple times and jump to the link when all decoded URLs are the same. This works better than the above detection method and is convenient for users. Still, some problems remain. The first problem is that the detection does not work well for a few readings. Since the error probability can be controlled and can be $10 \%$, for example, at least 10 scans are required to detect the fake QR code. Secondly, the detection is affected by environmental factors. The detection method is susceptible to an environmental change such as weather, sunshine, or change of the angle. The last and the greatest problem is that if the fake QR code is not detected by the detection method, which is likely to occur especially when the error probability is low, then the fake QR code will remain.

## 4. New Detection Methods

As introduced in Section 3.3, previous detection methods proposed by Takita et al. have limitations. Since the construction of the fake code is artificial, the locations of corrected symbols have common characteristics. In this section, we propose new detection methods against fake QR codes by using information obtained from error-correction. More precisely, we propose three detection methods: (1) a detection method using the number of errors (2) a detection method using the locations of errors and (3) a detection method using the symmetry and locality of errors. In addition, we propose a combined detection method of these detections.

### 4.1 Detection Method Using the Number of Errors

The decoding process of the RS code used in the QR code consists of the following steps:
Step 1 Compute the syndrome from the received codeword,
Step 2 Compute the error-polynomial from the syndrome,
Step 3 Compute the error locations from the error-polynomial,
Step 4 Compute the number of corrected symbols from the error evaluating polynomial,
Step 5 Output the decoded result with error-corrections, so that the number of the corrected symbols (errors) is obtained from Step 4. Therefore, this number can be used for the detection against the fake QR code.
In the fake QR code construction introduced in Section 3, deterministic and probabilistic errors are added to the codeword corresponding to the legitimate URL. In order to make the decoding error occur, the number of the probabilistic errors $b$ is chosen to be small, while the number of the deterministic errors $a$ is large. Thus the number of corrected symbols equals or is larger than $a$
when the fake QR code is scanned, which can be used to distinguish between legitimate or fake QR codes. One way is to prepare a threshold $a^{\prime}$ in advance, and make a warning when the number of corrected symbols in the decoding process is larger than $a^{\prime}$ in order to detect the fake QR code. This detection method will be suitable for cases where the environmental errors are unlikely to occur such as in the daytime, with little stains and tears on the QR code.

When the number of deterministic errors $a$ is small and the probabilistic errors $b$ is large, the above approach does not work well. In this case, another threshold works as well. For $b$ probabilistic errors, denote the each error probability as $p_{1}, p_{2}, \ldots, p_{b}$. Assume that $a$ deterministic errors and $b$ probabilistic errors are added to the legitimate sequence and $a+b$ errors are required to make the detection error occur. The probabilty of making the decoding error occur or namely leading the user to a malicious website is $\prod_{i=1}^{b} p_{i}$, which is much smaller than each of $p_{1}, p_{2}, \ldots, p_{b}$ since they all are probabilistic variables. For example, when $b=4$, and each error probability is set to be 0.2 , the probability of occurring the decoding error is $0.2^{4}=0.0016$. In such cases, the number of corrected symbols is likely to be different in each scan, which can be used as another threshold for detecting the fake QR code. In fact, in the above setting, the number of errors can be $a+0$ with a probability of $0.4096, a+1$ with $0.4096, a+2$ with $0.1536, a+3$ with 0.0256 , and $a+4$ with 0.0016 , so that the number of errors will vary from $a+0$ to $a+4$ in each scan. Thus, the detection method based on the number of corrected symbols is valid even for a smaller $a$.

### 4.2 Detection Method Using Locations of Errors

As described in the previous subsection, not only the number of corrected symbols, but the locations of corrected symbols (errors) can be obtained from the error-correcting process. Therefore, it is possible to use the location information for detecting fake QR codes as well.

Let us observe the sample fake QR code described in Section 3.2. When the fake QR code is scanned, and if the probabilistic error does not occur, the legitimate sequence $c_{1}$ will be decoded from the fake sequence $c_{2}$. This is because error symbols are corrected from other symbols of namely the underlined symbols in $c_{1}^{\prime \prime}$. If the probabilistic error does occur, the malicious sequence $c_{1}^{\prime}$ will be decoded from the fake sequence $c_{2}$, by correcting error symbols by other symbols, namely, bold symbols in $c_{2}$ but not underlined in $c_{1}^{\prime \prime}$. In any cases, most error symbols are in the error-correction part. In fact, this is one of the distinguishing features of the fake QR codes. In the construction of the fake QR codes by Takita et al., the difference between a legitimate URL and a malicious URL is set to be small in order to make the fake URL hard to notice. Thus the error symbols are generally gathered in the error-correction part.

For detecting the fake QR codes, we count the numbers of corrected symbols in the error-correction part and in other parts, and compare with a threshold (determined in advance) to decide whether the scanned QR code is fake or not.

Note that, in practice, since the error-correction modules are located together in a QR code, there will be a case when natu-


Fig. 6 Difference of errors.
ral errors are gathered to the error-correction part, for example, a burst error on the error-correcting modules by a felt pen. The above detection method might possibly recognize this natural error as a fake. However, in such cases, the ratio of errors in the error-correction part will be very high so that treating a too high ratio case as non-fake by another threshold will work.

### 4.3 Detection Method Using the Symmetry and Locality of Errors

When errors occur on a QR code printed on a sheet of paper, there may be a series of errors, such as a specific region is stained by a felt pen, a part of the paper is torn, a finger is captured when scanned (see Fig. 6, for example). On the other hand, in the construction of the fake QR code, locations of errors are generally scattered. The difference between such natural and artificial error patterns can be used as a detection of fake QR codes. Especially, in the natural case, all erroneous modules are likely to be all black (1) or white (0) because of its nature, which can be used as a detection method against the fake QR code.
We demonstrate a typical example of a detection method using the error pattern. Here, $E 1$ of the fake QR code in Section 3.2 is $207=(11001111)_{2}$. If the Fake QR code is decoded to the original QR code, then the $E 1$ is decoded from 207 to $36=(00100100)_{2}$. Then, the modules corresponding to two of the most significant bits are changed from black (1) to white (0), and the modules corresponding to the 3rd, 5th, 7th, and 8th are changed from white (0) to black (1). The mixed error patterns are not natural error patterns for a QR code printed on a sheet of paper. Similarly, when the fake QR code is decoded to the QR code of the malicious URL, then the $E 1$ is decoded from $243=(10001111)_{2}$ to $38=(00100110)_{2}$. This case also occurs in the mixed error patterns. Therefore, as a detection against the fake QR codes, we count the numbers of symbols in which the mixed error patterns have occurred, and compare with a threshold (determined in advance) to decide whether the scanned QR code is fake or not.

## 5. Implementation

This section describes implementation details and results of
the proposed detection methods. We actually implemented a QR code reader application on Android with ZXing library [18], which is an open-source, multi-format 1D/2D barcode image processing library.

### 5.1 Implementation Details

### 5.1.1 Detection Method Using the Number of Errors

This detection method uses the number of corrected symbols (errors) which has appeared in the error-correction process in the RS code or namely the fake QR code is detected if the number of corrected symbols is larger than a threshold. This threshold is bounded by the number of correctable symbols $t$, and as introduced in Section 2, $t$ is computed by the number of entire symbols $n$ and the number of symbols in the information part $k$ by $t=\left\lfloor\frac{n-k}{2}\right\rfloor$. Since $n, k$ are embedded in the QR code, the values of these parameters are obtained and computed easily. Implementation results are as follows: note that we use the ratio $r_{1}$, the number of corrected symbols over $t$, is used as a threshold for simplicity.

1. Set a value of the threshold $T_{1}$ from 0 to 1 .
2. Obtain $n$ and $k$ from the QR code.
3. Compute $t$ from $n$ and $k$.
4. Obtain the number of corrected symbols $n_{1}$ from the errorcorrection process.
5. Compute the ratio $r_{1}=n_{1} / t$.
6. Output "fake" if $r_{1}>T_{1}$ and "non-fake" otherwise.

### 5.1.2 Detection Method Using Locations of Errors

This detection method uses locations of corrected symbols (errors) which have appeared in the error-correction process in the RS code. In other words, the method detects the fake QR code if the number of corrected symbols in the error-correction part is larger than a threshold, which is bounded by $n-k$. Similar to the previous case, values of these parameters are obtained and computed easily. Implementation results are as follows: note that we use the ratio $r_{2}$, the number of corrected symbols in errorcorrection part over the entire number of corrected symbols $n_{1}$, is used as a threshold for simplicity.

1. Set a value of the threshold $T_{2}$ from 0 to 1.
2. Obtain the entire number of corrected symbols $n_{1}$ and the number of corrected symbols in error-correction part $n_{2}$ from the error-correction process.
3. Compute the ratio $r_{2}=n_{2} / n_{1}$.
4. Output "fake" if $r_{2}>T_{2}$ and "non-fake" otherwise.

In order to obtain the number of corrected symbols and their locations, we modify the decode function in the ReedSolomonDecoder class provided by the ZXing library (written in Java language). We show the modified decode function in the below. The number of entire corrected symbols is obtained by sigma.getDegree() in line 29, and locations of corrected symbols are obtained in line 37.

```
public void decode(int[] received, int twoS) throws ReedSolomonException {
    MyGenericGFPoly poly = new MyGenericGFPoly(field, received);
    int[] syndromeCoefficients = new int[twoS];
    boolean noError = true;
    for (int i = 0; i < twoS; i++) {
        int eval = poly.evaluateAt(field.exp(i + field.getGeneratorBase()));
        syndromeCoefficients[syndromeCoefficients. length - 1- i] = eval;
        f (eval != 0) {
        noError = false
    },
byte[] rawByte = new byte[received.length];
```

```
    for (int i = 0; i < received.length; i++){
    rawByte[i] = (byte) received[i];
if (noError)
    MyDataClass.setErrorCount (0);
    return;
\
MyGenericGFPoly syndrome = new MyGenericGFPoly(field
        syndromeCoefficients);
    MyGenericGFPoly[] sigmaOmega =
        runEuclideanAlgorithm(field.buildMonomial(twoS, 1), syndrome,
        twoS),
    MyGenericGFPoly sigma = sigmaOmega[0];
    MyGenericGFPoly omega = sigmaOmega[1];
    int[] errorLocations = finderrorLocations(sigma);
    int[] errorMagnitudes = findErrorMagnitudes(omega, errorLocations);
    crrorPositions = new int[errorLocations.length];
    MyDataClassunt = sigma.getDegree();
    MyDataClass.setErrorCount(errorCount);
    for (int i = 0; i < errorLocations.length; i ++) {
    int position = received.length - 1- field.log(errorLocations[i]);
        if (position < 0) (
        throw new ReedSolomonException("Bad_error_location");
    errorPositions[i] = position
    received[position] = MyGenericGF.addOrSubtract(received[position],
        errorMagnitudes[i]);
    for (int i = 0; i < received.len
    rawByte[i] = (byte) received[i]; i++)}
    f
    Arrays.sort(errorPositions):
MyDataClass.setErrorPositions(errorPositions);
```

)

### 5.1.3 Detection Method Using the Symmetry and Locality of Errors

This detection method uses the symmetry and locality of corrected symbols (errors) which have appeared in the errorcorrection process in the RS code. In other words, the fake QR code is detected if the number of symbols which has occurred the mixed error patterns is larger than a threshold. Implementation results are as follows: note that we use the ratio $r_{3}$, the number of symbols occurred the mixed error patterns over the entire number of corrected symbols $n_{1}$ is used as a threshold for simplicity.

1. Set a value of the threshold $T_{3}$ from 0 to 1 .
2. Obtain the number of entire corrected symbols $n_{1}$ and their locations.
3. Obtain a decoded cordword of the QR code by using the error-correction process.
4. Compare the decoded codeword with the sequence obtained from a camera, and count the number of symbols occurred the mixed error patterns $n_{3}$.
5. Compute the ratio $r_{3}=n_{3} / n_{1}$.
6. Output "fake" if $r_{3}>T_{3}$ and "non-fake" otherwise.

### 5.1.4 Combined Detection Method

Each of the proposed detection methods can potentiall detect the fake QR code. However, it may fail depending on the stains. For example, when a felt pen gives stains on a legitimate QR code, the detection method using the number of errors may judge it as the fake. In order to avoid such false positives, we also implement a combination of the detection methods. In fact, the combined detection method judges as a fake if all three detection methods judge as a fake. This combined detection method will likely avoid occurrence of false positives.

### 5.2 Discussions

In this subsection, we discuss the limitations of the proposed detection methods and possible workarounds.

### 5.2.1 Fake QR Code based on Design QR Code

The "design QR code" is a variation of the QR code with illustrations, letters or logos (QRgraphy is one of the examples of the design QR code [10]). Since such irregular data are recognized

Table 2 Device Specifications.

| Device Name | HUAWEI nova lite 2 |
| :---: | :---: |
| OS | EMUI9.1.0 (Build 9.1.0.205 (C635E6R1P5)) <br> (Original OS based on Android 9.0) |
| CPU | Hisilicon Kirin 659 |
| Memory | 3.0 GB |

Table 3 Conditions for Experiments.

| Illuminance | 69 lux |
| :---: | :---: |
| Distance between target QR code with the camera | 30 cm |
| Size of target QR code | $12 \times 12 \mathrm{~cm}^{2}$ |

as errors in a QR code, a certain number of errors will occur even when the code is not faked. Therefore, when countering such fake QR codes it may seem difficult to distinguish whether the QR code is fake or not by using the number of errors. However, in this case, the detection method by the error locations is effective.

### 5.2.2 Changing Error Locations and Countermeasures

In order to avoid the fake QR code detection method using the error locations, we consider changing the locations of errors from the error-correction part to other parts in a QR code.
Firstly, we consider a method to use the padding part. The padding is used to fill in the data with a specific pattern when the length of the data is not sufficient. According to the specifications of the QR code, 236 and 17 are used to fill in the data. Since these data are included in the data body of the QR code, and can be corrected by the RS code, these data can be used instead of the error-correction part to add errors in order to decrease the ratio of the error-correction part in errors. However, such additions can be detected easily by checking the padding part since it must be a repetition of 236 and 17 in the format.
Another trick is to use the parameter part of the GET method in a target URL. For example, when the legitimate website is http://www.u-tokai.ac.jp/?ABCDEF, it is natural that an adversary set a malicious website as http://www.u-yokai.ac.jp/ ?ABCDEF. However, in the GET method, if such a parameter is invalid, it is automatically moved to a home page such as http://www.u-yokai.ac.jp/ so that the adversary can change the parameter part in the fake QR code. In other words, the adversary can choose a sequence with suitable error numbers and locations to deceive the above detection methods. Alternatively, the HTML anchor \# can be used as such a trick. Currently, it appears difficult to detect such intelligent tricks.

### 5.3 Experimental Results

In order to show the effectiveness of our detection methods and the implementation, we conducted three experiments by using an Android device where our implementation is installed (see Table $\mathbf{2}$ for detail specifications). Note that we used ZXing 3.4.0 for the implementation.
In the following experiments, we print QR codes/Fake QR codes on paper, and scan the QR codes by the camera of a smartphone from the front with the conditions in Table 3.

### 5.3.1 Experiment 1

In the first experiment, we prepare 10 fake QR codes in 2-M type whose legitimate and malicious URLs (lead by the fake QR codes) are shown in Table 4. Then, we scan the fake QR codes

Table 4 List of pairs of legitimate and malicious URLs for Fake QR codes.

| No. | Legitimate URL | Malicious URL |
| :---: | :--- | :--- |
| 1 | http://www.u-tokai.ac.jp/ | http://www.u-yokai.ac.jp/ |
| 2 | http://www.tokai-adm.jp/ | http://www.yokai-adm.jp/ |
| 3 | http://www.fujitsu.com/ | http://www.fukitsu.com/ |
| 4 | http://www.tsukuba.ac.jp/ | http://www.tsukubi.ac.jp/ |
| 5 | http://www.kobe-u.ac.jp/ | http://www.kabe-u.ac.jp/ |
| 6 | http://www.google.com/ | http://www.googlo.com/ |
| 7 | http://www.yahoo.co.jp/ | http://www.yagoo.co.jp/ |
| 8 | http://www.goo.ne.jp/ | http://www.hoo.ne.jp/ |
| 9 | http://www.nifty.com/ | http://www.nefty.com/ |
| 10 | http://zoom.us/ | http://zaom.us/ |

Table 5 Experimental results of detecting Fake QR codes made by Table 4.

| No. | Legitimate URL is decoded |  |  | Malicious URL is decoded |  |  |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- |
|  | $r_{1}$ | $r_{2}$ | $r_{3}$ | $r_{1}$ | $r_{2}$ | $r_{3}$ |
| 1 | 1.00 | 0.88 | 0.88 | 1.00 | 0.88 | 0.75 |
| 2 | 1.00 | 0.88 | 0.75 | 1.00 | 0.88 | 0.63 |
| 3 | 1.00 | 0.88 | 0.75 | 1.00 | 0.88 | 0.75 |
| 4 | 1.00 | 0.88 | 0.88 | 1.00 | 0.88 | 0.75 |
| 5 | 1.00 | 0.88 | 1.00 | 1.00 | 0.88 | 0.75 |
| 6 | 1.00 | 0.88 | 0.63 | 1.00 | 0.88 | 0.63 |
| 7 | 1.00 | 0.88 | 0.88 | 1.00 | 0.88 | 0.88 |
| 8 | 1.00 | 0.88 | 0.88 | 1.00 | 0.88 | 0.63 |
| 9 | 1.00 | 0.88 | 0.88 | 1.00 | 0.88 | 1.00 |
| 10 | 1.00 | 0.88 | 0.88 | 1.00 | 0.88 | 0.63 |

Table 6 Processing Times for Scanning QR Codes.

|  | Original | Our Implementation |
| :--- | :---: | :---: |
| Legitimate QR Code | 40.8 msec | 42.2 msec |
| Fake QR Code | 44.4 msec | 49.8 msec |

and collect the decoded URL, the ratio values $r_{1}, r_{2}, r_{3}$ in order to evaluate the thresholds. Table 5 summarizes the collected results. As in this table, when we set the threshold values as $T_{1}=0.8$, $T_{2}=0.8, T_{3}=0.4$, we can say that all detection methods for all fake QR codes detect the fake successfully independent from the decoded URLs.

### 5.3.2 Experiment 2

In order to evaluate the processing overhead, we measure the processing times of the reading by the original ZXing and by our implementation with the modified ZXing. The two targets of this experiment are the legitimate QR code (Fig. 3) and the fake QR code (Fig. 4). We scanned each QR code 10 times and the averaged times are summarized in Table 6. As seen in this table, the overhead of our methods is sufficiently smaller than the processing of the original ZXing.

### 5.3.3 Experiment 3

In this experiment, we add stains to the legitimate QR code artificially. We used the following four QR codes in 2-M type for evaluating the implementation. The first QR code is the legitimate QR code (Fig. 3). The other three QR codes are legitimate with three patterns of stains. Pattern 1 (Fig. 7) has small stains in black only, while Pattern 2 has small stains in black and white (Fig. 8). Pattern 3 (Fig. 9) has stains in black and white on the error-correction part, whose number of errors are the maximum number that the RS code can correct. Patterns 1 and 2 are natural stains rather than artificial. The characteristics of Pattern 3 are set similar to that of the fake QR code so that it seems hard to distinguish fake or not.

- Legitimate QR code (Fig. 3).
- Legitimate QR code with stains: Pattern 1 (Fig. 7).


Fig. 7 Legitimate QR code (with small black stains).


Fig. 8 Legitimate QR code (with small black and white stains).


Fig. 9 Legitimate QR code (with black and white correctable stains).
Table 7 Experimental Results ( $T_{1}=0.8, T_{2}=0.8, T_{3}=0.4$ ).

|  | $r_{1}$ | $r_{2}$ | $r_{3}$ | Combination |
| :---: | :---: | :---: | :---: | :---: |
| Legitimate (Fig. 3) | 0.00 | 0.00 | 0.00 | Legitimate |
| Legitimate (pattern 1, Fig. 7) | 0.50 | 0.25 | 0.00 | Legitimate |
| Legitimate (pattern 2, Fig. 8) | $\mathbf{1 . 0 0}$ | 0.13 | 0.13 | Legitimate |
| Legitimate (pattern 3, Fig. 9) | $\mathbf{1 . 0 0}$ | $\mathbf{1 . 0 0}$ | $\mathbf{0 . 7 5}$ | Fake |

- Legitimate QR code with stains: Pattern 2 (Fig. 8).
- Legitimate QR code with stains: Pattern 3 (Fig. 9).

Table 7 shows the results of our experiments, where the second column denotes the ratio $r_{1}=n_{1} / t$, for the number of errors $n_{1}$ and the number of correctable symbols $t$, the third denotes the ratio $r_{2}=n_{2} / n_{1}$, for the number of errors in error-correction part $n_{2}$ and the above $n_{1}$, the fourth denotes the ratio $r_{3}=n_{3} / n_{1}$, for the numbers of symbols occurred the mixed error patterns $n_{3}$ and the above $n_{1}$, and the last column denotes the output of the combinatorial approach. Bold values are beyond the thresholds so that the QR codes are judged as fake. Here, we use values $T_{1}=0.8$, $T_{2}=0.8, T_{3}=0.4$ for the thresholds.

According to the experimental results, the fake QR code was detected by all three detection methods and thus by the combination of methods. On the other hand, Pattern 2 was misdetected by the number of errors method, and Pattern 3 was misdetected by all methods. For Pattern 2, the other detection methods work well so the combination of 3 detection methods is effective. However, for Pattern 3, it seems hard to avoid the misdetection in the current approach.

## 6. Concluding Remarks

This paper proposed three detection methods for fake QR codes and a combination of these detection methods. Specifically, by observing the information obtained from the error-correction, we proposed the use of the number of corrected symbols (errors), locations of corrected symbols (errors), the symmetry and the locality of errors (error patterns), and their combination. As far as we were able to observe, our detection methods performed well in the experiments. However, the issue remains that none of the proposed detection methods correctly detected certain stained QR code. Further investigation is required to clarify the performance of our detection methods.

In this paper, we only discuss the case when providing probabilistic errors by adding a stain at the center of a module with different luminosity values. We believe that both the detection method using the number of errors and the detection method using the error locations are valid when probabilistic errors are provided by shifting the position of the module.

## Research Ethics and Disclosure

Since this relates to attacks against the QR code which is widely used in the real world, we discuss the impact of our research on services and products that utilize the QR code. The construction method of fake QR codes has been published in Refs. [6], [12], [14], and the detection method for the attack, which directs users to the malicious website, was given in Refs. [13], [14]. The purpose of this paper is to provide advanced security against fake QR codes. Namely, the proposed detection methods determine whether a QR code is fake or not in order to remove potential threats from fake QR codes. We therefore believe that none of the contributions provided by this paper pose additional threats to currently used QR codes or services and associated products.

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## Editor＇s Recommendation

The authors of this paper proposed，implemented，and evalu－ ated defense schemes against existing spoofed QR code attacks． Their experimental results clearly demonstrated that the proposed schemes can detect the attacks with high accuracy．The authors also evaluated the detection accuracy in a realistic situation where stains are added to the QR code，deriving the practical findings． The theme addressed in this paper is about attacks using QR codes，which are widely used in our life，and the research ethics that should be taken into consideration as security research are fully discussed in the paper．For these reasons，we have selected this paper as our recommended paper．
（Program Chair of the Computer Security Symposium 2020， Tatsuya Mori）


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