# An Easy-Hard-Easy Cost Profile in Distributed Constraint Satisfaction

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We first present an algorithm called multi-ABT as a baseline algorithm for solving distributed constraint satisfaction problems where each agent has multiple local variables. Then, we show a cost profile of multi-ABT for various numbers of intra-agent constraints (constraints defined over variables of one agent) and *inter-agent constraints* (constraints defined over variables of multiple agents) in a distributed graph-coloring problem. This cost profile enabled us to make the following observations: (1) the satisfiability thresholds are identified in the narrow region on the x-y plane (where the x-axis is the number of intra-agent constraints and the y-axis is the number of inter-agent constraints) in which the sum of intra- and interagent constraints is constant, and problem instances in the region (called the *crossover belt*) are likely to be expensive in terms of the median cost; (2) among problem instances on the crossover belt, those with a smaller number of intra-agent constraints and a larger number of inter-agent constraints may be more expensive; and (3) for a fixed total number of variables, problem instances on the crossover belt may be more expensive as the number of agents increases or the number of variables per agent decreases. Our further experiments suggest that these observations can be generalized to cases where different algorithms are applied or different sets of parameters of the problem are used.

## 1. Introduction

Many problems in artificial intelligence can be formalized as constraint satisfaction problems (CSPs). A CSP instance consists of variables with finite and discrete domains and constraints over subsets of variables. A solution to a CSP instance is a set of values for the variables that satisfies all of the constraints.

CSPs are typical NP-complete problems, and thus it has been said that no algorithm has a worst-case search cost that is not exponential in relation to the size of the problem. However, recent studies have observed that for certain CSPs, such as the propositional satisfiability problem, the graph-coloring problem, and the binary CSP, an order parameter exists on which the median computational costs of algorithms show an *easy-hard-easy* cost profile  $^{2),11),15)}$ . The search cost grows very rapidly when the problem size increases in the hard region on the parameter, but relatively slowly in the other regions on  $it^{3}$ . In other words, really computationally expensive problem instances are concentrated on some specific region of the parameter.

For example, in the graph-coloring problem, an instance of which consists of a graph, a specified number of available colors, and the requirement to find a color for each node of the graph such that no adjacent nodes have the same color, such an order parameter is the ratio of the number of links to the number of nodes. For randomly generated instances of the graph 3-coloring problem, it has been shown that the peak of the median computational cost is located at 2.3, i.e., where the number of links is 2.3 times as many as the number of nodes<sup>8</sup>.

Distributed CSPs (DisCSPs)  $^{17),18}$  are CSPs where variables and constraints are distributed among multiple agents, each of which tries to solve its own problem. Various application problems in multi-agent systems that are concerned with finding a consistent combination of agent actions (e.g., the distributed resource allocation problem<sup>4)</sup>, the distributed scheduling problem<sup>16)</sup>, the distributed interpretation task<sup>10)</sup>, and the multi-agent truth maintenance task<sup>9)</sup>) can be formalized as DisCSPs.

Recently, several researchers have developed distributed constraint satisfaction algorithms  $^{1),7),14},^{18}$ ,  $^{20)}$ . In a distributed constraint satisfaction algorithm, since an agent usually has *intra-agent constraints* (constraints defined over variables of one agent) and *interagent constraints* (constraints defined over variables of multiple agents), an agent must not only perform local computation to satisfy its intra- and inter-agent constraints but must also communicate with other agents to satisfy its

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inter-agent constraints. We can therefore assume that the cost of a distributed constraint satisfaction algorithm can vary with the numbers of intra- and inter-agents constraints. Our goal is to understand how the numbers of intraand inter-agent constraints affect the cost of a standard distributed constraint satisfaction algorithm, since such information may provide a hint for formulating some problems as DisCSPs and designing more efficient distributed constraint satisfaction algorithms.

In this paper, we first present an algorithm called *multi-ABT*, which is an extension of the asynchronous backtracking algorithm  $(ABT)^{18}$ , as a baseline algorithm for solving DisCSPs where each agent has multiple local variables. Then, we show a cost profile of multi-ABT for various numbers of intra- and inter-agent constraints in the distributed graphcoloring problem. As we will show in this paper, the cost profile exhibits an interesting pattern on the x-y plane (where the x-axis is the number of intra-agent constraints and the yaxis is the number of inter-agent constraints), and the pattern is closely related to the satisfiability thresholds where the ratios of solvable problem instances rapidly change from one to zero. Since the pattern seems independent of algorithms and instance generation methods, we expect that our results could serve as the basis of further theoretical or experimental analyses.

This paper is organized as follows. In Section 2, we provide a general definition of the DisCSPs and give an instance of the distributed graph-coloring problem. In Section 3, we present multi-ABT as a baseline algorithm for solving DisCSPs where each agent has multiple local variables. In Section 4, we describe the details of our experimental settings and results. Finally, in Section 5, we conclude our discussion and outline our plans for future work.

## 2. Distributed Constraint Satisfaction Problem

A CSP instance consists of variables with finite and discrete domains and constraints over subsets of the variables. A constraint can be represented as a predicate that is defined over some variables' domains and becomes true when the constraint is satisfied and false otherwise. A solution to a CSP instance is a set of values for the variables that satisfies all of the constraints.

The DisCSPs is the CSP where variables

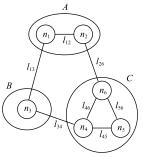


Fig. 1 Instance of the distributed graph coloring problem.

and constraints are distributed among multiple agents. A DisCSP instance consists of the following:

- a set of agents  $1, 2, \ldots, k$
- a set of CSP instances  $P_1, P_2, \ldots, P_k$  such that  $P_i$  belongs to agent i  $(i = 1, \ldots, k)$

A solution to a DisCSP instance is the state where all of the agents find solutions to their own CSP instances. We usually assume that each agent has a CSP instance that includes inter-agent constraints. An *inter-agent constraint* is a constraint that is defined over variables of multiple agents. On the other hand, an *intra-agent constraint* is a constraint that is defined over variables of one agent. Consideration of inter-agent constraints complicates the search process over DisCSPs, because communication is required among agents to satisfy those constraints.

Figure 1 illustrates an instance of the distributed graph-coloring problem. In this problem, nodes are partitioned among agents and a link is assigned to the agent(s) having a node that is involved in the link. It is known that the scheduling problem in a distributed sensor network can be formulated as the distributed graph-coloring problem  $^{12),21)}$ . In Fig.1, each of the three agents A, B, and C has nodes in the corresponding ellipse and links that are connected to the nodes. For example, agent A has the nodes  $n_1$  and  $n_2$  and the links  $l_{12}$ ,  $l_{13}$ , and  $l_{26}$ . In other words, agent A has a CSP instance with the variables  $n_1$ and  $n_2$  and the constraints not\_equal $(n_1, n_2)$ , not\_equal $(n_1, n_3)$ , and not\_equal $(n_2, n_6)$ . Note that there are 7 links (constraints) in this figure, of which three,  $l_{13}$ ,  $l_{34}$ , and  $l_{26}$ , are inter-agent constraints, and the other four,  $l_{12}$ ,  $l_{45}$ ,  $l_{46}$ , and  $l_{56}$ , are intra-agent constraints.

## 3. Multi-ABT

The asynchronous backtracking algorithm (ABT) belongs to the first generation of distributed constraint satisfaction algorithms, and is basically designed for solving DisCSPs where each agent has exactly one local variable  $^{18)}$ . Although several researchers have been trying to extend ABT in various directions  $^{1),14),18)}$ . not much effort has been made to extend ABT in such a way that it can explicitly handle DisC-SPs where each agent has multiple local variables. Therefore, as a baseline algorithm for such problems, we present multi-ABT in this paper. This algorithm is basically similar to ABT, but differs in that it can explicitly handle DisCSPs where each agent has multiple local variables. Figure 2 shows the main part of this algorithm (the procedure to be followed when an agent receives an ok? message). The outline of this algorithm is as follows. Note that we are using graph-coloring terminology.

• A priority order among agents is intro-

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when received (ok?, (sender, node, color)) do
  add (sender, node, color) to agent_view;
  L := an ordered list of all nodes within this agent (descending
      order of priority);
  N := null:
  if check_nodes(L, N) then
    wait for a next message;
  else
    broadcast "no solution exists";
end do;
procedure check\_nodes(L, N)
  if L is empty then
    send each nogood in N to the agent whose priority is the lowest
    in the nogood:
    send all changed colors to neighbors;
    return true:
  else
    n := the first node in L;
    if n's color is consistent (with the colors of higher-priority
       agents' nodes and the colors of this agent's higher-priority
       nodes) then
      L := \hat{L} with n deleted; check_nodes(L, N);
    else
      if there is another consistent color, c, for n then
         change n's color to c;
         L := L with n deleted; check_nodes(L, N);
      else
         nogood := a set of nodes' colors causing this conflict;
         if nogood is empty then
           return false;
         else
           if nogood includes nodes of this agent then
             m := the lowest-priority node among these nodes;
             L :=a list of m and all lower-priority nodes than m;
             record nogood as a new constraint;
             check\_nodes(L, N);
           else
             add nogood to N;
             L := L with n deleted; check_nodes(L, N);
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duced such that an agent with more links has higher priority (ties are broken in favor of an agent with a smaller identifier). Also, for each agent, a priority order among (internal) nodes is introduced such that a node with more connected links has higher priority (ties are broken in favor of a node with a smaller identifier).

- Each agent starts the procedure by randomly assigning a color to each of its nodes and sending these colors to *lower-priority neighbors* (a set of lower-priority agents that have nodes included in this agent's inter-agent constraints) via *ok?* messages.
- When an agent receives an *ok?* message, it updates an *agent\_view*, which records the latest colors for nodes of *higher-priority neighbors* (a set of higher-priority agents that have nodes included in this agent's inter-agent constraints), and then executes the following procedure for each of its nodes, say n, in order of node priority.
  - Select a color for n that is consistent with the agent\_view and the colors of this agent's higher-priority nodes, and then move to the next node. If the current color for n is already consistent, do not change that color.
  - If there is no such consistent color for n, generate a *nogood* by using the method described in Hirayama and Yokoo<sup>6)</sup>. A nogood is a set of colors for some nodes under which there is no consistent color for n, and it can be considered a new constraint discovered during algorithm execution. Since no superset of a nogood can be a solution, an empty nogood eliminates all possible colors for nodes. Therefore, an agent can detect the fact that there is no solution if it generates an empty nogood.
  - If any of this agent's nodes are contained in the generated nogood, record the nogood as a new constraint, backjump to the lowest-priority node among those nodes, and reselect colors for the node and its subsequent nodes. On the other hand, if none of this agent's nodes is contained in the generated nogood, keep the current color for n, push the nogood into a *stack*, and move to the next node.

When an agent finishes selecting colors for

all of its nodes, it sends each nogood in the stack via a *nogood* message to the lowest-priority agent among those having nodes in the nogood, and then sends the changed colors to lower-priority neighbors via *ok*? messages.

• When an agent receives a *nogood* message, it records the content of that message as a new constraint and examines all of its nodes in the same way as described above. Note that when a received nogood includes an unknown node that belongs to a non-neighboring agent, an agent requests the non-neighboring agent to keep informed about a color for the node.

Since agents record all nogoods discovered in their concurrent search processes, this algorithm is complete, that is, it can reach a solution if a problem instance has at least one solution, or it can establish that no solution exists.

#### 4. Experiments

Our next question is how multi-ABT behaves on the space constructed from the numbers of intra- and inter-agent constraints of the distributed graph-coloring problem.

We implemented multi-ABT on a simulator of a synchronous distributed system. A synchronous distributed system is a model of a distributed system, in which every agent synchronously performs the following cycle: (1)receive all of the messages that were sent to the agent in the previous cycle and (2) perform local computation to change its internal state and determine the contents of messages and then send those messages to other agents. Although multi-ABT can work on any type of distributed system, we assumed a synchronous distributed system in this study, since it is one of the simplest distributed systems and we wanted to make the underlying distributed system simple in order to focus on the characteristics of the algorithm. We would like to point out that a similar simulator has traditionally been used to evaluate the performance of distributed constraint satisfaction algorithms<sup>17),18)</sup>.

Using this simulator, we measured *cycles* and *maxccks* as the costs of an algorithm. The value of *cycles* represents the number of iterations in which the agents concurrently perform local computation until an algorithm is terminated. This measure has been conventionally used to estimate the cost of distributed constraint satisfaction algorithms  $^{17),18}$ . We should, however,

notice that the number of cycles is completely unrelated to how much computational effort an individual agent makes in one cycle. Such computational effort must be considered when an agent has multiple local variables along with some intra- and inter-agent constraints, since it would impose a non-negligible cost on an algorithm. Therefore, we introduce another measure, maxccks, representing the total sum of the maximum number of consistency checks over the agents in each cycle until the algorithm is terminated. More specifically, the value of maxccks is measured as follows: in each cycle we identify a bottleneck agent that performed the most consistency checks among the agents and sum up all of those maximum numbers of consistency checks over the running cycles.

Several parameters are used to specify an instance of the distributed graph-coloring problem, such as the number of agents, the number of nodes, and the average number of nodes per agent. Since our goal is to clarify the relation between the cost of algorithms and the numbers of intra- and inter-agent constraints, we varied the numbers of intra- and inter-agent constraints while keeping the other parameters constant. In our experiments, we randomly generated an instance of the distributed graphcoloring problem using the method in **Fig. 3**, where the inputs are the number of nodes, the number of available colors for a node, the number of agents, and the numbers of intra- and inter-agent constraints.

We first set the number of nodes to 100 and

<b>INPUTS:</b> # of nodes $(n)$ , # of available colors for a node $(c)$ , # of agents $(k)$ , # of intra-agent constraints $(x)$ , # of inter-agent constraints $(y)$ ;
<b>OUTPUT:</b> an instance of the distributed graph-coloring problem;
Step 1 Distribute $n$ nodes each with $c$ available colors among $k$ agents such that these agents have numbers of nodes that are as nearly equal as possible;
<b>Step 2</b> Define each of $x$ intra-agent constraints as follows:
<b>Step 2.1</b> Randomly select one agent from $k$ agents;
Step 2.2 Randomly select two nodes from those belonging to the selected agent to define a link between them. If there already exists a link between the nodes, repeat the selection until two nodes with no link are found;
<b>Step 3</b> Define each of $y$ inter-agent constraints as follows:
<b>Step 3.1</b> Randomly select two agents from $k$ agents;
Step 3.2 Randomly select one node each from those belonging to the above two agents to define a link between these two nodes. If there already exists a link between the nodes, repeat the selection until two nodes with no link are found;
Step 4 Accept the graph if it is connected. If it is not connected, delete all of the links and go to Step 2;
<b>Fig. 2</b> Mathed for constituting instances

Fig. 3 Method for generating instances.

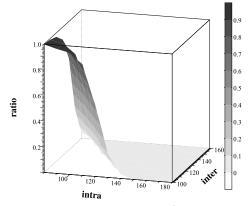


Fig. 4 Ratio of solvable instances (5 agents with 20 nodes each, random 3col).

the number of available colors for a node to 3. Then, we randomly generated instances for two cases — 2 agents with 50 nodes each and 5 agents with 20 nodes each — while varying the numbers of intra- and inter-agent constraints.

Figure 4 shows the ratios of solvable instances for 5 agents with 20 nodes each on the x-y plane. Since the result we obtained for 2 agents with 50 nodes each was very similar, the figure is omitted for reasons of space. For each case, we generated 500 instances at every combination of the number of intra-agent constraints,  $intra \in \{80, 90, \dots, 180\}$ , and the number of inter-agent constraints, inter  $\in$  $\{100, 110, \dots, 160\}$ , and plotted the ratio of solvable instances among 500 instances at each data point. The figure clearly shows that when the numbers of intra- and inter-agent constraints are increased, we can observe a rapid drop from almost one to zero in the ratio of solvable instances. For each case, the region where such a rapid drop occurs lies around  $210 \leq intra + inter \leq 240$  on the x-y plane. We refer to such a region as a *crossover belt*.

Figures 5 and 6 show the median cycles and the median maxccks for 2 agents with 50 nodes each, respectively, and Figs. 7 and 8 show those for 5 agents with 20 nodes each, respectively. We can observe the following from these results.

**Observation 1:** Both the median cycles and the median maxccks on the crossover belt are higher than those in the other regions. For each of these figures, we can see that there is a "ridge" along the crossover belt and that the top of the ridge lies around  $230 \leq intra + inter \leq$ 240 on the x-y plane, which corresponds to the

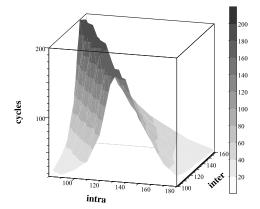


Fig. 5 Median cycles (2 agents with 50 nodes each, random 3col, with multi-ABT).

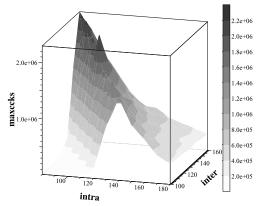


Fig. 6 Median maxccks (2 agents with 50 nodes each, random 3col, with multi-ABT).

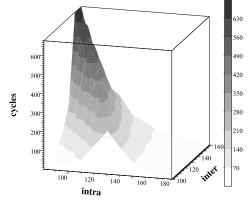


Fig. 7 Median cycles (5 agents with 20 nodes each, random 3col, with multi-ABT).

region where the ratios of solvable instances are roughly between 0.3 and 0.

According to Hogg and Williams<sup>8)</sup>, for randomly generated instances of the (centralized) graph 3-coloring problem, the median computation cost of a depth-first backtracking search

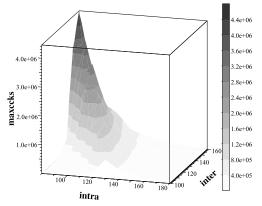


Fig. 8 Median maxceks (5 agents with 20 nodes each, random 3col, with multi-ABT).

with the Brelaz heuristic rises to a peak when the ratio of the number of links to the number of nodes is 2.3, and the location of the peak coincides with the point at which the ratio of solvable instances is 0.5. In our experiments, although we used a distributed constraint satisfaction algorithm, we can observe a basically similar result, where the top of the ridge of the median cost appears when the ratio of the total number of links (*intra* + *inter*) to the number of nodes (100) is about 2.3 or 2.4. Its location, however, does not coincide with the region where the ratio of solvable instances is 0.5.

**Observation 2:** When the number of intraagent constraints decreases and the number of inter-agent constraints increases, the top of the ridge becomes higher.

This implies that the instances on the crossover belt are not uniformly hard. Among the instances on the crossover belt, those with a small number of intra-agent constraints and a large number of inter-agent constraints tend to be expensive both in terms of cycles and max-ccks.

The increase in cycles in that direction could be explained as follows. When solving an instance with a small number of intra-agent constraints and a large number of inter-agent constraints, an agent is likely to select misleading colors for its nodes, that is, colors that appear to be correct from its local point of view but actually are incorrect from the global point of view. Once an agent (especially a higherpriority agent) selects such misleading colors, other agents have to perform a considerable amount of search to make the agent change the misleading colors, and thus the number of cycles grows in such an instance.

On the other hand, the increase in maxccks could be explained as the result of two competing effects: a decrease in the computational cost of a cycle and an increase in the total number of cycles. For a problem instance with a small number of intra-agent constraints and a large number of inter-agent constraints, the computational cost of a cycle decreases, because an agent tends to perform nogood sending rather than internal backjumping. On the other hand, as mentioned above, we see that the total number of cycles can increase in such an instance. These two phenomena might have conflicting effects on maxccks, but our experimental result shows that the latter overrides the former, leading to an increase in maxccks in that direction.

This result might offer some insight into how to describe a problem as a DisCSP instance. If possible, we should make local problems tight (by increasing intra-agent constraints) and global problems loose (by decreasing interagent constraints) in order to reduce the costs of algorithms.

**Observation 3:** The top of the ridge has a steeper slope for 5 agents with 20 nodes each than for 2 agents with 50 nodes each. As a result, the former case has a higher peak.

For example, for 5 agents with 20 nodes each, the maximum and minimum cycles of the top of the ridge are 680 (at *intra* = 80 and *inter* = 160) and 232 (at *intra* = 130 and *inter* = 100), respectively, and for 2 agents with 50 nodes each they are 200 (at *intra* = 80 and *inter* = 150) and 170 (at *intra* = 130 and *inter* = 100), respectively. This result implies that the misleading colors mentioned above can have a great impact on the entire performance if the number of agents increases or the number of nodes per agent decreases.

This result might also offer some insight into how to describe a problem as a DisCSP instance. If possible, we should make local problems large (or equivalently reduce the number of agents) in order to reduce the costs of algorithms.

In order to test the generality of our findings, we conducted more experiments using other combinations of problem settings and algorithms. First, we conducted experiments for solvable instances of the distributed 3-coloring problem when using multi-ABT and multi-AWC  $^{20}$ . The results of these experiments are shown in **Figs. 9** and **10** (median cycles of 500 instances for 5 agents with 20 nodes each). A

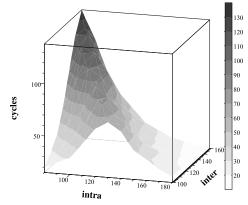


Fig. 9 Median cycles (5 agents with 20 nodes each, solvable 3col, with multi-ABT).

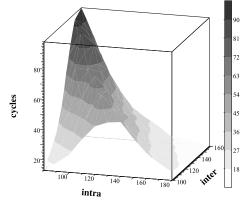


Fig. 10 Median cycles (5 agents with 20 nodes each, solvable 3col, with multi-AWC).

solvable instance was generated using a method similar to that in Fig. 3, but modified to be able to specify a solution in advance and avoid any link that would eliminate the solution. For each case we can observe a ridge in almost the same region as in Figs. 5–8, and the qualitative characteristics of the cost profile were consistent with our findings. Next, we conducted another experiment for random instances of the distributed 4-coloring problem when using multi-The method used to generate an in-ABT. stance was the same as the one in Fig. 3, except that we set the number of available colors for a node to 4. A cost profile (median cycles of 500 instances for 5 agents with 10 nodes each) is shown in Fig. 11. We again found a qualitatively similar pattern, where the top of the ridge was around  $200 \leq intra + inter \leq 210$ and became higher when the number of intraagent constraints decreased and the number of inter-agent constraints increased.

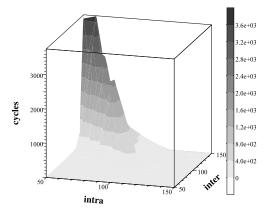


Fig. 11 Median cycles (5 agents with 10 nodes each, random 4col, with multi-ABT).

## 5. Conclusions and Future Work

In this paper, we have presented multi-ABT as a baseline algorithm for solving distributed constraint satisfaction problems where each agent has multiple local variables, and shown a cost profile of multi-ABT for various numbers of intra- and inter-agent constraints in the distributed graph-coloring problem. From our experimental results, we can conclude that a really hard DisCSP instance is the one on the crossover belt where each agent has a limited amount of knowledge of the instance, that is, a small number of intra-agent constraints and a small number of variables per agent. This view may be helpful not only in formulating some application problems as DisCSP instances, but also in developing effective strategies, especially for distributed constraint satisfaction algorithms where agents are allowed to enlarge (or join) their local problems during algorithm execution  $^{5),13)}$ .

Obviously, much still remains to be done to obtain a more accurate picture of the cost profiles of distributed constraint satisfaction algorithms.

As with most of the work on the cost profiles of centralized constraint satisfaction algorithms, this work has concentrated on specific cases where multi-ABT and multi-AWC, which we believe are standard distributed constraint satisfaction algorithms, are applied to the distributed graph-coloring problem. However, in order to strongly confirm the findings, we may need to conduct more experiments using other combinations of algorithms and problems.

Also, as with most of the previous work, the terms "easy" and "hard" are intuitively used in this work. Recently, a detailed investigation of a phase transition in computational complexity, namely, the complexity shifts from polynomial (easy) to exponential (hard) in the order, has been reported for the random 3-SAT problem<sup>3)</sup>. It may be interesting to explore where such complexity shifts occur on the x-y plane for multi-ABT and multi-AWC.

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